# **Overview of Magnetless Brushless Machines**

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*Abstract*—Because of the definite merits of high efficiency and high power density, the permanent-magnet (PM) brushless machines have been dominating the high-performance industrial applications. However, the problems of high PM material cost, fluctuating supply of rare-earth materials and ineffective PM flux control have hindered the widespread applications of the PM brushless machines. In recent years, many attentions have been shifted to the magnetless candidates, while the focuses are mainly placed on the classical candidates. In this paper, an overview of magnetless brushless machines, including both the classical and advanced types, is presented, with emphasis on their machine topologies, features and performances. In addition, the upcoming trend of these machines is reviewed and discussed.

*Index Terms*—Brushless, doubly-salient, electric vehicle, flux-reversal, flux-switching, flywheel, magnetless, mass transit transportation, overview, reluctance, robotic, ship propulsion, wind power generation.

### I. INTRODUCTION

Due to a large variety of industrial applications, including the electric vehicles, wind power generations, ship propulsion systems, and robotic applications, the development of electric machines has become a hot research topic in last century. The electric machines can be generally categorized as two major groups, namely the brushed machines, and the brushless machines. As compared with the brushed ones, the brushless machines can enjoy the absolute advantage of maintenance-free operation, so that these type of machines have become the major trend since the last few decades [1], [2]. By the classification of machine materials, the brushless machines can be further divided into two subgroups, namely the permanent-magnet (PM) brushless machines, and the magnetless brushless machines.

Upon the installation of high-energy-density PM materials, the PM brushless machines can provide superior performances and hence they have become very attractive for high-performance applications [3]. However, due to the fluctuating supply of rareearth materials, there is a drastic increase of PM material costs [4]. To improve the product competitiveness and market penetration, the magnetless brushless machines are becoming more attractive, especially for the automotive electric drives [5]. Nevertheless, the research interests are mainly focused on the classical candidates, while the discussions on the advanced machine types are still inadequate. In particular, a comprehensive overview and discussion on the magnetless brushless machine family, especially on the advanced candidates, is still absent in literature.

The purpose of this paper is to provide an overview of the magnetless brushless machines, including both the classical and advanced candidates. Current technologies of various magnetless brushless machines, including the machine structures, characteristics, operation principles, control algorithms, and upcoming trends, will be critically reviewed and discussed.

# II. CLASSICAL TOPOLOGIES

In general, there are four major types of fundamental magnetless brushless machines available, namely the squirrel-cage induction machine (IM) [6], the synchronous reluctance machine (SynRM) [7], the vernier reluctance machine (VRM) [8] and the switched reluctance machine (SRM) [9]. Even though all these candidates are categorized as the magnetless brushless machines, each of them exhibits the unique features and distinctive characteristics.

### A. Induction Machine

The IM has been regarded as one of the most developed electric machines [10]. Literally speaking, the IM is operated based on the principle of electromagnetic induction, which can be achieved by the rotating magnetic field. The induction brushless machine with the squirrel-cage structure [11] is a magnetless brushless machine. The basic performances of the IM can be accurately estimated by the equation modeling [12]. The IM has been employed in many variable-speed situations, such as wind power generation, while the doubly-fed IM has been widely accepted as one of the best options for these applications [13]. To further improve the torque density, the dual-electrical-port control scheme has been recently implemented to the cascaded doubly-fed IM [14].

Even though the three-phase topology is the most common design, the IM with higher number of phases have also drawn some attentions for various applications [15]. In particular, the nine-phase IM with the dual-inverter-fed topology has been proposed [16]. Apart from the design of machine structure, the control algorithm is another attractive technology that has drawn considerable attentions [17]. In particular, a huge variety of sensorless control schemes have been employed in the industrial applications [18]. However, the sensorless vector control cannot estimate the rotor frequency in the ultra-low speed region. To cater this situation, a mechanical simulator that estimates the disturbance torque by the error of the torque current has been developed [19].

