Scalability of Quasi-Hysteretic FSM-Based Digitally Controlled Single-Inductor Dual-String Buck LED Driver to Multiple Strings

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***Abstract*—There has been growing interest in single-inductor multiple-output (SIMO) dc–dc converters due to its reduced cost and smaller form factor in comparison with using multiple single-output converters. An application for such a SIMO-based switching converter is to drive multiple LED strings in a multichannel LED display. This paper proposes a quasi-hysteretic finite-state-machine-based digitally controlled single-inductor dual-output buck switching LED driver operating in discontinuous conduction mode (DCM) and extends it to drive multiple outputs. Based on the time-multiplexing control scheme in DCM, a theoretical upper limit of the total number of outputs in a SIMO buck switching LED driver for various backlight LED current values can be derived analytically. The advantages of the proposed SIMO LED driver include reducing the controller design complexity by eliminating loop compensation, driving more LED strings without limited by the maximum LED current rating, performing digital dimming with no additional switches required, and optimization of local bus voltage to compensate for variability of LED forward voltage V_F in each individual LED string with smaller power loss. Loosely binned LEDs with larger V_F variation can, therefore, be used for reduced LED costs.**

***Index Terms*—Boundary conduction mode (BCM), discontinuous conduction mode (DCM), finite-state machine (FSM), single-inductor dual-output (SIDO), single-inductor multiple-output (SIMO).**

I. Introduction

An LED driver is essentially a current source (or sink) which maintains a constant current required for achieving the desired color and luminous flux from an array of LEDs. A number of highly efficient switching LED drivers have been reported in the literature and their primary objective is to achieve high power conversion efficiency [1]–[11]. Besides efficiency, another important consideration is the scalability of the existing single-inductor dual-output (SIDO) switching converter to drive multiple independent LED strings in a single-inductor multiple-output (SIMO) topology for reduced cost and smaller form factor [12]. However, in practice, only a finite number of outputs can be served by each LED driver.

The prior arts of SIMO switching converter use either one of two ways to distribute energy from a single power supply to multiple outputs with a single inductor, namely multiple energizing phases [13]–[20] and single energizing phase per switching cycle [21]. The former with time-multiplexing control leads to much better suppression of cross regulation because the outputs are decoupled in time. In this paper, a quasi-hysteretic finite-state machine (FSM)-based digital control scheme is employed in a SIDO buck LED driver consisting of two independent parallel strings operating in discontinuous conduction mode (DCM). The extension of this SIDO architecture to SIMO is formally investigated. The proposed SIMO-based switching buck LED driver enables separate control of the three primary colors (red, green, and blue), thereby offering more flexibility for color mixing. The rest of this paper is organized as follows. Section II introduces the proposed quasi-hysteretic FSM-based digital controller for a SIDO switching buck LED driver operating in DCM. Section III provides a theoretical analysis on the scalability of the proposed digital control scheme from SIDO to SIMO and suggests a general formula for determining the theoretical upper bound in the total number of outputs in SIMO. Section IV shows Cadence Spectre simulation results that are used to verify the theoretical model. Section V contains the experimental results for the proposed digitally controlled SIDO buck LED driver. Section VI concludes our research effort.

II. Quasi-Hysteretic FSM-Based Digital Control for SIDO LED Driver

A SIDO switching converter with time-multiplexing control scheme operating in DCM was first reported in [13]–[16]. With such kind of time-multiplexing control scheme, a SIDO converter can easily be extended to drive multiple outputs and it exhibits negligible cross regulation in DCM. A SIMO parallel-string LED driver operating in DCM has recently been reported [12]. It uses an analog-based controller with dominant pole compensation for stability, and time-multiplexing control in DCM is employed to suppress cross regulation among the LED strings. Unlike conventional pulse width modulation (PWM)-based analog controllers, the proposed digital controller utilizing quasi-hysteretic control does not require any compensation circuits because of its inherent stability [22]–[24], hence simplifying the control loop design and reducing the component count and cost. Quasi-hysteretic control offers a good

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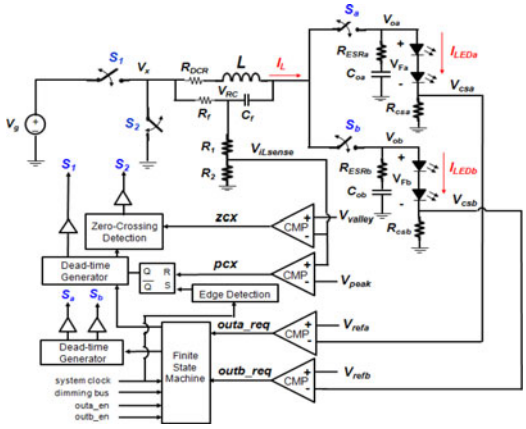


Fig. 1. System architecture of the quasi-hysteretic FSM-based digitally controlled SIDO buck LED driver.

compromise between traditional fixed-frequency PWM control and pure hysteretic control with variable switching frequency. In the proposed design, an external clock is used to synchronize the buck LED driver which switches at a fixed frequency. Fast comparators are used to control the on-time of the high-side and low-side power switches by monitoring the inductor current. This is particularly suitable for lighting applications where variable switching frequencies are not desirable. The reconfigurability and scalability of a digital controller makes it especially attractive for SIMO.

A major drawback of the previously proposed SIMO LED driver operating in DCM [12] is that since the LED current is discontinuous, the LED endures a higher maximum peak current for the same average current required. In other words, the LED could potentially be operating close to its absolute maximum current rating, thereby increasing the current stress and possibly shortening the operating lifetime of the LED. In their approach, the LED current scales with the number of LED strings in SIMO. Hence, the maximum current rating of the LED unnecessarily restricts the maximum achievable number of LED strings which can be implemented in SIMO. In the proposed design, the LED current is always continuous and the LED can be regulated very close to the target average current value which is much lower than its maximum current rating. During the time interval when the output switch is OFF, the output capacitor, acting as a constant current source, continues to discharge its current to the corresponding LED string. When the output switch is ON, the power stage is reconnected to the LED string and the inductor current is transferred to the output capacitor and the LED string simultaneously. The current-sense feedback control ensures that the LED current is maintained at the desired dc level. Hence, a time-continuous current is supplied to the LED string. Consequently, the LED current does *not* scale with the number of LED strings in the proposed SIMO architecture, making it possible to drive more LED strings without inducing too much stress on the LEDs. Fig. 1 shows the system architecture of the proposed quasi-hysteretic FSM-based digitally controlled SIDO buck switching LED driver which takes into account the parasitic effects including the dc resistance (DCR) of the inductor L and equivalent series resistance (ESR) of the output capacitors (C_{oa}, C_{ob}). The two independently driven LED strings share the same inductor L and the two main power switches (S_1, S_2) of the buck converter. The output switches (S_a, S_b) enable the charge stored in the inductor to be distributed between the two outputs in a time-multiplexed fashion. Dead-time generators are used to eliminate shoot-through current by ensuring that S_1 and S_2 are not turned ON simultaneously. Dead-times are also introduced between S_a and S_b to prevent inadvertent cross conduction between the two LED strings.

Since an LED is essentially a current driven device, an LED driver typically regulates the LED current rather than its forward voltage. A straightforward way is to insert a small high-precision current sensing resistor $(R_{\rm csa}, R_{\rm csb})$ in series with the corresponding LED string to sense the LED current by converting it to the current-sense voltage $(V_{\rm csa}, V_{\rm csb})$. The current-sense voltage is then compared with the reference voltage $(V_{\rm refa}, V_{\rm refb})$ to generate the corresponding logic signals (*outa_req*, *outb_req*) which determine the opening or closing of the two output switches in a SIDO buck converter. Since the LED's *I–V* curve is usually provided by the LED manufacturer, the target dc current value for a particular LED string can be set by choosing an appropriate reference voltage. On the other hand, a two-limit hysteretic control determines the on-time of the high-side and low-side power switches (S_1, S_2) of the buck converter. The upper and lower limits of the inductor current, namely the peak current limit and the valley current limit, define the average value of the inductor current which is the *total* LED current for a SIDO buck LED driver. In DCM, the valley current limit is set to zero to prevent the inductor current from going negative which degrades the power conversion efficiency [12], [16], [25]. As illustrated in Fig. 1, R_fC$_f$ is connected in parallel to the inductor so that the slopes of V_{RC} are proportional to the inductor current ramp-up and ramp-down slopes [26]. A small resistor ladder is connected between V_{RC} and ground in order to generate a lower voltage signal $V_{iLsense}$ which falls within the input voltage range of the comparator (CMP). $V_{0iLsense}$ is fed forward to the corresponding comparators to determine the peak-crossing and zero-crossing of the inductor current. Fig. 2 is a simplified flowchart showing the system-level operation of the proposed SIDO buck driver. Suppose identical current flows through each of the two LED strings, also referred to as the *balanced load* condition, the inductor current I_L is assigned to each string in alternate switching cycles. The working principle of the proposed SIDO buck LED driver is represented by the timing diagram shown in Fig. 3. During $D_{1a}T_s$ or $D_{1b}T_s$, I_L ramps up with a slope of $m_1 = (V_g - V_o)/L$ and the inductor is charged with a voltage of $V_L = V_g - V_o$, where V_g and V_o represent the input voltage and the output voltage, respectively. During $D_{2a}T_s$ or $D_{2b}T_s$, I_L ramps down with a slope of $m_2 = -V_o/L$ and the inductor discharges its current to the corresponding output capacitor and the LED string until I_L returns to zero. During $D_{3a}T_s$ or $D_{3b}T_s$, I_L stays at zero with both S_1 and S_2 OFF. In the proposed SIDO LED driver, the system clock defines the switching frequency. The rising edge of the system clock triggers the ON duty cycle ($D_{1a}T_s$, D_1bT_s) by charging up the inductor during which S_1 is ON and S_2 is OFF. The

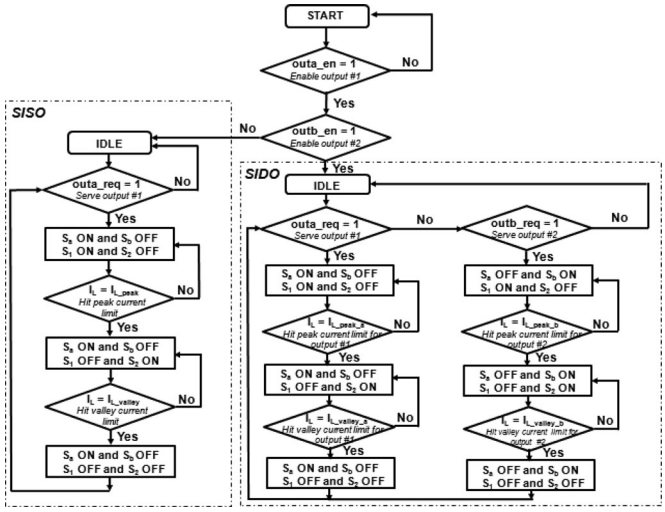


Fig. 2. Simplified flowchart representing the system-level operation of the proposed SIDO buck LED driver.

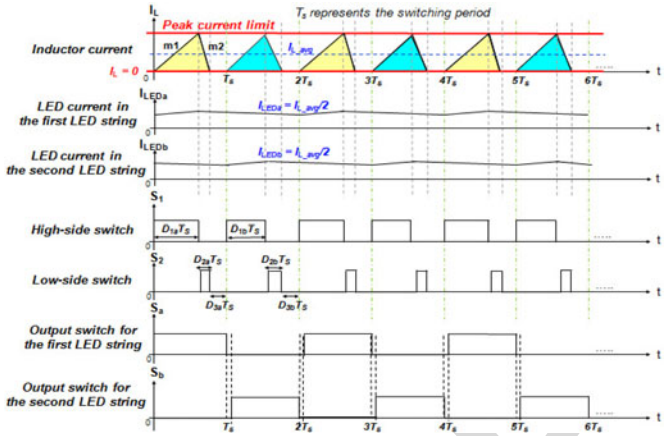
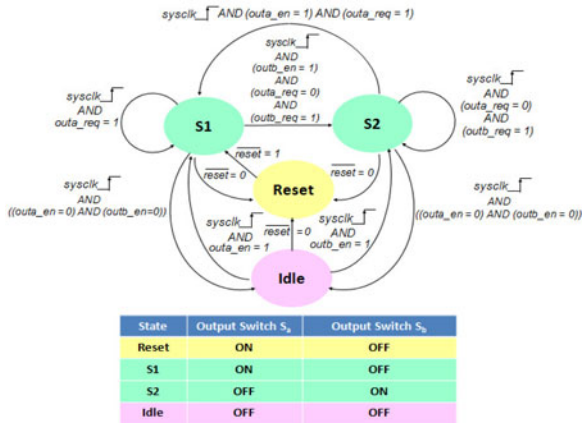


Fig. 3. Timing diagram of the proposed SIDO buck LED driver with balanced load operating in DCM.



State	Output Switch S_a	Output Switch S_b
Reset	ON	OFF
S1	ON	OFF
S2	OFF	ON
Idle	OFF	OFF

Fig. 4. State diagram of the proposed FSM for controlling the two output switches in SIDO buck LED driver.

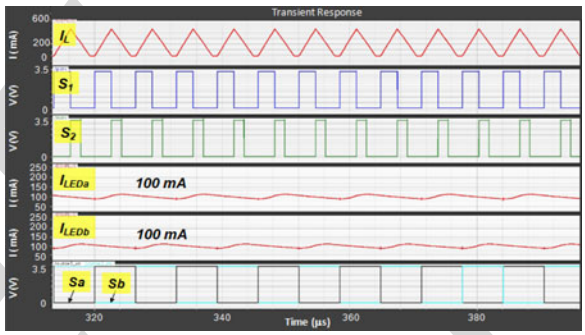


Fig. 5. Simulated steady-state waveforms for the proposed SIDO buck LED driver operating in DCM.

inductor current continues to increase until it hits the peak current limit at which point the buck converter enters $(D_{2a}T_s, D_{2b}T_s)$ where S_1 is OFF and S_2 is ON. The inductor discharges its current to the corresponding output until the zero-crossing of the inductor current is detected. The converter then enters the idle phase $(D_{3a}T_s,\ D_{3b}T_s)$ during which both S_1*and* S_2 are OFF. The inductor current remains at zero until the next rising edge of the system clock arrives and the switching sequence repeats itself. The two output switches $(S_a,\ S_b)$ are controlled by the FSM as shown in Fig. 4.

The state machine is triggered by the rising edge of the system clock (*sysclk*) so that the transitions of the output switches (S_a, S_b) are in sync with the system clock. The input signals of the state machine are the output enable signals (*outa_en*, *outb_en*) and the output request signals (*outa_req*, *outb_req*) which determine the switching sequence of the two outputs. The first LED string is always given a higher priority over the second one. For instance, if both strings request service simultaneously, i.e., *outa_req* $= 1$ and *outb_req* $= 1$, S_a is turned ON first and S_b remains OFF. S_b is turned ON only when *outa_req* $= 0$ and *outb_req* $= 1$. S_a and S_b must be nonoverlapping to avoid undesirable cross conduction between the two LED strings. In addition, an enable signal (*out1en*, *out2en*) is associated with either of the two LED strings. It provides the option of shutting down any or all of the LED strings, for example, in response to an overcurrent fault condition. An overriding signal can also be sent from the FSM to the hysteretic controller to disable the high-side and low-side power switches accordingly. The FSM-based controller can be modified quickly and conveniently to drive multiple LED strings in a SIMO configuration by simply adding more states in the VHDL or Verilog code. A mixed-signal macromodel of the proposed FSM-based digitally controlled SIDO buck switching LED operating in DCM is simulated in the time domain using Cadence Spectre [27]. The FSM is modeled in Verilog RTL and the rest are modeled as ideal circuit elements. The simulation model also incorporates parasitics such as DCR of the inductor L and ESR of the output capacitors (C_{oa}, C_{ob}). For *balanced load* condition, the current between the two LED strings is identical and each string consists of *two* LEDs connected in series. First, the steady-state performance is investigated. Fig. 5 contains the simulated steady-state waveforms for the inductor current (I_L), the LED current $(I_{\mathrm{LED}a}, I_{\mathrm{LED}b})$, and the four switches (S_1, S_2, S_a, S_b) of the proposed SIDO buck LED driver operating in DCM. The switching frequency is 156.25 kHz and the input voltage V_g is 15 V. The simulation results show that the LED current in either

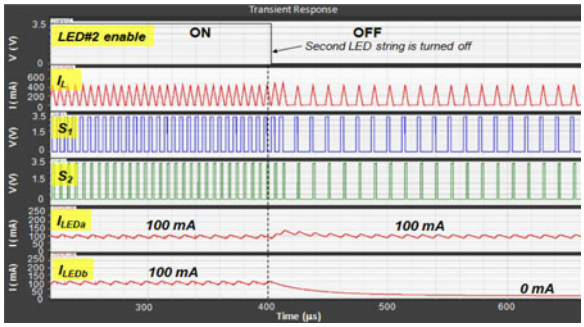


Fig. 6. First LED string remains under regulation without cross regulation when the second LED string is shut down completely.