# B. Synchronous Reluctance Machine

As one of the earliest types of electric machines, the SynRM has been developed as a cylindrical rotor with multiple slits in early 1900s [7]. The SynRM is operated based on the principle of minimum reluctance, which can be achieved by the rotating

magnetic field. The major torque component of the SynRM comes from the reluctance torque, which is directly proportional to the saliency ratio. To improve the saliency ratio as well as the output torque performance, a segmental rotor structure [20] and an axially laminated rotor structure [21] have been developed. The rotor design is crucial for the SynRM, while the multi-objective genetic algorithm with the Pareto front solutions has been employed for rotor optimization [22].

Apart from the average torque value, the torque ripple issue is another important criterion to determine the machine performance. To minimize the torque pulsation, the asymmetrical rotor barrier arrangement [23] and the torque harmonic compensation approach [24] have been proposed. With the advantages of high reliability and low maintenance, the doubly-fed SynRM has shed great potential for variable-speed applications [25].

# C. Vernier Reluctance Machine

Same as the SynRM, the VRM is also operated based on the principle of minimum reluctance. Yet, the VRM distinguishes itself by the salient rotor pole structure [26]. In the meantime, the VRM is operated based on the rotating field scheme [27], whose operation is similar as the SynRM one.

Based on the rotating field operation with the salient pole structure, the relatively smoother torque can be produced even in the low-speed situation. To utilizing these characteristics, the VRM is purposely designed with the machine structure of relatively higher number of poles, and hence the high-torque low-speed operation can be achieved [28]. The VRM has been extended to form the double-stator VRM (DS-VRM) [29] and the double-rotor VRM (DR-VRM) [30]. Yet, same as other reluctance machines, the VRM also suffers from the problem of relatively lower power factor. To improve the power factor, the VRM with the doubly-slotted stator structure has been developed [31]. As the extension from the doubly-slotted structure, the VRM with the fractional slot concentrated winding arrangement has been developed [32].

### D. Switched Reluctance Machine

Same as the VRM, the SRM consists of the salient pole structure and this type of machine is also operated based on the principle of minimum reluctance. Yet, unlike the SynRM and VRM that are operated by the rotating field, the SRM is instead operated by the phase current pulse scheme. The simplest SRM consists of the one-phase 2/2-pole (two-stator-pole/two-rotor-pole) topology [33], while it is not practical for industrial applications. The SRM has been further developed as the three-phase 6/4-pole structure [34], the three-phase 12/8-pole structure [35], the three-phase 24/16-pole structure [36] and the four-phase 8/6-pole structure [33]. It has been reported that the torque density can be improved based on the machine dimension optimization, the selection of pole-pair combinations and the choice of materials [37]. Recently, the new topology with higher ratio of rotor to stator pole has also been explored [38]. With the new rotor to stator pole arrangement, more winding slot area as well as larger torque density can be achieved.

To improve the performance of the SRM, the reduction of torque ripple and acoustic noise have become a hot research topic in the past few decades. The torque pulsations as well as the acoustic noise are generally produced at the point of phase commutation [39]. Hence, these problems can be relieved by the optimization of machine dimension [40] and the optimized control of the commutation angle [41]. In particular, the SRM with the cylindrical rotor design has been proposed to reduce the windage loss and acoustic noise, such that it can enjoy better efficiency at high operating speed [42]. In addition, to optimize the current waveforms, the implementation of phase shift to the second and third harmonics has been introduced [43].

In order to produce the torque properly, the phase current pulse of the SRM conventionally has to synchronize with its rotor position. However, the position sensors not only increase the construction cost and system complexity, but also decrease the reliability of the system [44]. Upon the analysis of the variation of the flux-linkages among the phases, the sensorless control algorithm can be accomplished [45]. Recently, the utilization of the mutual inductance between the two excited phases has been realized for position sensorless control [46].

	IM	SynRM	VRM	SRM
Operating principle	Induction	Reluctance	Reluctance	Reluctance
Rotor structure	Squirrel-cage	Axially laminated	Salient pole	Salient pole
Control scheme	Rotating field	Rotating field	Rotating field	Switching pulse
Efficiency	High	Medium	Medium	Low
Torque range	Low	Medium	High	Low
Speed range	High	Medium	Low	High

TABLE I COMPARISONS OF THE CLASSICAL MAGNETLESS MACHINES

### E. Comparison and Summary

The qualitative comparisons between the four classical magnetless brushless machines are given in Table I, while the quantitative comparisons can be found on the other literatures [37, 47 and 48]. The comparisons are based on the key features, including the operating principle, rotor structure, control scheme, efficiency, torque range, and speed range.

# **III. RECENT TOPOLOGIES**

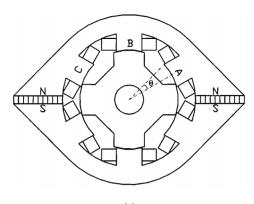
Apart from the aforementioned accomplishments, new developments of other magnetless topologies have received well attentions recently.

With reference to the design philosophies from the profound PM machines (PMMs), the advanced magnetless machines can then be produced. Not surprisingly, the derived magnetless machine can share the similar characteristics as well as advantages from its ancestors.

### 1) Doubly-Salient DC Machine

Sharing the same design philosophy with the doubly-salient PM machine (DSPMM) [49], as shown in Fig. 1(a) [50], the magnetless DSDCM can also incorporate the benefits from both the SRM and the PMM. Same as the DSPMM, the DSDCM also exhibits the unipolar flux-linkage characteristics. Moreover, the DSDCM can utilize its independent dc-field excitation for flux-regulation. As a result, its overall efficiency can be improved under different situations, namely at different loads and different operating speed ranges [51].

Apart from the conventional three-phase 6/4-pole topology, other slot/pole combinations, such as three-phase 12/8-pole, as shown in Fig. 1(b) [52], three-phase 24/32-pole [53], five-phase 10/8-pole topologies [54] and five-phase 30/24-pole topologies [55] have also been developed. All the developed machines exhibit different characteristics, in terms of power densities, torque densities, operating ranges, for various applications. The machine dimension optimizations based on the sizing equation and non-linear varying-network magnetic circuit method have been reported [56]. Apart from the profound symmetric stator/rotor pole combination, the asymmetric stator/rotor pole machines have also been proposed [57]. Based on the newly suggested arrangement, the DSDCM with odd-number rotor-pole structure are developed. Hence, higher design flexibility can be provided accordingly.



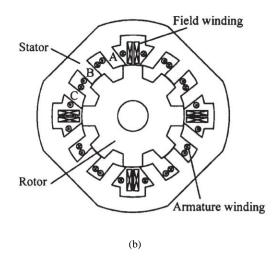
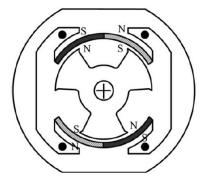


Fig. 1 Doubly-salient machines. (a) Three-phase 6/4-pole DSPMM [50]. (b) Three-phase 12/8-pole DSDCM [52].

# 2) Flux-Reversal DC Machine

Exhibiting the bipolar flux-linkage patterns, the flux-reversal PMM (FRPMM) can potentially provide higher power density than the unipolar candidate does, i.e., the DSPMM. Unlike the DSPMM that inserts the PM pieces within the stator yoke, the FRPMM instead mounts the PM pieces with alternating polarities on its stator tooth [58], as shown in Fig. 2(a). Undoubtedly, the magnetless version of the FRPMM can be established, while some special arrangement on the stator pole should be implemented.

To imitate the FRPMM structure, the stator poles of the magnetless FRDCM are purposely modulated as a three-tooth per stator pole topology [59], as shown in Fig. 2(b). With the modulated stator pole, the dc-field winding can be wound in a way to imitate the PM pieces with the alternating polarities. Based on the magnetless structure, the FRDCM enjoys the definite costbenefit as compared with the PM counterparts. However, high saturation effect occurs within the modulated tooth easily, such that further improvement of the power density may be hindered.



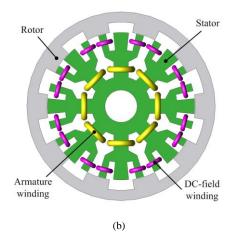


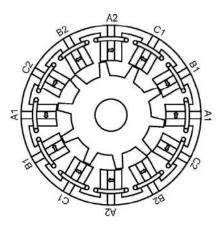
Fig. 2 Flux-reversal machines. (a) The outer-stator inner-rotor FRPMM [58]. (b) The outer-rotor inner-stator FRDCM [59].