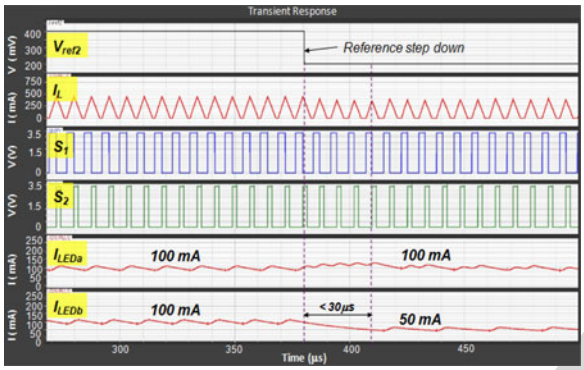


Fig. 7. First LED string remains under regulation without cross regulation despite a reference step in the second LED string from 100 to 50 mA in 20 ns.

of the two strings is regulated successfully to the target steady-state dc value of 100 mA with a current ripple of $23\%_{\text{P-P}}$. The steady-state output voltage for the first and second LED string is approximately 6.48 V with a voltage ripple of $2.6\%_{\text{P-P}}$. Second, the stability of the closed-loop system is verified by examining its dynamic performance. In the first scenario, the second LED string needs to be shut down instantly in response to an over-current condition. Fig. 6 shows that despite the immediate shutdown of the second LED string, the LED current $I_{\text{LED}a}$ in the first LED string continues to be regulated successfully at its target nominal value of 100 mA with minimal cross regulation. In the second scenario, the second LED string experiences a reference step of 50 mA, i.e., $I_{\text{LED}b}$ transitions from 100 to 50 mA in 20 ns. Fig. 7 shows that the current in the first LED string continues to be regulated at around 100 mA, virtually unaffected by the sudden reference step in the other string. The second LED string settles to the new nominal current value of 50 mA. It demonstrates that the closed-loop system remains stable in response to the reference transient in the second string.

Unlike conventional backlight LED drivers that use PWM dimming transistor connected in series with the LED string [3], [8], [28]–[31], the proposed SIDO LED driver takes advantage of the existing four switches to perform dimming without requiring additional switches. When the dimming control signal for a particular LED string goes high, certain phases of the inductor current are skipped so that the average inductor current (also the average load current) going into that string is reduced accordingly. The digital dimming control signals (*dim_ctrl1*, *dim_ctrl2*) essentially modulate the dc current level flowing through the corresponding LED string. No additional dimming transistors in series with the LED string are required, thereby leading to a smaller voltage headroom and reduced power loss. The only voltage headroom is the voltage across the current-sense resistor $(V_{\text{csa}}, V_{\text{csb}})$ which is typically between 0.2 and 0.4 V. Fig. 8 depicts the timing diagram of the proposed digital dimming control scheme. In this particular case, the second LED string is dimmed by reducing its current from 100 to 50 mA, while the current in the first LED string stays constant at 100 mA.

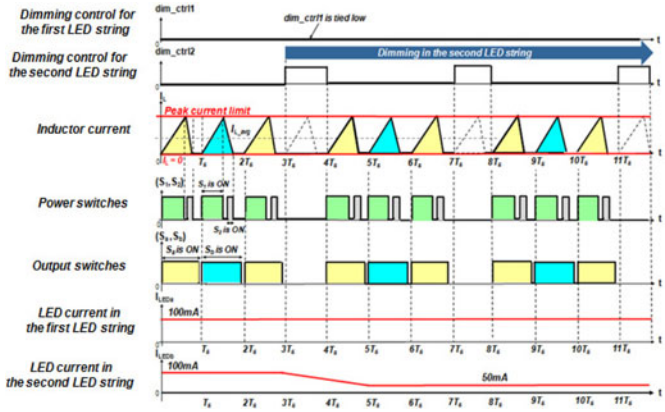


Fig. 8. Proposed digital dimming control in SIDO buck LED driver.

Any combination of LED strings in a SIMO LED driver can be dimmed or even shut down momentarily to achieve flexible dimming and optimum luminance levels. In addition, it is reported in the literature [32]–[34] that a bilevel or N-level current driving technique for LED dimming improves the luminous efficacy of LEDs by introducing a dc offset to the PWM current. The proposed SIDO converter can potentially be used as a bilevel LED driver by generating two programmable dc current values for each individual LED string in a time-multiplexed fashion. Another major difference between the proposed LED driver and the existing ones [3], [8], [28]–[31] is that the former provides N optimized output bus voltage for each individual LED string, whereas the latter only uses a common output bus shared by all the LED strings. Due to manufacture, process, and temperature variations, V_F in each LED does not match perfectly, which means that the voltage drop across each LED string differs. Using the proposed SIDO buck LED driver in Fig. 1 as an example and assuming the LED current is 100 mA in each string, the voltage headroom $(V_{\text{csa}}, V_{\text{csb}})$ is 0.4 V, and the voltage drop across each of the two LED strings are $V_{Fa} =$ 6.0 V and $V_{Fb} = 7.0$ V, respectively. The output voltages are $V_{oa} = 6.4$ V and $V_{ob} = 7.4$ V. The total power consumption of the load P_{LOAD}, including the LED string and current-sense resistor, is $P_{\text{LOAD}} = V_{oa} \times I_{\text{LED}} + V_{ob} \times I_{\text{LED}} = 1.38$ W. The output voltage for each LED string is independently optimized based on its corresponding V_F, resulting in the same voltage headroom of 0.4 V for each string. This is different from a conventional LED driver in which the common output bus voltage is usually regulated using the LED string with the maximum voltage drop. For the same LED current, the total power consumption using a conventional LED driver is given by: $P_{\text{LOAD}} =$

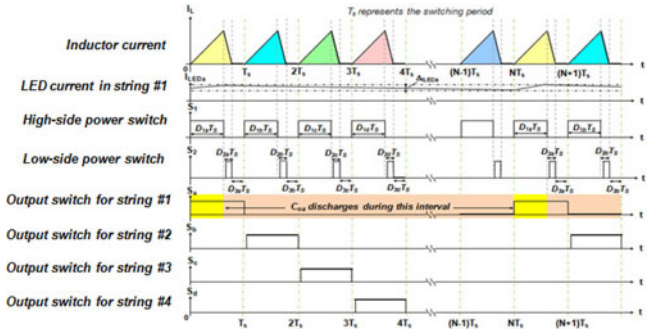


Fig. 9. Timing diagram of the proposed SIMO buck LED driver.

$2 \times \max(V_{oa}, V_{ob}) \times I_{\rm LED} = 1.48$ W, which is more than 7% higher than that of the proposed driver. The voltage headroom for the first LED string increases from 0.4 to 1.4 V, resulting in 450 mW more power loss or additional 30% efficiency degradation. Since the output voltage is self-optimized to match the total V_F in each individual LED string in the proposed driver, same-colored LEDs from neighboring bins (not only from a single bin) with larger V_F variance can be used which helps reduce the LED costs. In the event that a particular application demands a total LED current greater than the average inductor current, the same time-multiplexing control scheme operating in DCM can still be employed either by lowering the switching frequency with a higher inductor peak current limit or by operating the buck LED driver in pseudocontinuous conduction mode (PCCM) [17], [35], [36]. In PCCM, the average inductor current is increased by simply adding a nonzero dc offset of $I_{\rm DC}$ to that of DCM.

III. Extension From SIDO to SIMO Buck LED Driver

Having demonstrated the feasibility of the proposed SIDO buck LED driver, it is natural for us to extend it to SIMO with N independently driven LED strings. In particular, the theoretical maximum number of LED strings $N_{\max}$ is determined for this SIMO architecture. Fig. 9 shows a timing diagram of the inductor current, the two power switches (S_1, S_2), and the first four output switches (S_a, S_b, S_c, S_d) in a SIMO buck LED driver. To simplify the analysis, the *balanced load* condition is assumed. Based on the time-multiplexing control scheme, energy is being transferred from the dc supply to each individual output *exactly once* within a total of N switching phases. For a particular output, the corresponding output switch is OFF during D_3, while the output capacitor discharges to the LED string. During the subsequent $(N-1) \times T_s$ phases, the output switch remains OFF and the output capacitor continues to discharge to the corresponding LED string. Hence, the *total* discharging time for the output capacitor $t_{\rm dch}$ can be expressed as

$$t_{\rm dch} = D_3 T_s + (N-1)T_s = (D_3 + N - 1)T_s. \quad (1)$$

$$\text{For } D_3 = 0, t_{\rm dch} = (N-1)T_s. \quad (2)$$

The proposed SIMO buck LED driver is essentially a constant-current regulator which maintains a constant dc current $I_{\rm LED}$ flowing through the LED string via a closed-loop current-sense feedback control. For very small variation of forward voltage around the quiescent point (also known as bias point) on the LED's exponential *I–V* curve, the dc forward current is assumed to be constant. During $t_{\rm dch}$ when the output switch is OFF, the output capacitor is connected to the LED string which acts as a constant-current sink (CCS). Assuming ideal capacitor with no ESR (the effect of the ESR will be explained later), the voltage across the output capacitor v_c(t) is the same as the output voltage which is expressed as the charge *q(t)* divided by the capacitance value C_o, i.e.,

$$v_c(t) = \frac{q(t)}{C_o} = \frac{1}{C_o}\int_0^{t_{\rm dch}} i_c(\tau)d\tau + v_c(0). \quad (3)$$

$$\text{For CCS, } i_c(\tau) = I_{\rm LED}. \quad (4)$$

Combining (3) and (4) and rearranging, we have

$$\Delta v_o = \Delta v_c = v_c(t) - v_c(0) = \frac{1}{C_o}(I_{\rm LED} t_{\rm dch}). \quad (5)$$

Hence, the *total* discharging time $t_{\rm dch}$ can be expressed as

$$t_{\rm dch} = \frac{C_o \Delta v_o}{I_{\rm LED}} \quad (6)$$

where Δv_o is the output voltage drop due to the discharging of the output capacitor. In general, Δv_o is assumed to be reasonably small relative to the output voltage. The LED ripple current $\Delta i_{\rm LED}$ usually ranges from $10\%_{\text{P-P}}$ to $40\%_{\text{P-P}}$ of the dc forward current as recommended by the LED manufacturers [37], [38]. For a particular $\Delta i_{\rm LED}$, the corresponding voltage ripple $\Delta v_{\rm LED}$ at the chosen bias point can be readily obtained from the exponential *I–V* curve. Suppose each LED string contains a total of n LEDs connected in series. The output voltage ripple Δv_o is, therefore, the sum of the voltage ripple across the LED string and the voltage ripple across the current-sense resistor, i.e., $\Delta v_o = n \times \Delta v_{\rm LED} + \Delta v_{cs}$. Suppose $\Delta v_{o\max}$ represents the *maximum* output voltage ripple allowed. Equation (6) can, therefore, be rewritten as

$$t_{\rm dch} \le \frac{C_o \Delta v_{o\max}}{I_{\rm LED}}. \quad (7)$$

Substituting (1) into (7), we have

$$(D_3 + N - 1)T_s \le \frac{C_o \Delta v_{o\max}}{I_{\rm LED}} \Rightarrow N \le \frac{C_o \Delta v_{o\max}}{I_{\rm LED} T_s} + 1 - D_3. \quad (8)$$

Hence, the theoretical maximum possible number of LED strings in SIMO, $N_{\max}$, is given by

$$N_{\max} = \frac{C_o \Delta v_{o\max}}{I_{\rm LED} T_s} + 1 - D_3 = \frac{C_o \Delta v_{o\max}}{I_{\rm LED} T_s} + D_1 + D_2. \quad (9a)$$

Since $N_{\max}$ is an integer value, the *floor*$(\cdot)$ function is used to round the result down to the closest integer. Hence, (9a) becomes

$$N_{\max} = \text{floor}\left(\frac{C_o \Delta v_{o\max} + I_{\rm LED} T_s (1 - D_3)}{I_{\rm LED} T_s}\right). \quad (9b)$$

Equation (9b) represents a general formula for determining the scalability limit of a SIMO buck LED driver operating in DCM

and is referred to as a *scalable DCM-based SIMO scheme* for the sake of our ensuing discussion. In particular, when $D_3 = 0$, the SIMO buck LED driver operates in boundary conduction mode (BCM). Hence, (9a) and (9b) become (10a) and (10b), respectively. Also, $N_{\max}$ in BCM is greater than or equal to that in DCM for the same set of design parameter values

$$N_{\max} = \frac{C_o \Delta v_{o\max}}{I_{\rm LED} T_s} + 1 \tag{10a}$$

$$N_{\max} = \text{floor}\left(\frac{C_o \Delta v_{o\max}}{I_{\rm LED} T_s} + 1\right). \tag{10b}$$

For a single-output buck converter, the average inductor current is identical to the load current. Due to the nature of the time-multiplexing control scheme in the proposed SIMO converter, the average inductor current $I_{L\_\rm avg}$ is the *sum* of the individual load current $I_{\rm LED}$ in each LED string. Assuming balanced load condition, $I_{L\_\rm avg} = N \times I_{\rm LED}$, where N is the total number of LED strings. The average inductor current reaches its maximum value in BCM, resulting in a maximum transfer of power [16]. Since the current in each LED string remains the same, a theoretical upper bound of the total achievable number of LED strings in SIMO can be expressed as

$$N_{\max} = \frac{I_{L\_\rm avg\_max}}{I_{\rm LED}}. \tag{11}$$

By simple geometry, $I_{L\_\rm avg\_max}$ is given by the following equation [39]:

$$I_{L\_\rm avg\_max} = \frac{m_1 D_1 T_s}{2} = \frac{(V_g - V_o) D_1 T_s}{2L}. \tag{12}$$

By substituting (12) into (11) and rearranging, T_s can be expressed as

$$T_s = \frac{2LN_{\max} I_{\rm LED}}{D_1 (V_g - V_o)}. \tag{13}$$

Now, by substituting (13) into (10a) and rearranging, we have

$$2LI_{\rm LED}^2 N_{\max}^2 - 2LI_{\rm LED}^2 N_{\max} - C_o \Delta v_{o\max} (V_g - V_o) D_1 = 0. \tag{14}$$

Equation (14) is a quadratic equation in $N_{\max}$. The discriminant Δ of (14) can be expressed as

$$\Delta = 4L^2 I_{\rm LED}^4 + 8LI_{\rm LED}^2 C_o \Delta v_{o\max} (V_g - V_o) D_1 > 0. \tag{15}$$

Since $(V_g - V_o) > 0$ for a buck switcher, the discriminant in (15) is always a positive number which implies that (14) has two real roots as given by

$$r_1, r_2 = \frac{2LI_{\rm LED}^2 \pm \sqrt{\Delta}}{4LI_{\rm LED}^2}. \tag{16}$$

Since $N_{\max}$ must be a *positive integer*, the negative root is eliminated, leaving only the positive root, i.e.,

$$N_{\max\_\rm BCM} = \text{floor}\left(\frac{1}{2} \times \left[1 + \sqrt{1 + \frac{2C_o \Delta v_{o\max} V_o (V_g - V_o)}{LI_{\rm LED}^2 V_g}}\right]\right) \tag{17}$$