# 3) Flux-Switching DC Machine

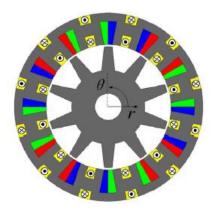
Same as the flux-switching PMM (FSPMM), as shown in Fig. 3(a), that has drawn most of the attentions among its competitive group [60], its derived magnetless candidate, namely the FSDCM has also become very popular recently. Inheriting the characteristics from its ancestor, the FSDCM exhibits the bipolar flux-linkage patterns. As a result, higher power density can be potentially produced [61].

To achieve the bipolar flux-linkage patterns, there are generally two fundamental dc-field winding arrangements available, namely the toroidal-field winding arrangement [62] and the wound-field winding arrangement [63], as shown in Fig. 3(b) and Fig. 3(c), respectively. Unlike the FRDCM that modulates the fluxes within the stator tooth, the FSDCM instead regulates the fluxes within the stator yoke. Consequently, better core utilization and lower saturation effect can be potentially resulted. Even though the toroidal-field winding machine can potentially produce higher torque density, it suffers from more severe saturation problem within its stator iron yoke. On the other hand, the magnetic field of the would-field winding machine is radially excited and not concentrated, so that the saturation problem can be relieved. To achieve the maximum output torque, the relationship between the armature and the field currents has also been carried out [64].

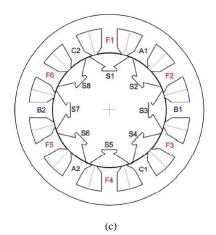
With the attempt to further utilize the inner space of the FSDCM, the DR-FSDCM has been proposed [65], as shown in Fig. 3(d). Based on the toroidal-field winding arrangement, the armature and dc-field windings can provide the symmetrical fluxes towards the two rotors. Hence, very simple and robust structure is resulted.

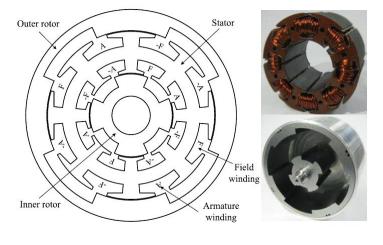


(a)



(b)





(d)

Fig. 3 Flux-switching machines. (a) Three-phase FSPMM [60]. (b) FSDCM with toroidal-field winding arrangement [62]. (c) FSDCM with wound-field winding arrangement [63]. (d) DR-FSDCM with toroidal-field winding arrangement [65].

### 4) Operating Principles

With respect to the back electromotive force (EMF) waveforms, the advanced magnetless machines can be further classified into two major groups, namely the sinusoidal-like machine and the trapezoidal-like machine [66]. In order to operate these machines properly, two conduction schemes are available, namely the brushless ac (BLAC) scheme and the brushless dc (BLDC) scheme. In particular, the BLAC scheme is more suitable for the sinusoidal-like machine while the BLDC scheme is for the trapezoidal-like machine.

In the BLAC scheme, the sinusoidal armature current  $I_{BLAC}$  is employed in accordance to the status of the flux-linkage  $\Psi_{BLAC}$ , such that the positive electromagnetic torque  $T_{BLAC}$  is produced. This BLAC operating scheme is shown in Fig. 4(a). Since the injected armature current in the BLAC scheme is perfectly aligned with the back EMF waveform, the minimized torque pulsation performance can be achieved.

In the BLDC scheme, when the flux-linkage  $\Psi_{BLDC}$  is increasing, a positive rectangular current  $I_{BLDC}$  is employed. As a result, the positive electromagnetic torque  $T_{BLDC}$  is produced. Meanwhile, when the flux-linkage is decreasing, a negative rectangular current is instead employed to produce also the positive electromagnetic torque. This BLAC operating scheme is shown in Fig. 4(b). With respect to the interaction between the back EMF and the armature current pattern, the trapezoidal-like machine with the BLDC scheme can potentially produce higher output power and torque levels.

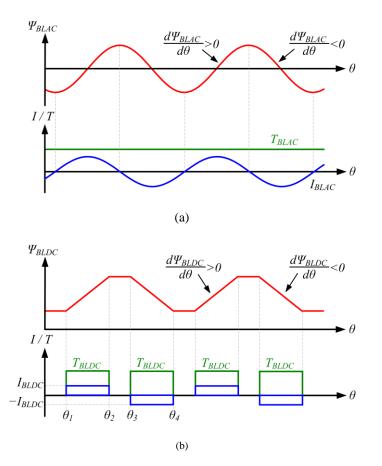


Fig. 4 Operating schemes [66]. (a) BLAC conduction scheme. (b) BLDC conduction scheme.

# 5) Machine Performance Analysis

To analyze the electromagnetic performances of the electric machines, various analytical theories, such as the winding function theory [67], the unified theory of torque production [68], the rotating magnetic field theory [69], the cross-field theory [70] and the two-reaction theory [71], are available. However, the traditional analytical theories are inadequate for the advanced electric machines. To cater these situations, a general airgap field modulation theory, which analogizes the electric machine with the switching converter, has been developed [72]. In this paper, other than using the analytical theories, a commercial finite-element method software package, the JMAG-Designer is employed for machine performance analysis.

The three advanced magnetless machines and the PM counterpart [73] are designed and quantitatively compared in Table II. In particular, the key design data, namely the outside stator diameter, the inside rotor diameter, the airgap length and the stack length are set equal. To offer a more comprehensive analysis, the qualitative comparisons between the three derived magnetless machines and the corresponding PM counterparts [74] are given in Table III. The comparisons are based on the key features, including the phase flux, efficiency, power density, flux controllability, operating range and cost-effectiveness.

As shown, the PM candidate enjoys the highest power and torque densities within the comparing group. Yet, the magnetless brushless machines can somehow provide better cost-effectiveness than the PM counterpart. In particular, the FSDCM can

achieve the highest efficiency, power density and cost-effectiveness among the magnetless candidates, such that more research endeavors should be made on this machine type.

	РММ	DSDCM	FRDCM	FSDCM
Outside stator diameter	269 mm	269 mm	269 mm	269 mm
Inside rotor diameter	110 mm	110 mm	110 mm	110 mm
Airgap length	0.7 mm	0.7 mm	0.7 mm	0.7 mm
Stack length	84 mm	84 mm	84 mm	84 mm
Efficiency	89 %	85 %	85 %	86 %
Power	43 kW	18 kW	20 kW	24 kW
Output torque	345 Nm	147 Nm	161 Nm	194 Nm
Total mass	32.8 kg	34.1 kg	34.7 kg	33.4 kg
Material cost	218 USD	84 USD	83 USD	82 USD
Power density	1310 W/kg	530 W/kg	580 W/kg	720 W/kg
Torque density	10.5 Nm/kg	4.3 Nm/kg	4.6 Nm/kg	5.8 Nm/kg
Power / cost	200 W/USD	210 W/USD	240 W/USD	290 W/USD
Torque / cost	1.6 Nm/USD	1.8 Nm/USD	1.9 Nm/USD	2.4 Nm/USD

#### TABLE II DESIGN EXAMPLES OF THE ADVANCED MACHINES

### TABLE III COMPARISONS OF THE ADVANCED MACHINES

	РММ	DSDCM	FRDCM	FSDCM
Phase flux	Unipolar / Bipolar	Unipolar	Bipolar	Bipolar
Efficiency	High	Medium	Medium	Medium
Power density	Very high	Medium	Medium	High
Flux controllability	Low	Medium	High	High
Operating range	Narrow	Wide	Very wide	Very wide
Cost-effectiveness	Low	Medium	High	Very high

# B. Technologies to Improve the Machine Performances

Without the installation of the high-energy-density PM materials, the magnetless machines suffer from the definite disadvantage from poor power and torque performances than the PM counterparts. In order to improve the market competitiveness of the magnetless machines, the technologies that improve the machine performances have been suggested.