Equation (17) defines the theoretical maximum total number of outputs in SIMO operating in BCM. It is referred to as a *scalable BCM-based SIMO scheme* which is a special case of *scalable DCM-based SIMO scheme*. In fact, it is observed that (11) is also valid for the case of DCM. By simple geometry, the switching period T_s in DCM can be expressed as

$$T_s = \frac{2LN_{\max} I_{\rm LED}}{D_1 (D_1 + D_2)(V_g - V_o)}. \tag{18}$$

Realizing that the same calculations that lead to (17) for the case of BCM can also be performed in DCM, the theoretical maximum total number of LED strings in a SIMO converter operating in DCM can, therefore, be written as[1]

$$N_{\max\_\rm DCM} = \text{floor}\left(\frac{1}{2} \times (1 - D_3) \times \left[1 + \sqrt{1 + \frac{2C_o \Delta v_{o\max} (V_g - V_o) D_1}{LI_{\rm LED}^2 (1 - D_3)}}\right]\right). \tag{19}$$

Notice that for the case of BCM, $D_3 = 0$ and $D_1 = V_o / V_g$, (19) reduces to (17). Hence, (19) represents the generalized formula for the theoretical maximum total number of outputs in SIMO which is applicable to either BCM or DCM. It is also interesting to note that the average inductor current in DCM is smaller than (or equal to) that in BCM. As a result, for the same LED current, the theoretical maximum achievable number of outputs in SIMO operating in DCM is no greater than that in BCM, i.e., $N_{\max\_\rm DCM} \le N_{\max\_\rm BCM}$. In reality, the ESR of the output capacitor needs to be taken into consideration. Any current flowing through the output capacitor C_o must also flow through the $R_{\rm ESR}$, resulting in an additional voltage drop of $\Delta V_{\rm ESR} = I_{\rm LED} \times R_{\rm ESR}$. Hence, Δv_o can be expressed as

$$\Delta v_o = \Delta v_c + \Delta v_{\rm ESR} = \Delta v_c + I_{\rm LED} \times R_{\rm ESR}. \tag{20}$$

Rearranging the terms in (20), we have

$$\Delta v_c = \Delta v_o - I_{\rm LED} \times R_{\rm ESR}. \tag{21}$$

Hence, (17) and (19) are modified slightly to become (22) and (23), respectively: BCM:

$$N_{\max\_\rm BCM} = \text{floor}\left(\frac{1}{2} \times \left[1 + \sqrt{1 + \frac{2C_o V_o (\Delta v_{o\max} - I_{\rm LED} R_{\rm ESR})(V_g - V_o)}{LI_{\rm LED}^2 V_g}}\right]\right) \tag{22}$$

DCM:

$$N_{\max\_\rm DCM} = \text{floor}\left(\frac{1}{2} \times (1 - D_3) \times \left[1 + \sqrt{1 + \frac{2C_o (\Delta v_{o\max} - I_{\rm LED} R_{\rm ESR})(V_g - V_o) D_1}{LI_{\rm LED}^2 (1 - D_3)}}\right]\right). \tag{23}$$

The presence of $R_{\rm ESR}$ in (22) and (23) reduces the theoretical maximum achievable number of outputs in SIMO. Therefore,

[1] In DCM, D_1 can be expressed as: $D_1 = M\sqrt{\frac{K}{1-M}}$, where $M = \frac{V_o}{V_g}$ and $K = \frac{2L}{R_L T_s} = \frac{2LI_{\rm LED}}{V_o T_s}$ [39].

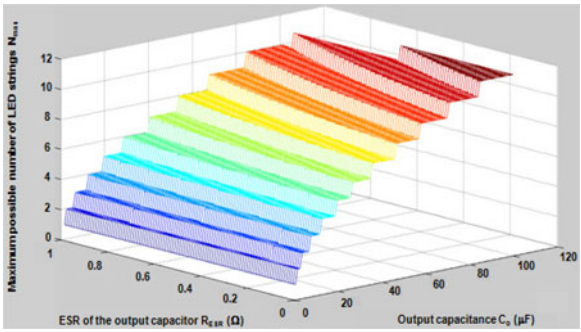


Fig. 10. Theoretical maximum achievable number of LED strings $(N_{\max})$ versus the output capacitance (C_o) and the capacitor ESR $(R_{\rm ESR})$ for the *scalable BCM-based SIMO scheme*.

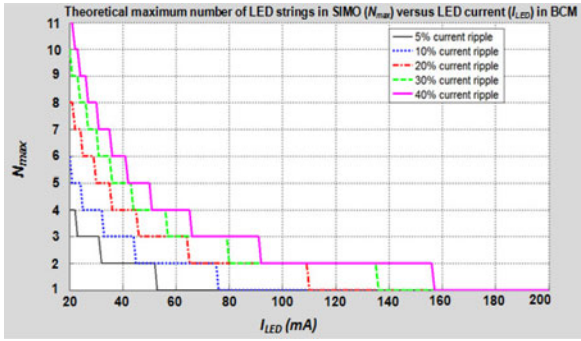


Fig. 11. Plot of theoretical maximum number of LED strings in SIMO $(N_{\max})$ versus the LED current $(I_{\rm LED})$ in the *scalable BCM-based SIMO scheme*.

it is always recommended to choose an output capacitor with a smaller ESR, whenever possible. Fig. 10 shows the theoretical maximum total number of LED strings versus the output capacitance and capacitor ESR for the scalable *BCM-based SIMO scheme*, given an LED current of 80 mA and a maximum ripple current requirement of $40\%_{\rm P\text{-}P}$.

Intuitively, for a particular LED current, an increasing number of outputs can be achieved by using a larger output capacitor with the same ESR value. For instance, if the output capacitance is increased from 4.7 to 22 μF (the ESR remains at 100 mΩ), the theoretical model based on (22) suggests that the maximum total number of LED strings can be increased from three to six. It is also interesting to note that the maximum number of outputs in SIMO has a stronger dependence on the output capacitance than the capacitor ESR, as shown in Fig. 10.

On the other hand, it is useful to study how the LED current affects the maximum achievable number of outputs in SIMO. As an example, assuming balanced load and two LEDs connected in series per string, a *scalable BCM-based SIMO scheme* is investigated with these parameter values: $L = 47$ μH, $C_o = 4.7$ μF, $R_{\rm ESR} = 100$ mΩ, $V_g = 15$ V, and $V_o = 6.4$ V. The relationship between $N_{\max}$ and $I_{\rm LED}$ can be obtained by using (22) for different values of output voltage ripple $\Delta v_{o\_\max}$. Based upon the *I–V* curve and/or SPICE model of the particular LED used, the corresponding output voltage ripple $\Delta v_{o\_\max}$ can be determined from the LED current ripple requirement $\Delta i_{\rm LED}$. The proposed design uses white LED [40] which is the target for LCD backlighting applications. For instance, a $20\%_{\rm P\text{-}P}$ current ripple corresponds to around $2\%_{\rm P\text{-}P}$ voltage ripple and a $40\%_{\rm P\text{-}P}$ current ripple corresponds to around $4\%_{\rm P\text{-}P}$ voltage ripple. Fig. 11 shows a plot of $N_{\max}$ versus $I_{\rm LED}$ for $\Delta i_{\rm LED}$ ranging from $5\%_{\rm P\text{-}P}$ to $40\%_{\rm P\text{-}P}$. This plot is beneficial to a practical SIMO design in two ways. First, for a given LED current and current ripple requirement, the theoretical maximum number of LED strings viable under the *scalable BCM-based SIMO scheme* can be extracted directly from the plot. Second, the maximum LED current allowed in order for a SIMO to remain at the same scaling level can also be obtained from the plot. For instance, given a 20% current ripple requirement (i.e., $\Delta i_{\rm LED} = 20\%_{\rm P\text{-}P}$), a SIDO (dual-string) configuration is possible as long as the LED current in each string is no more than 110 mA. In the event that an application demands an LED current greater than 110 mA, two options can be considered: 1) Relax the current ripple requirement whenever possible. A wider tolerance in $\Delta i_{\rm LED}$ is generally acceptable since the ripple frequency is too high for the human eye to detect. 2) Operate the SIMO buck LED driver in PCCM [17], [35], [36]. In PCCM, the floor of the inductor current is raised by a nonzero dc offset $I_{\rm DC}$ which distinguishes it from DCM. The proposed theoretical model can be extended to PCCM by adding a dc component to the average inductor current. By going through similar calculations as in DCM, the theoretical maximum number of outputs in SIMO operating in PCCM is given by (24), as shown at the bottom of the page. It is interesting to note that (24) continues to apply to the cases of DCM and BCM. For instance, in DCM, $I_{\rm DC} = 0$ and (24), therefore, reduces to (23).

In the event of unbalanced load with unequal current among the LED strings, the *scalable DCM- or BCM-based SIMO scheme* continues to hold. The only change is to replace $I_{\rm LED}$ in (22) and (23) by max$(I_{\rm LED})$, where max$(I_{\rm LED})$ denotes the *largest* LED current among all the LED strings. In other words, the maximum number of LED strings that can be realized in a SIMO buck LED driver is constrained by the *largest* LED current. Generally speaking, the input voltage V_g, output voltage V_o, and the current ripple requirement are typically fixed parameters defined in the design specification. Without making any hardware changes (i.e., *L and* C_o values are fixed), the primary design variable in (22) and (23) is the LED current $I_{\rm LED}$. In fact, the LED current is the dominant factor for determining the maximum possible number of outputs under the *scalable DCM-/BCM-based SIMO scheme*. By knowing the maximum LED current required for a particular application, the theoretical

$$N_{\max\_\rm PCCM} = \text{floor}\left(\frac{1}{2I_{\rm LED}}\times\left[\left(I_{\rm DC}+(1-D_3)\,I_{\rm LED}\right]\times\left[1+\sqrt{1+\frac{2C_o\left(\Delta v_{o\max}-I_{\rm LED}R_{\rm ESR}\right)\left(V_g-V_o\right)D_1(1-D_3)}{L\left[I_{\rm DC}-(1-D_3)I_{\rm LED}\right]^2}}\right]\right). \tag{24}$$

TABLE I
DESIGN SPECIFICATION OF A SISO BUCK LED DRIVER IN DCM

Design Parameter	Value	Unit
Input Voltage (V_g)	15	V
Output Voltage (V_o)	6.32	V
LED Forward Current (I_{LED})	80	mA
Switching Frequency (f_s)	100	kHz
Inductor (L)	47	μH
Output Capacitor (C_o)	*4.7*	*μF*
ESR of Output Capacitor (R_{ESR})	100	mΩ
Maximum LED Current Ripple (Δi_{LED})	40	$\%_{\text{P-P}}$
Maximum Output Voltage Ripple (Δv_o)	4	$\%_{\text{P-P}}$
Duty Ratio of Idle Phase (D_3)	≥10	%

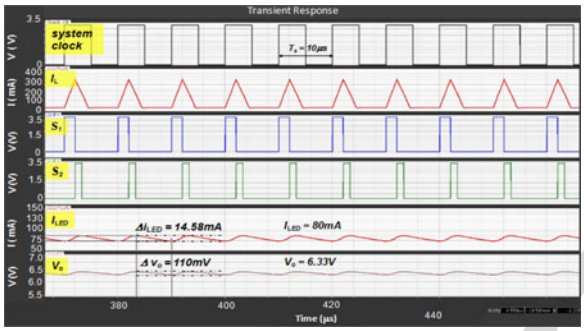


Fig. 12. Simulated steady-state waveforms for the SISO buck LED driver based on the design specification in Table I.

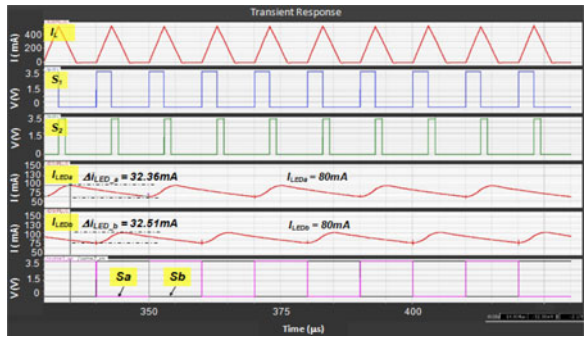


Fig. 13. Simulated steady-state waveforms showing SIDO is not viable since the $30\%_{\text{p-p}}$ maximum current ripple requirement is violated.

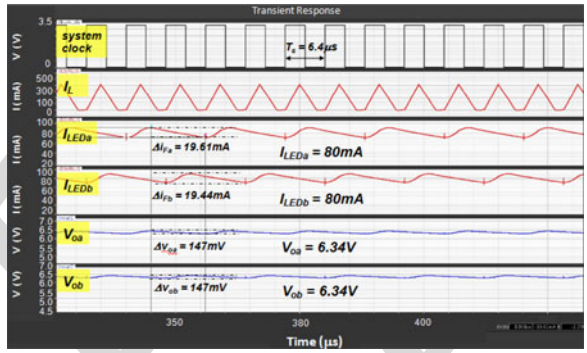


Fig. 14. Simulated steady-state waveforms showing SIDO is possible by increasing the switching frequency from 100 to 156.25 kHz.

maximum achievable number of independently driven LED strings can be estimated in advance.

IV. SIMULATION RESULTS

Ideal macromodels based on the *scalable DCM-based SIMO scheme* were constructed and simulated in Cadence Spectre [27] in order to compare with the theoretical results in Section III. The design specification of a single-inductor single-output (SISO) buck converter is shown in Table I. The theoretical model based on (23) suggests that $N_{\max\_\text{DCM}} = 1$, meaning only one LED string is viable. Fig. 12 shows the simulated steady-state waveforms of the inductor current I_L, the LED currents I_{LED}, and the output voltages V_o of a SISO buck LED driver. The simulated steady-state LED current I_{LED} is approximately 80 mA which meets the design target. The simulated LED current ripple Δi_{LED} is $18\%_{\text{P-P}}$ (also, the output voltage ripple Δv_o is $1.7\%_{\text{P-P}}$), which satisfies the maximum ripple requirement. Now, the SISO buck LED driver is transformed into SIDO by adding a second LED string. Fig. 13 shows the simulated steady-state waveforms from the resulting SIDO LED driver.

Despite the fact that the steady-state LED current in either string remains at 80 mA, the LED current ripple is more than $40\%_{\text{P-P}}$ which violates the maximum ripple current requirement. Hence, the simulation results show that SIDO is not viable based on the design requirement which is consistent with the theoretical result. By increasing the switching frequency from 100 to 156.25 kHz and keeping other parameters unchanged, $N_{\max\_\text{DCM}} = 2$ from (23). Fig. 14 shows the simulated waveforms for the corresponding signals in a SIDO buck LED driver. The simulated LED current ripple Δi_{LED} is $24\%_{\text{P-P}}$ and the corresponding output voltage ripple Δv_o is $2.3\%_{\text{P-P}}$, both of which satisfy their corresponding maximum ripple requirement. Consequently, both the theoretical and simulation results show that by increasing the switching frequency, a SIDO buck LED driver in DCM is feasible.

A third LED string is added to the SIDO buck LED driver to transform it into SIMO consisting of three independently driven LED strings. The LED current in each string remains unchanged at 80 mA as in the SISO or SIDO case. According to Fig. 11, the theoretical model suggests that for $I_{\text{LED}} = 80$ mA, a *scalable BCM-based SIMO* scheme with a maximum of *three* LED strings is feasible under the $40\%_{\text{P-P}}$ current ripple constraint. The switching period T_s is chosen to be 6 μs using (13) which corresponds to a switching frequency of 166.67 kHz. Fig. 15 shows the simulated waveforms from the resulting SIMO buck LED driver. The simulated LED current ripple Δi_{LED} is around $35\%_{\text{P-P}}$ and the output voltage ripple Δv_o is $3.5\%_{\text{P-P}}$, both of which satisfy their respective maximum ripple constraint. As a sanity check, the theoretical model based on (22) indeed suggests that a maximum possible number of *three* independently driven LED strings can be achieved in the *scalable BCM-based SIMO* scheme. Hence, it is shown that the simulation result agrees with the corresponding theoretical result. On the other hand, it is important to examine the transient performance of the

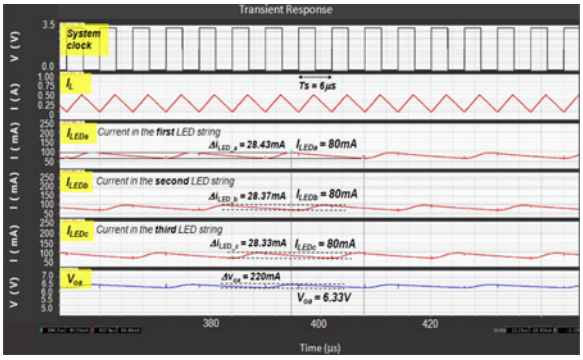


Fig. 15. Simulated steady-state waveforms of a three-string SIMO buck LED driver operating in BCM.