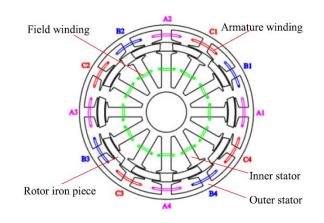
### 1) Multi-Tooth Structure

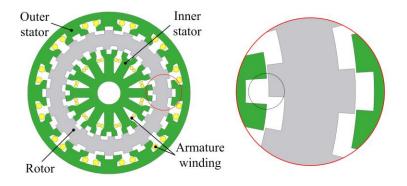
To improve the torque density, the multi-tooth (MT) structure, which employs the multiple tooth per stator pole arrangement, has been proposed [75]. Upon the MT topology, the magnetic flux within the stator yoke can be regulated in a way to transfer the energy to the rotor simultaneously. Consequently, the torque density can be potentially improved. In particular, the MT machine is favorable for the high-torque low-speed operation [76]. In order word, when larger number of tooth per stator pole is employed, higher torque density with lower operating range can then be achieved. However, the maximum number of the multiple tooth is limited by the physical constrain and the saturation within the tooth. Detailed analysis and comparisons between the MT structure and the conventional structure can be found in [77].

# 2) Double-Stator Structure

To improve the power density, the inner space of the single-stator machine has been utilized to serve as an additional stator. As a result, the double-stator (DS) machines, which consist of two separated stators, is formed. Unlike the typical DS machine, which accommodates both armature and dc-field windings in the same winding slots, the partitioned-stator machine instead allocates the two winding sets into two stators separately [78], as shown in Fig. 5(a). Consequently, the partitioned-stator machine can relieve the saturation problem that happens in the conventional DS machines. Hence, better efficiency can be potentially achieved.

Because the inner- and outer-rotor tooth of the DS machine are typically aligned with each other, the torque ripples of the two torque components are unfavorably superimposed. To improve the torque ripple problem, the mechanical-offset (MO) structure, whose inner- and outer-rotor tooth are purposely mismatched with a conjugated angle to each other, as shown in Fig. 5(b), is proposed [79]. As a result, the torque ripples from the inner-segment and outer-segment can be perfectly integrated, as shown in Fig. 5(c). Consequently, a smoother resultant torque can be produced. However, same as other DS machines, the MO structure suffers from the complex manufacturing processes.





(b)

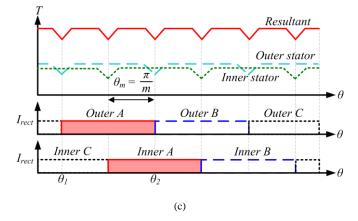


Fig. 5 Double-stator machines. (a) Partitioned-stator machine [78]. (b) MO machine [79]. (c) Operating waveforms for MO machine [79].

# 3) Axial-Field Structure

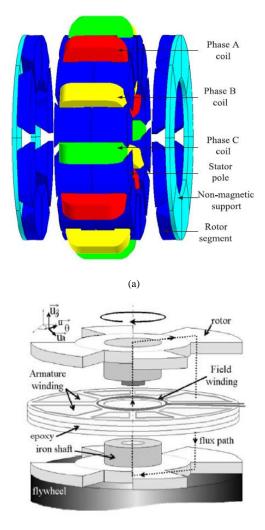
Despite the traditional radial-field (RF) structure, the magnetless machines can be extended to form the axial-field (AF) family [80]. Upon the employment of the radial area for the torque production, the AF machines can produce higher power and torque densities as compared with its RF counterparts do [81]. Since the AF machines are derived from the RF topologies, theoretically every RF machine should be able to form its corresponding AF derivation. As one of the most mature machine type, the AF-IM has been developed [82]. According to the theoretical and experimental results, the AF-IM can provide better performances, including higher efficiency and higher starting torque, than the RF counterparts do.

Same as the IM, another traditional magnetless machine, the SRM has been further extended to form the AF-SRM. The developed AF-SRM consists of the sandwiched-stator double-sided-rotor structure with the toroidal winding arrangement [83], as shown in Fig. 6(a). In particular, the AF-SRM with higher number of rotor pole is more preferable for the high-torque low-speed applications, such as the electric vehicle or electric ship propulsion.