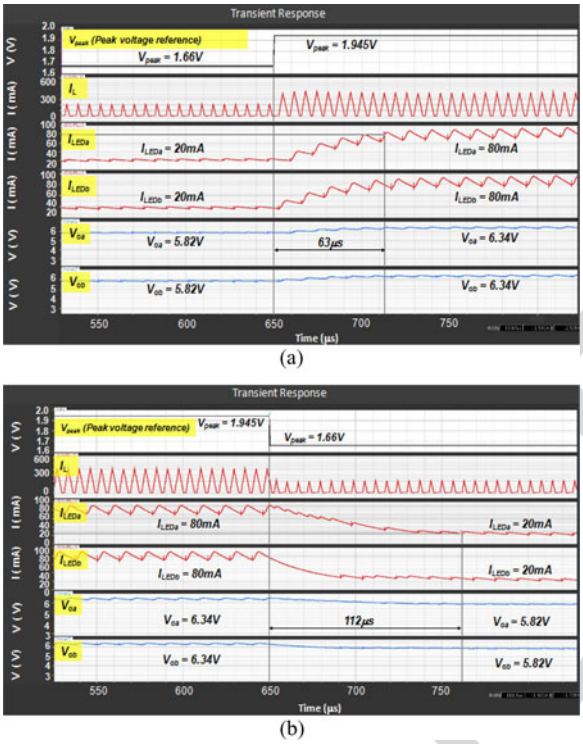


Fig. 16. Simulated transient waveforms for (a) peak reference step-up and (b) peak reference step-down response.

proposed SIDO buck LED driver. The LED current is changed by adjusting the peak limit of the inductor current. By stepping up the peak voltage reference ($V_{\rm peak}$ in Fig. 1) from 1.660 to 1.945 V in 400 ns, the peak inductor current limit is increased by approximately 200 mA, leading to an increase in the nominal LED current from 20 to 80 mA. The reference voltages ($V_{{\rm ref}a}, V_{{\rm ref}b}$) are also stepped up from 100 to 340 mV in order to maintain the same load current between the two LED strings. Conversely, by stepping down $V_{\rm peak}$ from 1.945 to 1.660 V, the LED current is reduced from 80 to 20 mA. Fig. 16 shows the simulated transient behavior for the peak voltage reference step-up and step-down response.

In the case of step-up reference response, the LED current in either string settles to the steady-state nominal value of 80 mA within 63 μs. The output voltage reaches its target steady-state value of 6.34 V. In the case of step-down reference response, the LED current in either string settles to the steady-state nominal value of 20 mA in less than 112 μs. The output voltage settles to its new steady-state value of 5.82 V without oscillations. Hence, the simulation results show that the closed-loop system remains in stable condition in response to a peak voltage reference transient.

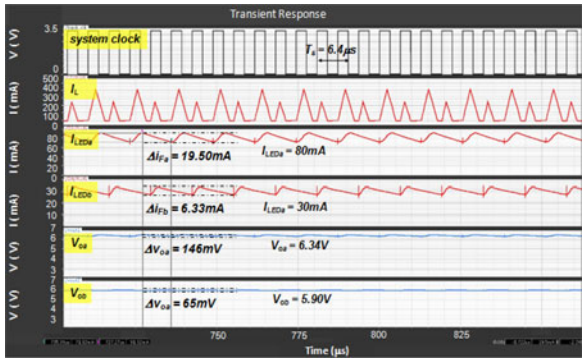


Fig. 17. Simulated steady-state waveforms of a SIDO buck LED driver with unbalanced load.

The effectiveness of the proposed SIDO converter to drive unbalanced load is also investigated. As an example, the first and second LED strings require an average current value of 80 and 30 mA, respectively. Unlike the balanced load case with a constant peak inductor current limit, two distinct peak current limits are employed for unbalanced load such that two different average inductor (or load) current values can be generated in alternate clock cycles. Fig. 17 depicts the simulated steady-state waveforms from the SIDO buck LED driver with unbalanced load. The simulation results show that the first and second LED strings are regulated with an average current value of 80 and 30 mA, respectively. For the first string, the simulated current ripple is 24.38%$_{\rm P\text{-}P}$ and the output voltage ripple is 2.3%$_{\rm P\text{-}P}$. Also, for the second string, the simulated current ripple is 21.1%$_{\rm P\text{-}P}$ and the output voltage ripple is 1.1%$_{\rm P\text{-}P}$. Either string meets the maximum ripple requirements. The simulation results demonstrate that the proposed SIDO converter is capable of delivering unequal currents to the two LED strings simultaneously.

V. Experimental Results

The proposed SIDO buck LED driver was implemented on a field-programmable gate array (FPGA)-based hardware prototype in accordance with the design specification provided in Table I. The switching frequency is increased to 156.25 kHz in order to satisfy the LED current ripple requirement. A photo of the experimental setup is shown in Fig. 18. The power stage of the buck converter consists of discrete ICs from International Rectifier such as power MOSFETs (IRF7828), dual-channel gate driver (IR2110), and output switches (IRF9388), as well as surface-mount inductor and low-ESR capacitors. In actual implementation, the top level of the proposed digital controller is partitioned into two major functional blocks. The functionality of the first block is to control the switching action of the power

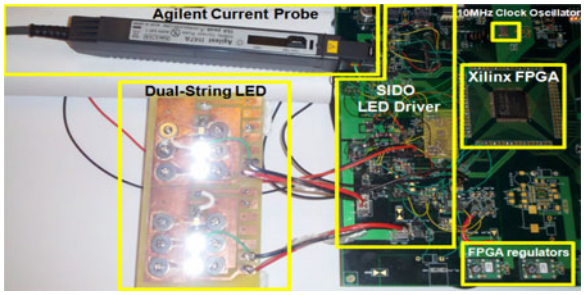


Fig. 18. Experimental setup for the proposed SIDO buck LED driver.

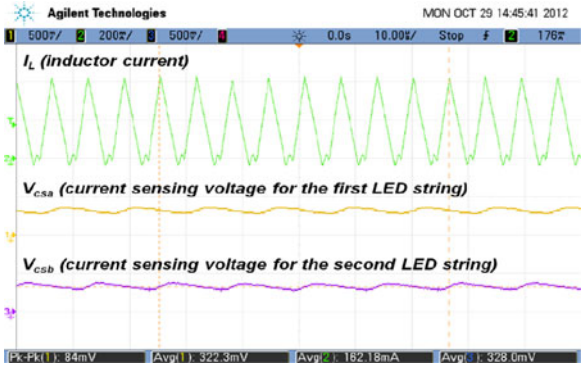


Fig. 19. Measured waveforms for inductor current and current sense feedback voltage.

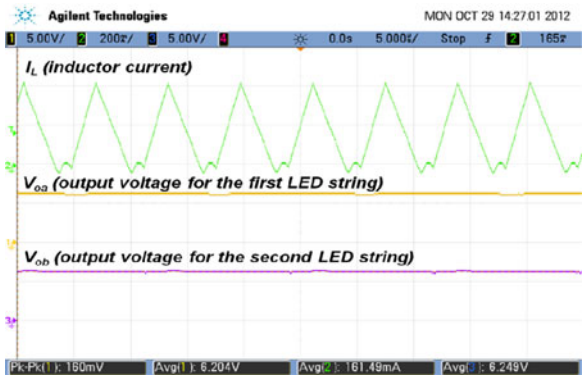


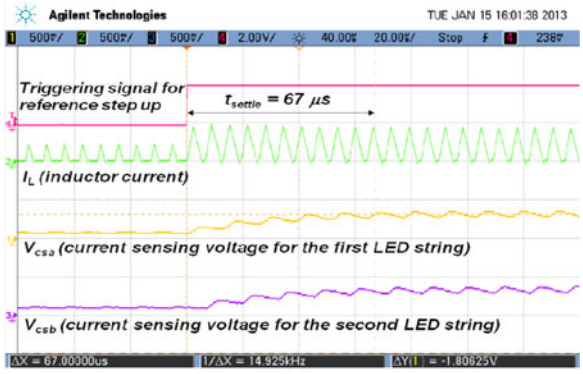
Fig. 20. Measured waveforms for inductor current and output voltage in either LED string.

stage by detecting the peak-crossing and zero-crossing events of the inductor current. It was implemented in hierarchical gate-level schematics using primitives and macros available from the Xilinx Spartan-3 Generation library. Dead-time logic is included to prevent shoot-through current of the power switches. The second logical block is used to control the switching sequence of the two output switches by continuously monitoring the current-sense feedback signals. It was modeled as an FSM in Verilog RTL. Only one of the two output switches can be ON and the other must be OFF per switching cycle. Dead-time logic is also added to prevent cross conduction between outputs. The two logical blocks are synchronized by the system clock to ensure that the high-side power switch and the output switches are triggered from the same clock edge. The entire digital controller was implemented with Xilinx Spartan-3E (XC3S250E) FPGA. The quasi-hysteretic control logic was realized using 4-ns fast comparators (AD8611 from Analog Devices) and semicustom synchronous logic.

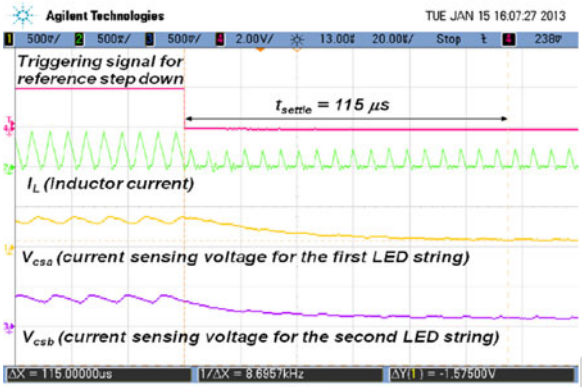
Using a current sensing resistor of 4 Ω and reference voltage of 320 mV, the target current in each of the two LED strings is 80 mA. Fig. 19 shows the current sensing feedback voltage $(V_{\rm csa}, V_{\rm csb})$ from which the corresponding average load current can be obtained, i.e., $I_{\rm LED} = V_{cs}/R_{cs}$. The average inductor current is measured to be 162 mA, which is the sum of the load currents in both LED strings. The average current values in the first and second LED string are measured to be around 80.6 and 82 mA, respectively. The measured LED current ripple $\Delta i_{\rm LED}$ in either string is around $26\%_{\rm P\text{-}P}$, which is reasonably close to the simulated current ripple of $24\%_{\rm P\text{-}P}$. In addition, the nominal output voltages in the first and second string are measured to be 6.204 and 6.249 V, respectively, as shown in Fig. 20. Under this balanced load condition, the measured current and voltage values are in close agreement between the two LED strings. The output voltage ripple is also measured to be around $2.57\%_{\rm P\text{-}P}$, compared to $2.3\%_{\rm P\text{-}P}$ from simulation. Therefore, the experimental results are shown to be consistent with the corresponding simulation ones. On the other hand, the measured power conversion efficiency of the proposed SIDO converter is 80% which is comparable to conventional driving topologies [41]. The efficiency can be further increased by employing a current-sensing resistor with a smaller value.

The transient response of the proposed SIDO buck LED driver is verified experimentally by measuring its peak voltage reference step response. An 8-bit digital-to-analog converter (AD558 from Analog Devices) is used to enable programming of the peak voltage reference $V_{\rm peak}$ and the current-sense voltage references $(V_{{\rm ref}a}, V_{{\rm ref}b})$ by the Xilinx FPGA. The measured waveforms of the inductor current and the voltage at the current sensing nodes in response to a peak voltage reference step are shown in Fig. 21. The settling time of the transient response is also measured and compared with the simulated settling time. For the step-up response, it is observed that the current-sensing voltage $V_{\rm csa}$ in the first LED string steps up from 81.8 to 325.4 mV, which corresponds to an increase in the average load current from 20.5 to 81.3 mA. Similarly, the current-sensing voltage $V_{\rm csb}$ in the second LED string steps up from 94.1 to 327.6 mV, which corresponds to an increase in the average load current from 23.5 to 81.9 mA. The settling time for the step-up response is measured to be 67 μs, compared to 63 μs from simulation. The measured results for the step-down response are the reverse of those from the step-up response. The only difference is that it takes longer for the step-down transient to settle. The settling time for the step-down response is measured to be 115 μs, compared to 112 μs from simulation. The measured settling times are shown to be very close to the simulated ones. The experimental results confirm that the system remains in stable condition when it is perturbed by the peak voltage reference transient.

The unbalanced load scenario in the proposed SIDO buck LED driver is also verified experimentally. The measured average load current values in the first and second LED string are



(a)



(b)

Fig. 21. Measured transient waveforms in response to (a) peak reference step-up and (b) peak reference step-down.

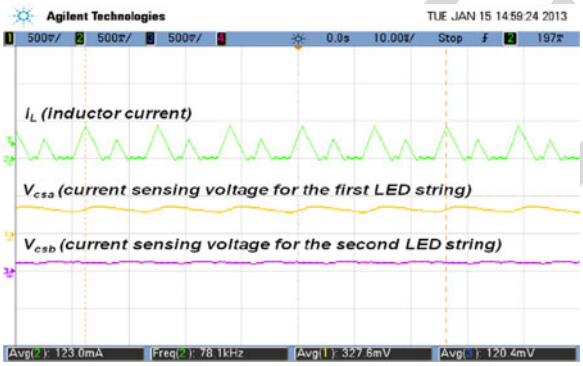


Fig. 22. Measured waveforms for inductor current and current sense voltages.

around 81.9 and 30.1 mA, respectively. Fig. 22 shows the measured waveforms for the inductor current and the current-sensing voltage per string. The inductor current waveform indicates that the proposed driver operates in DCM with *two* distinct peak current limits. Fig. 23 shows the measured inductor current and the output voltage in either string. The measured output voltage values in the first and second LED string are 6.22 and 5.70 V, respectively. The experimental results demonstrate that the proposed driver is capable of driving two independent LED strings concurrently with different load current.

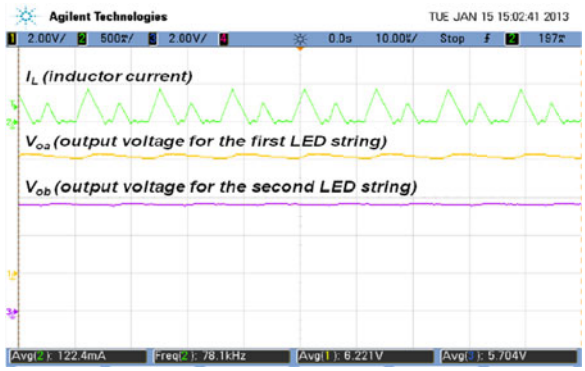


Fig. 23. Measured waveforms for inductor current and output voltages.

VI. Conclusion

The proposed SIDO buck LED driver was implemented in FPGA-based hardware. The experimental results correlate well with simulation ones. The scalability of the proposed SIDO buck LED driver to SIMO is closely examined. A general formula for determining the theoretical maximum achievable number of LED strings in SIMO is derived. The simulation results were shown to be consistent with those obtained from the theoretical model for the same design parameter values. The quasi-hysteretic digital control scheme does not require loop compensation which simplifies the control loop design and reduces component count. In addition, the proposed SIMO architecture offers the advantage of driving a larger number of parallel LED strings without being limited by the maximum current rating of the LED. It also enables dimming for the LED strings without additional dimming transistors. Local bus voltage and current optimization in each individual LED string compensates for the variability of the LED's forward voltage, which reduces power loss and enables mixing of white LEDs from different bins to lower LED costs.

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Scalability of Quasi-Hysteretic FSM-Based Digitally Controlled Single-Inductor Dual-String Buck LED Driver to Multiple Strings

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***Abstract*—There has been growing interest in single-inductor multiple-output (SIMO) dc–dc converters due to its reduced cost and smaller form factor in comparison with using multiple single-output converters. An application for such a SIMO-based switching converter is to drive multiple LED strings in a multichannel LED display. This paper proposes a quasi-hysteretic finite-state-machine-based digitally controlled single-inductor dual-output buck switching LED driver operating in discontinuous conduction mode (DCM) and extends it to drive multiple outputs. Based on the time-multiplexing control scheme in DCM, a theoretical upper limit of the total number of outputs in a SIMO buck switching LED driver for various backlight LED current values can be derived analytically. The advantages of the proposed SIMO LED driver include reducing the controller design complexity by eliminating loop compensation, driving more LED strings without limited by the maximum LED current rating, performing digital dimming with no additional switches required, and optimization of local bus voltage to compensate for variability of LED forward voltage V_F in each individual LED string with smaller power loss. Loosely binned LEDs with larger V_F variation can, therefore, be used for reduced LED costs.**

***Index Terms*—Boundary conduction mode (BCM), discontinuous conduction mode (DCM), finite-state machine (FSM), single-inductor dual-output (SIDO), single-inductor multiple-output (SIMO).**

I. Introduction

An LED driver is essentially a current source (or sink) which maintains a constant current required for achieving the desired color and luminous flux from an array of LEDs. A number of highly efficient switching LED drivers have been reported in the literature and their primary objective is to achieve high power conversion efficiency [1]–[11]. Besides efficiency, another important consideration is the scalability of the existing single-inductor dual-output (SIDO) switching converter to drive multiple independent LED strings in a single-inductor multiple-output (SIMO) topology for reduced cost and smaller form factor [12]. However, in practice, only a finite number of outputs can be served by each LED driver.

The prior arts of SIMO switching converter use either one of two ways to distribute energy from a single power supply to multiple outputs with a single inductor, namely multiple energizing phases [13]–[20] and single energizing phase per switching cycle [21]. The former with time-multiplexing control leads to much better suppression of cross regulation because the outputs are decoupled in time. In this paper, a quasi-hysteretic finite-state machine (FSM)-based digital control scheme is employed in a SIDO buck LED driver consisting of two independent parallel strings operating in discontinuous conduction mode (DCM). The extension of this SIDO architecture to SIMO is formally investigated. The proposed SIMO-based switching buck LED driver enables separate control of the three primary colors (red, green, and blue), thereby offering more flexibility for color mixing. The rest of this paper is organized as follows. Section II introduces the proposed quasi-hysteretic FSM-based digital controller for a SIDO switching buck LED driver operating in DCM. Section III provides a theoretical analysis on the scalability of the proposed digital control scheme from SIDO to SIMO and suggests a general formula for determining the theoretical upper bound in the total number of outputs in SIMO. Section IV shows Cadence Spectre simulation results that are used to verify the theoretical model. Section V contains the experimental results for the proposed digitally controlled SIDO buck LED driver. Section VI concludes our research effort.

II. Quasi-Hysteretic FSM-Based Digital Control for SIDO LED Driver

A SIDO switching converter with time-multiplexing control scheme operating in DCM was first reported in [13]–[16]. With such kind of time-multiplexing control scheme, a SIDO converter can easily be extended to drive multiple outputs and it exhibits negligible cross regulation in DCM. A SIMO parallel-string LED driver operating in DCM has recently been reported [12]. It uses an analog-based controller with dominant pole compensation for stability, and time-multiplexing control in DCM is employed to suppress cross regulation among the LED strings. Unlike conventional pulse width modulation (PWM)-based analog controllers, the proposed digital controller utilizing quasi-hysteretic control does not require any compensation circuits because of its inherent stability [22]–[24], hence simplifying the control loop design and reducing the component count and cost. Quasi-hysteretic control offers a good

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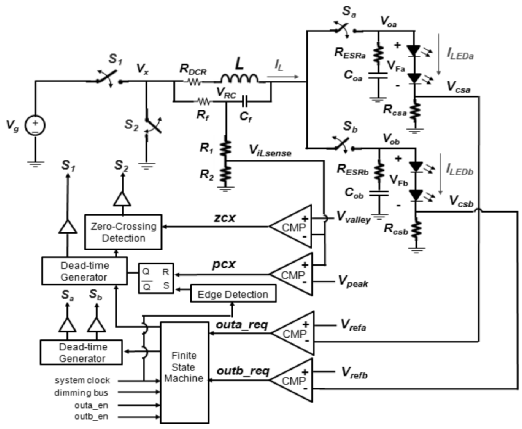


Fig. 1. System architecture of the quasi-hysteretic FSM-based digitally controlled SIDO buck LED driver.

compromise between traditional fixed-frequency PWM control and pure hysteretic control with variable switching frequency. In the proposed design, an external clock is used to synchronize the buck LED driver which switches at a fixed frequency. Fast comparators are used to control the on-time of the high-side and low-side power switches by monitoring the inductor current. This is particularly suitable for lighting applications where variable switching frequencies are not desirable. The reconfigurability and scalability of a digital controller makes it especially attractive for SIMO.

A major drawback of the previously proposed SIMO LED driver operating in DCM [12] is that since the LED current is discontinuous, the LED endures a higher maximum peak current for the same average current required. In other words, the LED could potentially be operating close to its absolute maximum current rating, thereby increasing the current stress and possibly shortening the operating lifetime of the LED. In their approach, the LED current scales with the number of LED strings in SIMO. Hence, the maximum current rating of the LED unnecessarily restricts the maximum achievable number of LED strings which can be implemented in SIMO. In the proposed design, the LED current is always continuous and the LED can be regulated very close to the target average current value which is much lower than its maximum current rating. During the time interval when the output switch is OFF, the output capacitor, acting as a constant current source, continues to discharge its current to the corresponding LED string. When the output switch is ON, the power stage is reconnected to the LED string and the inductor current is transferred to the output capacitor and the LED string simultaneously. The current-sense feedback control ensures that the LED current is maintained at the desired dc level. Hence, a time-continuous current is supplied to the LED string. Consequently, the LED current does *not* scale with the number of LED strings in the proposed SIMO architecture, making it possible to drive more LED strings without inducing too much stress on the LEDs. Fig. 1 shows the system architecture of the proposed quasi-hysteretic FSM-based digitally controlled SIDO buck switching LED driver which takes into account the parasitic effects including the dc resistance (DCR) of the inductor L and equivalent series resistance (ESR) of the output capacitors (C_{oa}, C_{ob}). The two independently driven LED strings share the same inductor L and the two main power switches (S_1, S_2) of the buck converter. The output switches (S_a, S_b) enable the charge stored in the inductor to be distributed between the two outputs in a time-multiplexed fashion. Dead-time generators are used to eliminate shoot-through current by ensuring that S_1 and S_2 are not turned ON simultaneously. Dead-times are also introduced between S_a and S_b to prevent inadvertent cross conduction between the two LED strings.

Since an LED is essentially a current driven device, an LED driver typically regulates the LED current rather than its forward voltage. A straightforward way is to insert a small high-precision current sensing resistor $(R_{\rm csa}, R_{\rm csb})$ in series with the corresponding LED string to sense the LED current by converting it to the current-sense voltage $(V_{\rm csa}, V_{\rm csb})$. The current-sense voltage is then compared with the reference voltage $(V_{\rm refa}, V_{\rm refb})$ to generate the corresponding logic signals (*outa_req*, *outb_req*) which determine the opening or closing of the two output switches in a SIDO buck converter. Since the LED's *I–V* curve is usually provided by the LED manufacturer, the target dc current value for a particular LED string can be set by choosing an appropriate reference voltage. On the other hand, a two-limit hysteretic control determines the on-time of the high-side and low-side power switches (S_1, S_2) of the buck converter. The upper and lower limits of the inductor current, namely the peak current limit and the valley current limit, define the average value of the inductor current which is the *total* LED current for a SIDO buck LED driver. In DCM, the valley current limit is set to zero to prevent the inductor current from going negative which degrades the power conversion efficiency [12], [16], [25]. As illustrated in Fig. 1, R_fC$_f$ is connected in parallel to the inductor so that the slopes of V_{RC} are proportional to the inductor current ramp-up and ramp-down slopes [26]. A small resistor ladder is connected between V_{RC} and ground in order to generate a lower voltage signal $V_{iLsense}$ which falls within the input voltage range of the comparator (CMP). $V_{0iLsense}$ is fed forward to the corresponding comparators to determine the peak-crossing and zero-crossing of the inductor current. Fig. 2 is a simplified flowchart showing the system-level operation of the proposed SIDO buck driver. Suppose identical current flows through each of the two LED strings, also referred to as the *balanced load* condition, the inductor current I_L is assigned to each string in alternate switching cycles. The working principle of the proposed SIDO buck LED driver is represented by the timing diagram shown in Fig. 3. During $D_{1a}T_s$ or $D_{1b}T_s$, I_L ramps up with a slope of $m_1 = (V_g - V_o)/L$ and the inductor is charged with a voltage of $V_L = V_g - V_o$, where V_g and V_o represent the input voltage and the output voltage, respectively. During $D_{2a}T_s$ or $D_{2b}T_s$, I_L ramps down with a slope of $m_2 = -V_o/L$ and the inductor discharges its current to the corresponding output capacitor and the LED string until I_L returns to zero. During $D_{3a}T_s$ or $D_{3b}T_s$, I_L stays at zero with both S_1 and S_2 OFF. In the proposed SIDO LED driver, the system clock defines the switching frequency. The rising edge of the system clock triggers the ON duty cycle ($D_{1a}T_s$, D_1bT_s) by charging up the inductor during which S_1 is ON and S_2 is OFF. The

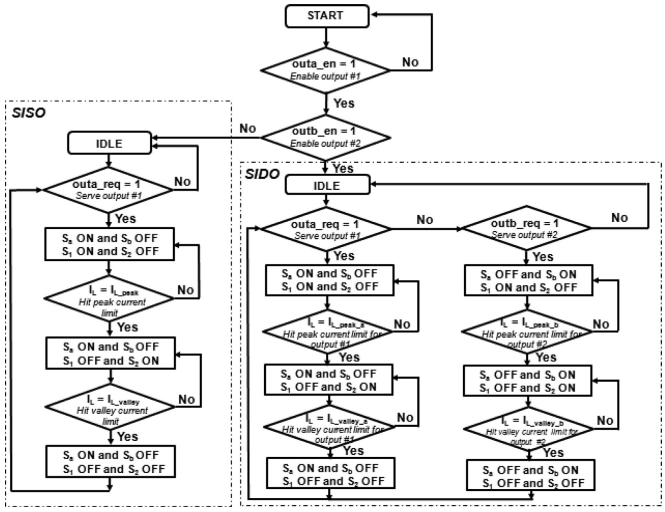


Fig. 2. Simplified flowchart representing the system-level operation of the proposed SIDO buck LED driver.

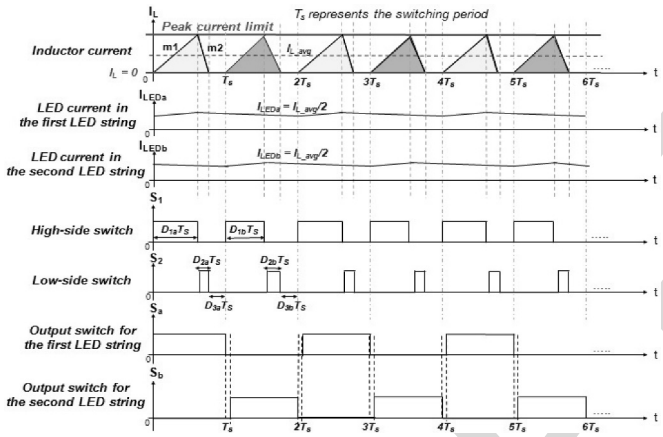
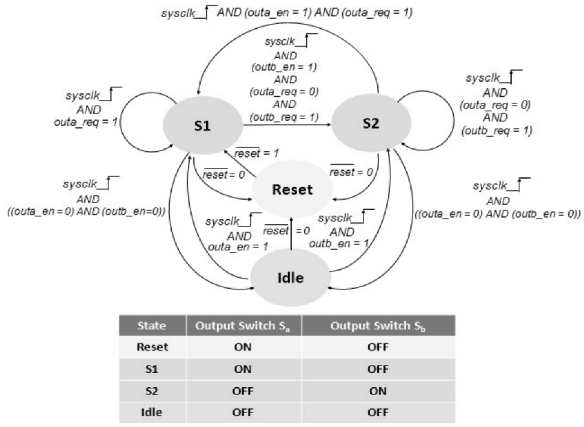


Fig. 3. Timing diagram of the proposed SIDO buck LED driver with balanced load operating in DCM.



State	Output Switch S_a	Output Switch S_b
Reset	ON	OFF
S1	ON	OFF
S2	OFF	ON
Idle	OFF	OFF

Fig. 4. State diagram of the proposed FSM for controlling the two output switches in SIDO buck LED driver.

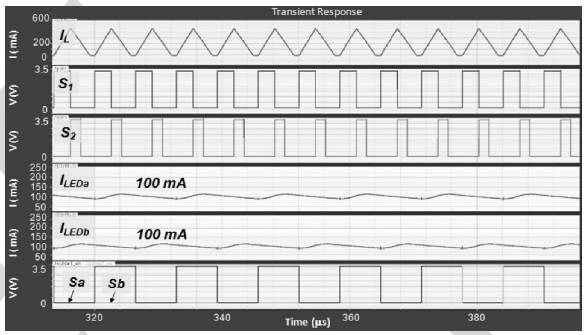


Fig. 5. Simulated steady-state waveforms for the proposed SIDO buck LED driver operating in DCM.

inductor current continues to increase until it hits the peak current limit at which point the buck converter enters $(D_{2a}T_s, D_{2b}T_s)$ where S_1 is OFF and S_2 is ON. The inductor discharges its current to the corresponding output until the zero-crossing of the inductor current is detected. The converter then enters the idle phase $(D_{3a}T_s,\ D_{3b}T_s)$ during which both S_1*and* S_2 are OFF. The inductor current remains at zero until the next rising edge of the system clock arrives and the switching sequence repeats itself. The two output switches $(S_a,\ S_b)$ are controlled by the FSM as shown in Fig. 4.

The state machine is triggered by the rising edge of the system clock (*sysclk*) so that the transitions of the output switches (S_a, S_b) are in sync with the system clock. The input signals of the state machine are the output enable signals (*outa_en*, *outb_en*) and the output request signals (*outa_req*, *outb_req*) which determine the switching sequence of the two outputs. The first LED string is always given a higher priority over the second one. For instance, if both strings request service simultaneously, i.e., *outa_req* $= 1$ and *outb_req* $= 1$, S_a is turned ON first and S_b remains OFF. S_b is turned ON only when *outa_req* $= 0$ and *outb_req* $= 1$. S_a and S_b must be nonoverlapping to avoid undesirable cross conduction between the two LED strings. In addition, an enable signal (*out1en*, *out2en*) is associated with either of the two LED strings. It provides the option of shutting down any or all of the LED strings, for example, in response to an overcurrent fault condition. An overriding signal can also be sent from the FSM to the hysteretic controller to disable the high-side and low-side power switches accordingly. The FSM-based controller can be modified quickly and conveniently to drive multiple LED strings in a SIMO configuration by simply adding more states in the VHDL or Verilog code. A mixed-signal macromodel of the proposed FSM-based digitally controlled SIDO buck switching LED operating in DCM is simulated in the time domain using Cadence Spectre [27]. The FSM is modeled in Verilog RTL and the rest are modeled as ideal circuit elements. The simulation model also incorporates parasitics such as DCR of the inductor L and ESR of the output capacitors (C_{oa}, C_{ob}). For *balanced load* condition, the current between the two LED strings is identical and each string consists of *two* LEDs connected in series. First, the steady-state performance is investigated. Fig. 5 contains the simulated steady-state waveforms for the inductor current (I_L), the LED current $(I_{\mathrm{LED}a}, I_{\mathrm{LED}b})$, and the four switches (S_1, S_2, S_a, S_b) of the proposed SIDO buck LED driver operating in DCM. The switching frequency is 156.25 kHz and the input voltage V_g is 15 V. The simulation results show that the LED current in either

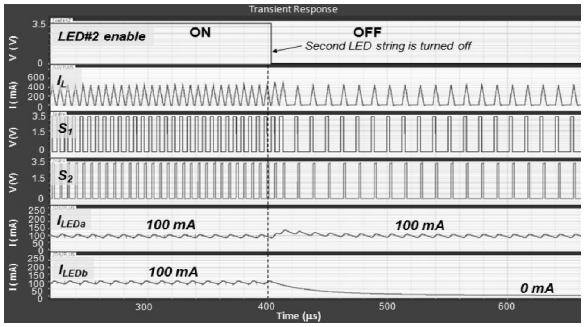


Fig. 6. First LED string remains under regulation without cross regulation when the second LED string is shut down completely.

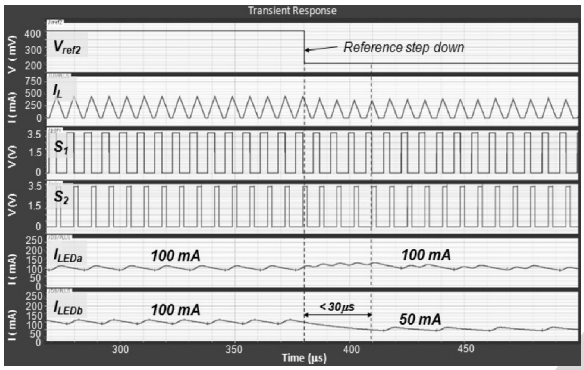


Fig. 7. First LED string remains under regulation without cross regulation despite a reference step in the second LED string from 100 to 50 mA in 20 ns.

of the two strings is regulated successfully to the target steady-state dc value of 100 mA with a current ripple of $23\backslash\%_{\text{P-P}}$. The steady-state output voltage for the first and second LED string is approximately 6.48 V with a voltage ripple of $2.6\%_{\text{P-P}}$. Second, the stability of the closed-loop system is verified by examining its dynamic performance. In the first scenario, the second LED string needs to be shut down instantly in response to an over-current condition. Fig. 6 shows that despite the immediate shutdown of the second LED string, the LED current $I_{\text{LED}a}$ in the first LED string continues to be regulated successfully at its target nominal value of 100 mA with minimal cross regulation. In the second scenario, the second LED string experiences a reference step of 50 mA, i.e., $I_{\text{LED}b}$ transitions from 100 to 50 mA in 20 ns. Fig. 7 shows that the current in the first LED string continues to be regulated at around 100 mA, virtually unaffected by the sudden reference step in the other string. The second LED string settles to the new nominal current value of 50 mA. It demonstrates that the closed-loop system remains stable in response to the reference transient in the second string.

Unlike conventional backlight LED drivers that use PWM dimming transistor connected in series with the LED string [3], [8], [28]–[31], the proposed SIDO LED driver takes advantage of the existing four switches to perform dimming without requiring additional switches. When the dimming control signal for a particular LED string goes high, certain phases of the inductor current are skipped so that the average inductor current (also the average load current) going into that string is reduced accordingly. The digital dimming control signals (*dim_ctrl1*, *dim_ctrl2*) essentially modulate the dc current level flowing through the corresponding LED string. No additional dimming transistors in series with the LED string are required, thereby leading to a smaller voltage headroom and reduced power loss. The only voltage headroom is the voltage across the current-sense resistor $(V_{\text{csa}}, V_{\text{csb}})$ which is typically between 0.2 and 0.4 V. Fig. 8 depicts the timing diagram of the proposed digital dimming control scheme. In this particular case, the second LED string is dimmed by reducing its current from 100 to 50 mA, while the current in the first LED string stays constant at 100 mA.

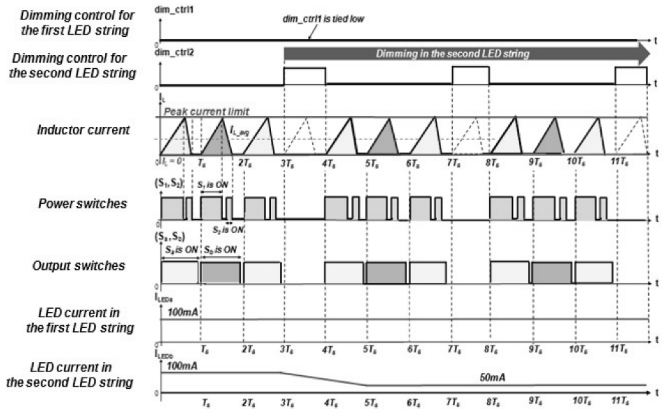


Fig. 8. Proposed digital dimming control in SIDO buck LED driver.

Any combination of LED strings in a SIMO LED driver can be dimmed or even shut down momentarily to achieve flexible dimming and optimum luminance levels. In addition, it is reported in the literature [32]–[34] that a bilevel or N-level current driving technique for LED dimming improves the luminous efficacy of LEDs by introducing a dc offset to the PWM current. The proposed SIDO converter can potentially be used as a bilevel LED driver by generating two programmable dc current values for each individual LED string in a time-multiplexed fashion. Another major difference between the proposed LED driver and the existing ones [3], [8], [28]–[31] is that the former provides N optimized output bus voltage for each individual LED string, whereas the latter only uses a common output bus shared by all the LED strings. Due to manufacture, process, and temperature variations, V_F in each LED does not match perfectly, which means that the voltage drop across each LED string differs. Using the proposed SIDO buck LED driver in Fig. 1 as an example and assuming the LED current is 100 mA in each string, the voltage headroom $(V_{\text{csa}}, V_{\text{csb}})$ is 0.4 V, and the voltage drop across each of the two LED strings are $V_{Fa} =$ 6.0 V and $V_{Fb} = 7.0$ V, respectively. The output voltages are $V_{oa} = 6.4$ V and $V_{ob} = 7.4$ V. The total power consumption of the load P_{LOAD}, including the LED string and current-sense resistor, is $P_{\text{LOAD}} = V_{oa} \times I_{\text{LED}} + V_{ob} \times I_{\text{LED}} = 1.38$ W. The output voltage for each LED string is independently optimized based on its corresponding V_F, resulting in the same voltage headroom of 0.4 V for each string. This is different from a conventional LED driver in which the common output bus voltage is usually regulated using the LED string with the maximum voltage drop. For the same LED current, the total power consumption using a conventional LED driver is given by: $P_{\text{LOAD}} =$

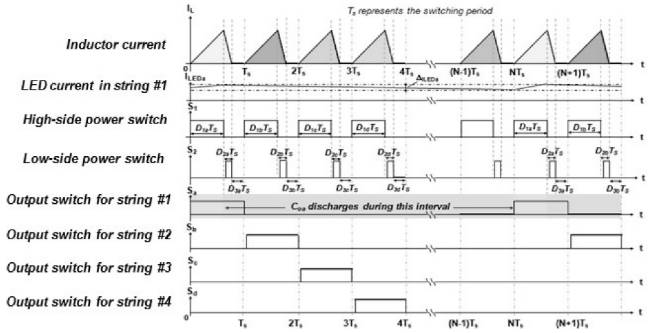


Fig. 9. Timing diagram of the proposed SIMO buck LED driver.

$2 \times \max(V_{oa}, V_{ob}) \times I_{\rm LED} = 1.48$ W, which is more than 7% higher than that of the proposed driver. The voltage headroom for the first LED string increases from 0.4 to 1.4 V, resulting in 450 mW more power loss or additional 30% efficiency degradation. Since the output voltage is self-optimized to match the total V_F in each individual LED string in the proposed driver, same-colored LEDs from neighboring bins (not only from a single bin) with larger V_F variance can be used which helps reduce the LED costs. In the event that a particular application demands a total LED current greater than the average inductor current, the same time-multiplexing control scheme operating in DCM can still be employed either by lowering the switching frequency with a higher inductor peak current limit or by operating the buck LED driver in pseudocontinuous conduction mode (PCCM) [17], [35], [36]. In PCCM, the average inductor current is increased by simply adding a nonzero dc offset of $I_{\rm DC}$ to that of DCM.

III. Extension From SIDO to SIMO Buck LED Driver

Having demonstrated the feasibility of the proposed SIDO buck LED driver, it is natural for us to extend it to SIMO with N independently driven LED strings. In particular, the theoretical maximum number of LED strings $N_{\max}$ is determined for this SIMO architecture. Fig. 9 shows a timing diagram of the inductor current, the two power switches (S_1, S_2), and the first four output switches (S_a, S_b, S_c, S_d) in a SIMO buck LED driver. To simplify the analysis, the *balanced load* condition is assumed. Based on the time-multiplexing control scheme, energy is being transferred from the dc supply to each individual output *exactly once* within a total of N switching phases. For a particular output, the corresponding output switch is OFF during D_3, while the output capacitor discharges to the LED string. During the subsequent $(N-1) \times T_s$ phases, the output switch remains OFF and the output capacitor continues to discharge to the corresponding LED string. Hence, the *total* discharging time for the output capacitor $t_{\rm dch}$ can be expressed as

$$t_{\rm dch} = D_3 T_s + (N-1)T_s = (D_3 + N - 1)T_s. \quad (1)$$

$$\text{For } D_3 = 0, t_{\rm dch} = (N-1)T_s. \quad (2)$$

The proposed SIMO buck LED driver is essentially a constant-current regulator which maintains a constant dc current $I_{\rm LED}$ flowing through the LED string via a closed-loop current-sense feedback control. For very small variation of forward voltage around the quiescent point (also known as bias point) on the LED's exponential *I–V* curve, the dc forward current is assumed to be constant. During $t_{\rm dch}$ when the output switch is OFF, the output capacitor is connected to the LED string which acts as a constant-current sink (CCS). Assuming ideal capacitor with no ESR (the effect of the ESR will be explained later), the voltage across the output capacitor v_c(t) is the same as the output voltage which is expressed as the charge *q(t)* divided by the capacitance value C_o, i.e.,

$$v_c(t) = \frac{q(t)}{C_o} = \frac{1}{C_o}\int_0^{t_{\rm dch}} i_c(\tau)d\tau + v_c(0). \quad (3)$$

$$\text{For CCS, } i_c(\tau) = I_{\rm LED}. \quad (4)$$

Combining (3) and (4) and rearranging, we have

$$\Delta v_o = \Delta v_c = v_c(t) - v_c(0) = \frac{1}{C_o}(I_{\rm LED}\, t_{\rm dch}). \quad (5)$$

Hence, the *total* discharging time $t_{\rm dch}$ can be expressed as

$$t_{\rm dch} = \frac{C_o \Delta v_o}{I_{\rm LED}} \quad (6)$$

where Δv_o is the output voltage drop due to the discharging of the output capacitor. In general, Δv_o is assumed to be reasonably small relative to the output voltage. The LED ripple current $\Delta i_{\rm LED}$ usually ranges from $10\%_{\text{P-P}}$ to $40\%_{\text{P-P}}$ of the dc forward current as recommended by the LED manufacturers [37], [38]. For a particular $\Delta i_{\rm LED}$, the corresponding voltage ripple $\Delta v_{\rm LED}$ at the chosen bias point can be readily obtained from the exponential *I–V* curve. Suppose each LED string contains a total of n LEDs connected in series. The output voltage ripple Δv_o is, therefore, the sum of the voltage ripple across the LED string and the voltage ripple across the current-sense resistor, i.e., $\Delta v_o = n \times \Delta v_{\rm LED} + \Delta v_{cs}$. Suppose $\Delta v_{o\max}$ represents the *maximum* output voltage ripple allowed. Equation (6) can, therefore, be rewritten as

$$t_{\rm dch} \le \frac{C_o \Delta v_{o\max}}{I_{\rm LED}}. \quad (7)$$

Substituting (1) into (7), we have

$$(D_3 + N - 1)T_s \le \frac{C_o \Delta v_{o\max}}{I_{\rm LED}} \Rightarrow N \le \frac{C_o \Delta v_{o\max}}{I_{\rm LED} T_s} + 1 - D_3. \quad (8)$$

Hence, the theoretical maximum possible number of LED strings in SIMO, $N_{\max}$, is given by

$$N_{\max} = \frac{C_o \Delta v_{o\max}}{I_{\rm LED} T_s} + 1 - D_3 = \frac{C_o \Delta v_{o\max}}{I_{\rm LED} T_s} + D_1 + D_2. \quad (9a)$$

Since $N_{\max}$ is an integer value, the *floor*$(\cdot)$ function is used to round the result down to the closest integer. Hence, (9a) becomes

$$N_{\max} = \text{floor}\left(\frac{C_o \Delta v_{o\max} + I_{\rm LED} T_s (1 - D_3)}{I_{\rm LED} T_s}\right). \quad (9b)$$

Equation (9b) represents a general formula for determining the scalability limit of a SIMO buck LED driver operating in DCM

and is referred to as a *scalable DCM-based SIMO scheme* for the sake of our ensuing discussion. In particular, when $D_3 = 0$, the SIMO buck LED driver operates in boundary conduction mode (BCM). Hence, (9a) and (9b) become (10a) and (10b), respectively. Also, $N_{\max}$ in BCM is greater than or equal to that in DCM for the same set of design parameter values

$$N_{\max} = \frac{C_o \Delta v_{o\max}}{I_{\rm LED} T_s} + 1 \tag{10a}$$

$$N_{\max} = \text{floor}\left(\frac{C_o \Delta v_{o\max}}{I_{\rm LED} T_s} + 1\right). \tag{10b}$$

For a single-output buck converter, the average inductor current is identical to the load current. Due to the nature of the time-multiplexing control scheme in the proposed SIMO converter, the average inductor current $I_{L\_\rm avg}$ is the *sum* of the individual load current $I_{\rm LED}$ in each LED string. Assuming balanced load condition, $I_{L\_\rm avg} = N \times I_{\rm LED}$, where N is the total number of LED strings. The average inductor current reaches its maximum value in BCM, resulting in a maximum transfer of power [16]. Since the current in each LED string remains the same, a theoretical upper bound of the total achievable number of LED strings in SIMO can be expressed as

$$N_{\max} = \frac{I_{L\_\rm avg\_max}}{I_{\rm LED}}. \tag{11}$$

By simple geometry, $I_{L\_\rm avg\_max}$ is given by the following equation [39]:

$$I_{L\_\rm avg\_max} = \frac{m_1 D_1 T_s}{2} = \frac{(V_g - V_o) D_1 T_s}{2L}. \tag{12}$$

By substituting (12) into (11) and rearranging, T_s can be expressed as

$$T_s = \frac{2LN_{\max} I_{\rm LED}}{D_1 (V_g - V_o)}. \tag{13}$$

Now, by substituting (13) into (10a) and rearranging, we have

$$2LI_{\rm LED}^2 N_{\max}^2 - 2LI_{\rm LED}^2 N_{\max} - C_o \Delta v_{o\max} (V_g - V_o) D_1 = 0. \tag{14}$$

Equation (14) is a quadratic equation in $N_{\max}$. The discriminant Δ of (14) can be expressed as

$$\Delta = 4L^2 I_{\rm LED}^4 + 8LI_{\rm LED}^2 C_o \Delta v_{o\max} (V_g - V_o) D_1 > 0. \tag{15}$$

Since $(V_g - V_o) > 0$ for a buck switcher, the discriminant in (15) is always a positive number which implies that (14) has two real roots as given by

$$r_1, r_2 = \frac{2LI_{\rm LED}^2 \pm \sqrt{\Delta}}{4LI_{\rm LED}^2}. \tag{16}$$

Since $N_{\max}$ must be a *positive integer*, the negative root is eliminated, leaving only the positive root, i.e.,

$$N_{\max\_\rm BCM} = \text{floor}\left(\frac{1}{2} \times \left[1 + \sqrt{1 + \frac{2C_o \Delta v_{o\max} V_o (V_g - V_o)}{LI_{\rm LED}^2 V_g}}\right]\right) \tag{17}$$

Equation (17) defines the theoretical maximum total number of outputs in SIMO operating in BCM. It is referred to as a *scalable BCM-based SIMO scheme* which is a special case of *scalable DCM-based SIMO scheme*. In fact, it is observed that (11) is also valid for the case of DCM. By simple geometry, the switching period T_s in DCM can be expressed as

$$T_s = \frac{2LN_{\max} I_{\rm LED}}{D_1 (D_1 + D_2)(V_g - V_o)}. \tag{18}$$

Realizing that the same calculations that lead to (17) for the case of BCM can also be performed in DCM, the theoretical maximum total number of LED strings in a SIMO converter operating in DCM can, therefore, be written as[1]

$$N_{\max\_\rm DCM} = \text{floor}\left(\frac{1}{2} \times (1 - D_3) \times \left[1 + \sqrt{1 + \frac{2C_o \Delta v_{o\max} (V_g - V_o) D_1}{LI_{\rm LED}^2 (1 - D_3)}}\right]\right). \tag{19}$$

Notice that for the case of BCM, $D_3 = 0$ and $D_1 = V_o / V_g$, (19) reduces to (17). Hence, (19) represents the generalized formula for the theoretical maximum total number of outputs in SIMO which is applicable to either BCM or DCM. It is also interesting to note that the average inductor current in DCM is smaller than (or equal to) that in BCM. As a result, for the same LED current, the theoretical maximum achievable number of outputs in SIMO operating in DCM is no greater than that in BCM, i.e., $N_{\max\_\rm DCM} \le N_{\max\_\rm BCM}$. In reality, the ESR of the output capacitor needs to be taken into consideration. Any current flowing through the output capacitor C_o must also flow through the $R_{\rm ESR}$, resulting in an additional voltage drop of $\Delta V_{\rm ESR} = I_{\rm LED} \times R_{\rm ESR}$. Hence, Δv_o can be expressed as

$$\Delta v_o = \Delta v_c + \Delta v_{\rm ESR} = \Delta v_c + I_{\rm LED} \times R_{\rm ESR}. \tag{20}$$

Rearranging the terms in (20), we have

$$\Delta v_c = \Delta v_o - I_{\rm LED} \times R_{\rm ESR}. \tag{21}$$

Hence, (17) and (19) are modified slightly to become (22) and (23), respectively: BCM:

$$N_{\max\_\rm BCM} = \text{floor}\left(\frac{1}{2} \times \left[1 + \sqrt{1 + \frac{2C_o V_o (\Delta v_{o\max} - I_{\rm LED} R_{\rm ESR})(V_g - V_o)}{LI_{\rm LED}^2 V_g}}\right]\right) \tag{22}$$

DCM:

$$N_{\max\_\rm DCM} = \text{floor}\left(\frac{1}{2} \times (1 - D_3) \times \left[1 + \sqrt{1 + \frac{2C_o (\Delta v_{o\max} - I_{\rm LED} R_{\rm ESR})(V_g - V_o) D_1}{LI_{\rm LED}^2 (1 - D_3)}}\right]\right). \tag{23}$$

The presence of $R_{\rm ESR}$ in (22) and (23) reduces the theoretical maximum achievable number of outputs in SIMO. Therefore,

[1] In DCM, D_1 can be expressed as: $D_1 = M\sqrt{\frac{K}{1-M}}$, where $M = \frac{V_o}{V_g}$ and $K = \frac{2L}{R_L T_s} = \frac{2LI_{\rm LED}}{V_o T_s}$ [39].

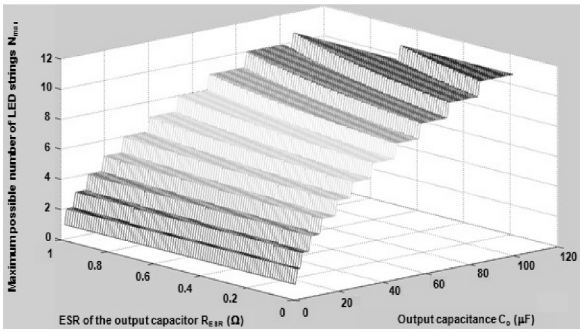


Fig. 10. Theoretical maximum achievable number of LED strings $(N_{\max})$ versus the output capacitance (C_o) and the capacitor ESR $(R_{\rm ESR})$ for the *scalable BCM-based SIMO scheme*.

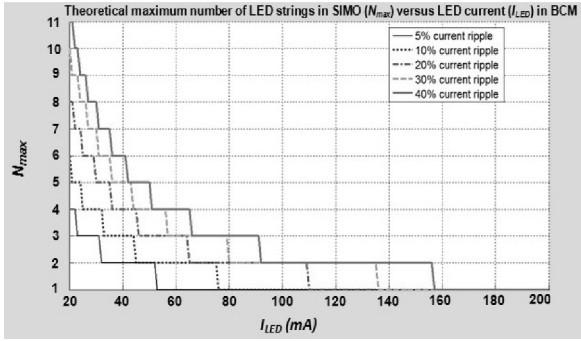


Fig. 11. Plot of theoretical maximum number of LED strings in SIMO $(N_{\max})$ versus the LED current $(I_{\rm LED})$ in the *scalable BCM-based SIMO scheme*.

it is always recommended to choose an output capacitor with a smaller ESR, whenever possible. Fig. 10 shows the theoretical maximum total number of LED strings versus the output capacitance and capacitor ESR for the scalable *BCM-based SIMO scheme*, given an LED current of 80 mA and a maximum ripple current requirement of $40\%_{\rm P\text{-}P}$.

Intuitively, for a particular LED current, an increasing number of outputs can be achieved by using a larger output capacitor with the same ESR value. For instance, if the output capacitance is increased from 4.7 to 22 μF (the ESR remains at 100 mΩ), the theoretical model based on (22) suggests that the maximum total number of LED strings can be increased from three to six. It is also interesting to note that the maximum number of outputs in SIMO has a stronger dependence on the output capacitance than the capacitor ESR, as shown in Fig. 10.

On the other hand, it is useful to study how the LED current affects the maximum achievable number of outputs in SIMO. As an example, assuming balanced load and two LEDs connected in series per string, a *scalable BCM-based SIMO scheme* is investigated with these parameter values: $L = 47$ μH, $C_o = 4.7$ μF, $R_{\rm ESR} = 100$ mΩ, $V_g = 15$ V, and $V_o = 6.4$ V. The relationship between $N_{\max}$ and $I_{\rm LED}$ can be obtained by using (22) for different values of output voltage ripple $\Delta v_{o\_\max}$. Based upon the *I–V* curve and/or SPICE model of the particular LED used, the corresponding output voltage ripple $\Delta v_{o\_\max}$ can be determined from the LED current ripple requirement $\Delta i_{\rm LED}$. The proposed design uses white LED [40] which is the target for LCD backlighting applications. For instance, a $20\%_{\rm P\text{-}P}$ current ripple corresponds to around $2\%_{\rm P\text{-}P}$ voltage ripple and a $40\%_{\rm P\text{-}P}$ current ripple corresponds to around $4\%_{\rm P\text{-}P}$ voltage ripple. Fig. 11 shows a plot of $N_{\max}$ versus $I_{\rm LED}$ for $\Delta i_{\rm LED}$ ranging from $5\%_{\rm P\text{-}P}$ to $40\%_{\rm P\text{-}P}$. This plot is beneficial to a practical SIMO design in two ways. First, for a given LED current and current ripple requirement, the theoretical maximum number of LED strings viable under the *scalable BCM-based SIMO scheme* can be extracted directly from the plot. Second, the maximum LED current allowed in order for a SIMO to remain at the same scaling level can also be obtained from the plot. For instance, given a 20% current ripple requirement (i.e., $\Delta i_{\rm LED} = 20\%_{\rm P\text{-}P}$), a SIDO (dual-string) configuration is possible as long as the LED current in each string is no more than 110 mA. In the event that an application demands an LED current greater than 110 mA, two options can be considered: 1) Relax the current ripple requirement whenever possible. A wider tolerance in $\Delta i_{\rm LED}$ is generally acceptable since the ripple frequency is too high for the human eye to detect. 2) Operate the SIMO buck LED driver in PCCM [17], [35], [36]. In PCCM, the floor of the inductor current is raised by a nonzero dc offset $I_{\rm DC}$ which distinguishes it from DCM. The proposed theoretical model can be extended to PCCM by adding a dc component to the average inductor current. By going through similar calculations as in DCM, the theoretical maximum number of outputs in SIMO operating in PCCM is given by (24), as shown at the bottom of the page. It is interesting to note that (24) continues to apply to the cases of DCM and BCM. For instance, in DCM, $I_{\rm DC} = 0$ and (24), therefore, reduces to (23).

In the event of unbalanced load with unequal current among the LED strings, the *scalable DCM- or BCM-based SIMO scheme* continues to hold. The only change is to replace $I_{\rm LED}$ in (22) and (23) by max$(I_{\rm LED})$, where max$(I_{\rm LED})$ denotes the *largest* LED current among all the LED strings. In other words, the maximum number of LED strings that can be realized in a SIMO buck LED driver is constrained by the *largest* LED current. Generally speaking, the input voltage V_g, output voltage V_o, and the current ripple requirement are typically fixed parameters defined in the design specification. Without making any hardware changes (i.e., *L and* C_o values are fixed), the primary design variable in (22) and (23) is the LED current $I_{\rm LED}$. In fact, the LED current is the dominant factor for determining the maximum possible number of outputs under the *scalable DCM-/BCM-based SIMO scheme*. By knowing the maximum LED current required for a particular application, the theoretical

$$N_{\max\_\rm PCCM} = \text{floor}\left(\frac{1}{2I_{\rm LED}} \times [(I_{\rm DC} + (1-D_3)\, I_{\rm LED}] \times \left[1 + \sqrt{1 + \frac{2C_o(\Delta v_{o\max} - I_{\rm LED} R_{\rm ESR})\,(V_g - V_o)\, D_1(1-D_3)}{L\,[I_{\rm DC} - (1-D_3) I_{\rm LED}]^2}}\right]\right). \tag{24}$$

TABLE I
DESIGN SPECIFICATION OF A SISO BUCK LED DRIVER IN DCM

Design Parameter	Value	Unit
Input Voltage (V_g)	15	V
Output Voltage (V_o)	6.32	V
LED Forward Current (I_{LED})	80	mA
Switching Frequency (f_s)	100	kHz
Inductor (L)	47	μH
Output Capacitor (C_o)	*4.7*	*μF*
ESR of Output Capacitor (R_{ESR})	100	mΩ
Maximum LED Current Ripple (Δi_{LED})	40	$\%_{\text{P-P}}$
Maximum Output Voltage Ripple (Δv_o)	4	$\%_{\text{P-P}}$
Duty Ratio of Idle Phase (D_3)	≥10	%

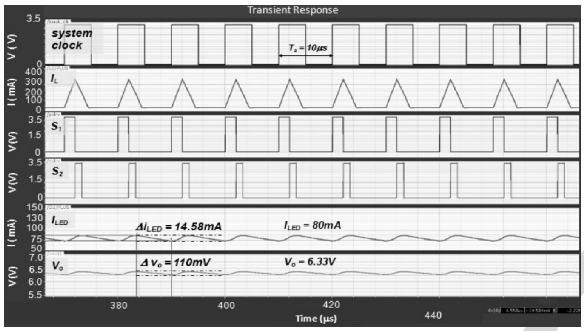


Fig. 12. Simulated steady-state waveforms for the SISO buck LED driver based on the design specification in Table I.

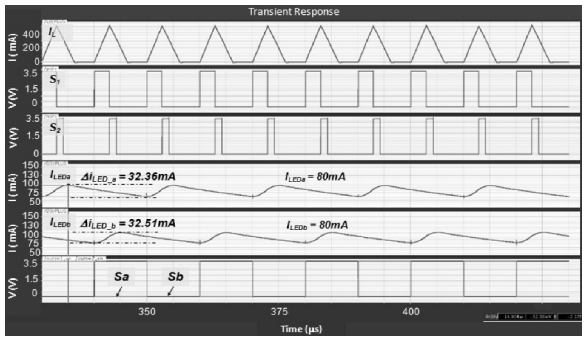


Fig. 13. Simulated steady-state waveforms showing SIDO is not viable since the $30\%_{\text{p-p}}$ maximum current ripple requirement is violated.

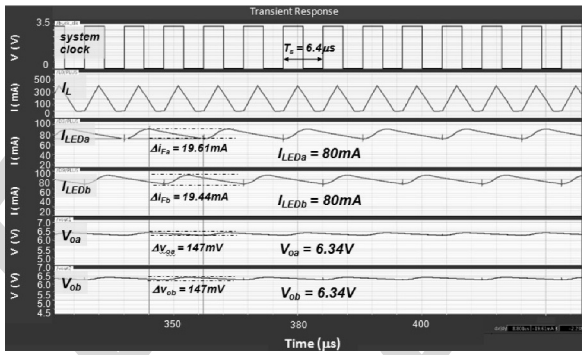


Fig. 14. Simulated steady-state waveforms showing SIDO is possible by increasing the switching frequency from 100 to 156.25 kHz.

maximum achievable number of independently driven LED strings can be estimated in advance.

IV. SIMULATION RESULTS

Ideal macromodels based on the *scalable DCM-based SIMO scheme* were constructed and simulated in Cadence Spectre [27] in order to compare with the theoretical results in Section III. The design specification of a single-inductor single-output (SISO) buck converter is shown in Table I. The theoretical model based on (23) suggests that $N_{\max\_\text{DCM}} = 1$, meaning only one LED string is viable. Fig. 12 shows the simulated steady-state waveforms of the inductor current I_L, the LED currents I_{LED}, and the output voltages V_o of a SISO buck LED driver. The simulated steady-state LED current I_{LED} is approximately 80 mA which meets the design target. The simulated LED current ripple Δi_{LED} is $18\%_{\text{P-P}}$ (also, the output voltage ripple Δv_o is $1.7\%_{\text{P-P}}$), which satisfies the maximum ripple requirement. Now, the SISO buck LED driver is transformed into SIDO by adding a second LED string. Fig. 13 shows the simulated steady-state waveforms from the resulting SIDO LED driver.

Despite the fact that the steady-state LED current in either string remains at 80 mA, the LED current ripple is more than $40\%_{\text{P-P}}$ which violates the maximum ripple current requirement. Hence, the simulation results show that SIDO is not viable based on the design requirement which is consistent with the theoretical result. By increasing the switching frequency from 100 to 156.25 kHz and keeping other parameters unchanged, $N_{\max\_\text{DCM}} = 2$ from (23). Fig. 14 shows the simulated waveforms for the corresponding signals in a SIDO buck LED driver. The simulated LED current ripple Δi_{LED} is $24\%_{\text{P-P}}$ and the corresponding output voltage ripple Δv_o is $2.3\%_{\text{P-P}}$, both of which satisfy their corresponding maximum ripple requirement. Consequently, both the theoretical and simulation results show that by increasing the switching frequency, a SIDO buck LED driver in DCM is feasible.

A third LED string is added to the SIDO buck LED driver to transform it into SIMO consisting of three independently driven LED strings. The LED current in each string remains unchanged at 80 mA as in the SISO or SIDO case. According to Fig. 11, the theoretical model suggests that for $I_{\text{LED}} = 80$ mA, a *scalable BCM-based SIMO* scheme with a maximum of *three* LED strings is feasible under the $40\%_{\text{P-P}}$ current ripple constraint. The switching period T_s is chosen to be 6 μs using (13) which corresponds to a switching frequency of 166.67 kHz. Fig. 15 shows the simulated waveforms from the resulting SIMO buck LED driver. The simulated LED current ripple Δi_{LED} is around $35\%_{\text{P-P}}$ and the output voltage ripple Δv_o is $3.5\%_{\text{P-P}}$, both of which satisfy their respective maximum ripple constraint. As a sanity check, the theoretical model based on (22) indeed suggests that a maximum possible number of *three* independently driven LED strings can be achieved in the *scalable BCM-based SIMO* scheme. Hence, it is shown that the simulation result agrees with the corresponding theoretical result. On the other hand, it is important to examine the transient performance of the

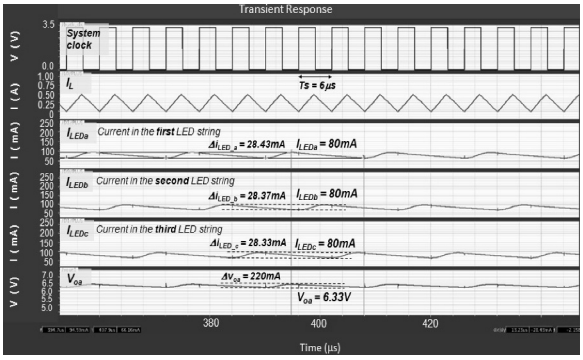
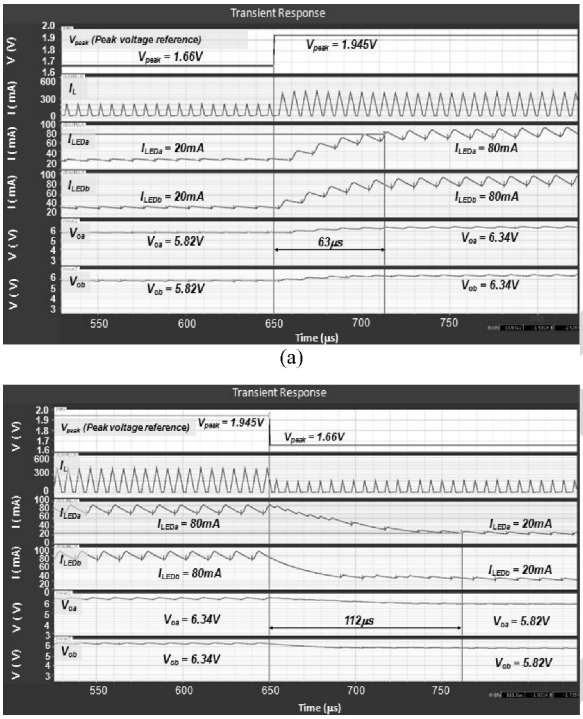


Fig. 15. Simulated steady-state waveforms of a three-string SIMO buck LED driver operating in BCM.



(a)

(b)

Fig. 16. Simulated transient waveforms for (a) peak reference step-up and (b) peak reference step-down response.

proposed SIDO buck LED driver. The LED current is changed by adjusting the peak limit of the inductor current. By stepping up the peak voltage reference ($V_{\rm peak}$ in Fig. 1) from 1.660 to 1.945 V in 400 ns, the peak inductor current limit is increased by approximately 200 mA, leading to an increase in the nominal LED current from 20 to 80 mA. The reference voltages ($V_{{\rm ref}a}, V_{{\rm ref}b}$) are also stepped up from 100 to 340 mV in order to maintain the same load current between the two LED strings. Conversely, by stepping down $V_{\rm peak}$ from 1.945 to 1.660 V, the LED current is reduced from 80 to 20 mA. Fig. 16 shows the simulated transient behavior for the peak voltage reference step-up and step-down response.

In the case of step-up reference response, the LED current in either string settles to the steady-state nominal value of 80 mA within 63 μs. The output voltage reaches its target steady-state value of 6.34 V. In the case of step-down reference response, the LED current in either string settles to the steady-state nominal value of 20 mA in less than 112 μs. The output voltage settles to its new steady-state value of 5.82 V without oscillations. Hence, the simulation results show that the closed-loop system remains in stable condition in response to a peak voltage reference transient.

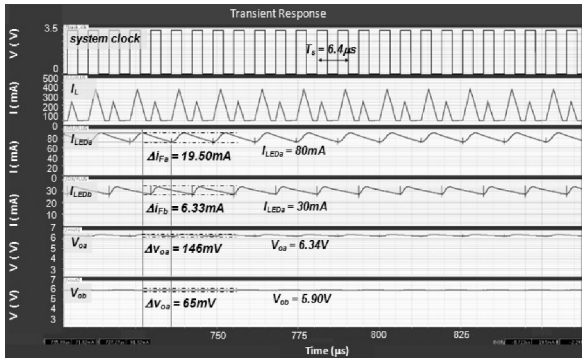


Fig. 17. Simulated steady-state waveforms of a SIDO buck LED driver with unbalanced load.

The effectiveness of the proposed SIDO converter to drive unbalanced load is also investigated. As an example, the first and second LED strings require an average current value of 80 and 30 mA, respectively. Unlike the balanced load case with a constant peak inductor current limit, two distinct peak current limits are employed for unbalanced load such that two different average inductor (or load) current values can be generated in alternate clock cycles. Fig. 17 depicts the simulated steady-state waveforms from the SIDO buck LED driver with unbalanced load. The simulation results show that the first and second LED strings are regulated with an average current value of 80 and 30 mA, respectively. For the first string, the simulated current ripple is 24.38%$_{\rm P\text{-}P}$ and the output voltage ripple is 2.3%$_{\rm P\text{-}P}$. Also, for the second string, the simulated current ripple is 21.1%$_{\rm P\text{-}P}$ and the output voltage ripple is 1.1%$_{\rm P\text{-}P}$. Either string meets the maximum ripple requirements. The simulation results demonstrate that the proposed SIDO converter is capable of delivering unequal currents to the two LED strings simultaneously.

V. Experimental Results

The proposed SIDO buck LED driver was implemented on a field-programmable gate array (FPGA)-based hardware prototype in accordance with the design specification provided in Table I. The switching frequency is increased to 156.25 kHz in order to satisfy the LED current ripple requirement. A photo of the experimental setup is shown in Fig. 18. The power stage of the buck converter consists of discrete ICs from International Rectifier such as power MOSFETs (IRF7828), dual-channel gate driver (IR2110), and output switches (IRF9388), as well as surface-mount inductor and low-ESR capacitors. In actual implementation, the top level of the proposed digital controller is partitioned into two major functional blocks. The functionality of the first block is to control the switching action of the power

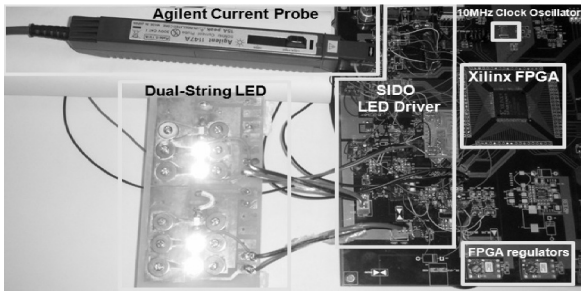


Fig. 18. Experimental setup for the proposed SIDO buck LED driver.

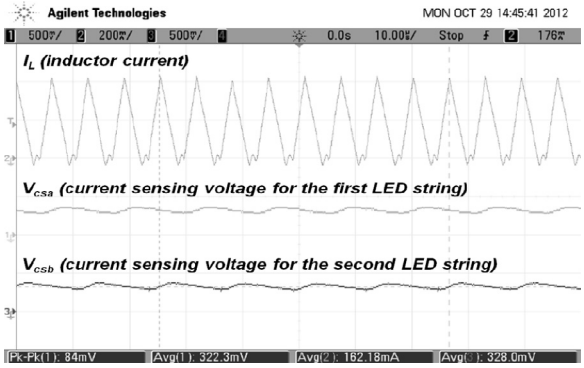


Fig. 19. Measured waveforms for inductor current and current sense feedback voltage.

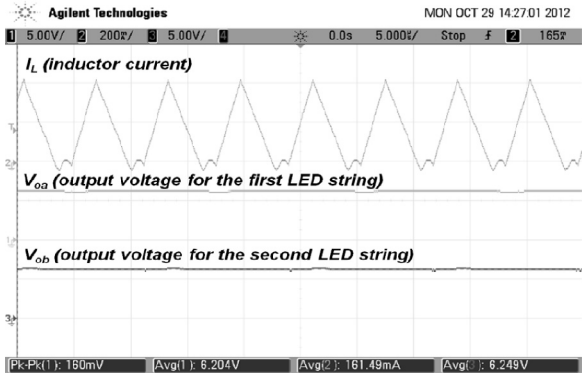


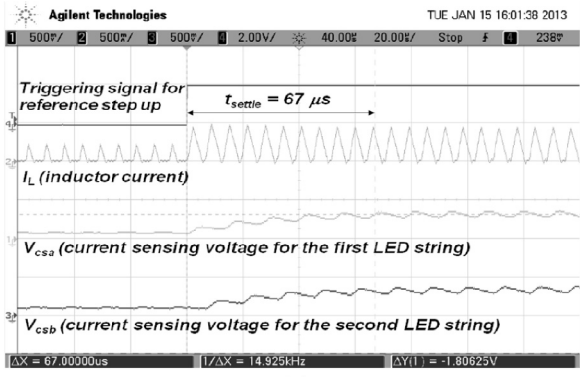
Fig. 20. Measured waveforms for inductor current and output voltage in either LED string.

stage by detecting the peak-crossing and zero-crossing events of the inductor current. It was implemented in hierarchical gate-level schematics using primitives and macros available from the Xilinx Spartan-3 Generation library. Dead-time logic is included to prevent shoot-through current of the power switches. The second logical block is used to control the switching sequence of the two output switches by continuously monitoring the current-sense feedback signals. It was modeled as an FSM in Verilog RTL. Only one of the two output switches can be ON and the other must be OFF per switching cycle. Dead-time logic is also added to prevent cross conduction between outputs. The two logical blocks are synchronized by the system clock to ensure that the high-side power switch and the output switches are triggered from the same clock edge. The entire digital controller was implemented with Xilinx Spartan-3E (XC3S250E) FPGA. The quasi-hysteretic control logic was realized using 4-ns fast comparators (AD8611 from Analog Devices) and semicustom synchronous logic.

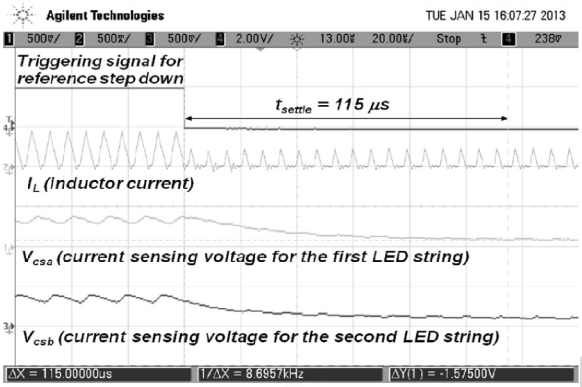
Using a current sensing resistor of 4 Ω and reference voltage of 320 mV, the target current in each of the two LED strings is 80 mA. Fig. 19 shows the current sensing feedback voltage $(V_{\rm csa}, V_{\rm csb})$ from which the corresponding average load current can be obtained, i.e., $I_{\rm LED} = V_{cs}/R_{cs}$. The average inductor current is measured to be 162 mA, which is the sum of the load currents in both LED strings. The average current values in the first and second LED string are measured to be around 80.6 and 82 mA, respectively. The measured LED current ripple $\Delta i_{\rm LED}$ in either string is around $26\%_{\rm P\text{-}P}$, which is reasonably close to the simulated current ripple of $24\%_{\rm P\text{-}P}$. In addition, the nominal output voltages in the first and second string are measured to be 6.204 and 6.249 V, respectively, as shown in Fig. 20. Under this balanced load condition, the measured current and voltage values are in close agreement between the two LED strings. The output voltage ripple is also measured to be around $2.57\%_{\rm P\text{-}P}$, compared to $2.3\%_{\rm P\text{-}P}$ from simulation. Therefore, the experimental results are shown to be consistent with the corresponding simulation ones. On the other hand, the measured power conversion efficiency of the proposed SIDO converter is 80% which is comparable to conventional driving topologies [41]. The efficiency can be further increased by employing a current-sensing resistor with a smaller value.

The transient response of the proposed SIDO buck LED driver is verified experimentally by measuring its peak voltage reference step response. An 8-bit digital-to-analog converter (AD558 from Analog Devices) is used to enable programming of the peak voltage reference $V_{\rm peak}$ and the current-sense voltage references $(V_{{\rm ref}a}, V_{{\rm ref}b})$ by the Xilinx FPGA. The measured waveforms of the inductor current and the voltage at the current sensing nodes in response to a peak voltage reference step are shown in Fig. 21. The settling time of the transient response is also measured and compared with the simulated settling time. For the step-up response, it is observed that the current-sensing voltage $V_{\rm csa}$ in the first LED string steps up from 81.8 to 325.4 mV, which corresponds to an increase in the average load current from 20.5 to 81.3 mA. Similarly, the current-sensing voltage $V_{\rm csb}$ in the second LED string steps up from 94.1 to 327.6 mV, which corresponds to an increase in the average load current from 23.5 to 81.9 mA. The settling time for the step-up response is measured to be 67 μs, compared to 63 μs from simulation. The measured results for the step-down response are the reverse of those from the step-up response. The only difference is that it takes longer for the step-down transient to settle. The settling time for the step-down response is measured to be 115 μs, compared to 112 μs from simulation. The measured settling times are shown to be very close to the simulated ones. The experimental results confirm that the system remains in stable condition when it is perturbed by the peak voltage reference transient.

The unbalanced load scenario in the proposed SIDO buck LED driver is also verified experimentally. The measured average load current values in the first and second LED string are



(a)



(b)

Fig. 21. Measured transient waveforms in response to (a) peak reference step-up and (b) peak reference step-down.

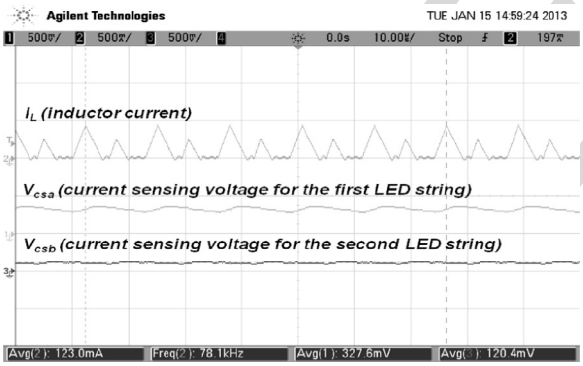


Fig. 22. Measured waveforms for inductor current and current sense voltages.

around 81.9 and 30.1 mA, respectively. Fig. 22 shows the measured waveforms for the inductor current and the current-sensing voltage per string. The inductor current waveform indicates that the proposed driver operates in DCM with *two* distinct peak current limits. Fig. 23 shows the measured inductor current and the output voltage in either string. The measured output voltage values in the first and second LED string are 6.22 and 5.70 V, respectively. The experimental results demonstrate that the proposed driver is capable of driving two independent LED strings concurrently with different load current.

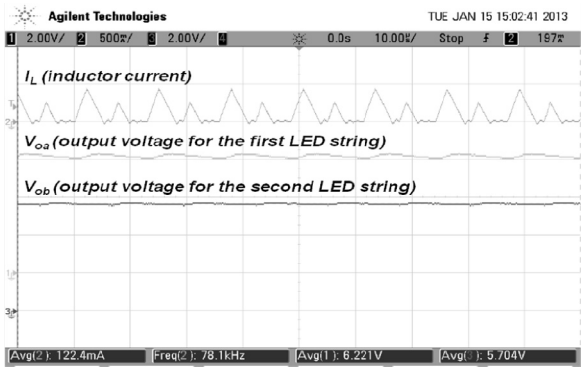


Fig. 23. Measured waveforms for inductor current and output voltages.

VI. Conclusion

The proposed SIDO buck LED driver was implemented in FPGA-based hardware. The experimental results correlate well with simulation ones. The scalability of the proposed SIDO buck LED driver to SIMO is closely examined. A general formula for determining the theoretical maximum achievable number of LED strings in SIMO is derived. The simulation results were shown to be consistent with those obtained from the theoretical model for the same design parameter values. The quasi-hysteretic digital control scheme does not require loop compensation which simplifies the control loop design and reduces component count. In addition, the proposed SIMO architecture offers the advantage of driving a larger number of parallel LED strings without being limited by the maximum current rating of the LED. It also enables dimming for the LED strings without additional dimming transistors. Local bus voltage and current optimization in each individual LED string compensates for the variability of the LED's forward voltage, which reduces power loss and enables mixing of white LEDs from different bins to lower LED costs.

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