With the definite advantage of relatively higher torque density, the AF-DSDCM with the sandwiched-stator double-sided-rotor structure has been proposed [84]. With the modular stator construction, the derived AF-DSDCM can reduce its stator yoke to improve the torque density and to minimize the material costs.

To reduce the iron losses within the yoke, the double-face printed circuit technology for the multilayer winding arrangement, has been implemented into the AF machine [85], as shown in Fig. 6(b). The torque of the double-face-printed machine is produced by the interaction between the homopolar flux and the rotating axial flux created by the dc-field and three-phase armature winding, respectively. The double-face-printed machine employs the solid steel discs as the rotor part, and therefore high robustness can be achieved for the flywheel application.

Even though the AF topology enjoys some superior advantages, as compared with the well-developed RF counterpart, this type of machine suffers from the immature technology and manufacturing complexity.



(b)

Fig. 6 Axial-field machines. (a) Sandwiched-stator double-sided-rotor AF-SRM [83]. (b) Double-face-printed AF machine [85].

The power density achieved by the copper field winding is relatively lower than that from the PM materials. To improve the situation, the high-temperature superconducting (HTS) materials have been implemented to the existing machine structures. There are two typical HTS implementations available, namely the HTS-field winding implementation [86] and the HTS-bulk implementation [87].

With the advantages of high current density and thus high power density, the HTS-field winding implementation is suitable for the machine that consists of limited winding slot area. In particular, this implementation has been employed to form the FS-HTSM [88]. To verify the concept, a cryogenic cooling system for FS-HTSM with stationary seal has been developed [89].

Instead of improving the power density directly, the HTS-bulk can be used to serve as the flux regulator to minimize the flux leakage problem. With the reduction of the flux leakage, the machine with the HTS-bulk can therefore achieve higher power density. There is no conflict between the two HTS implementations, and hence the hybrid HTS machine that incorporates the two implementations can be developed [90]. Despite the outstanding performances, the special cryogenic system is needed to keep the HTS materials within the functional temperature range.

The comparisons among the four upcoming technologies for performance improvement are given in Table IV.

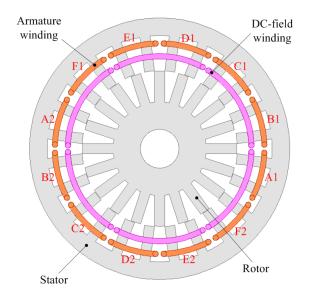
	МТ	DS	AF	HTS
Improved area	Torque density	Power density and torque	Power and torque density	Power density
		ripple		
Major constrain	Not suitable for high speed	Complex manufacturing	Immature technology	Cryogenic issue
	operation	process		
Developing rate	Medium	High	High	Low

TABLE IV COMPARISONS OF THE PERFORMANCE IMPROVING TECHNOLOGIES

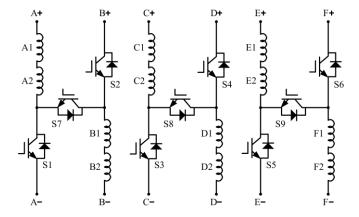
# C. Dual-Mode Machine

The electric machines can be roughly classified into two major categories, namely the high-torque low-speed machine and the low-torque high-speed machine. Two design philosophies, namely the MT high-torque low-speed machine and the single-tooth (ST) low-torque high-speed machine, have been purposely incorporated together to form a new set of design equations for the dual-mode machine [91], as shown in Fig. 7(a). With the support of the control circuit, as shown in Fig. 7(b), the dual-mode machine can reconfigure its winding arrangement to achieve the dual-mode operation.

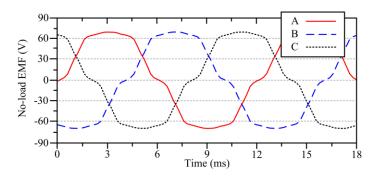
The design criteria of the back EMF have been carefully studied, such that better torque performances can be provided for various applications [66]. Upon the adoption of different winding configuration with the appropriate power electronic relay, the dual-mode machine can exhibit two operating modes, namely the MT mode and the ST mode, as shown in Fig. 7(c) and Fig. 7(d), respectively.











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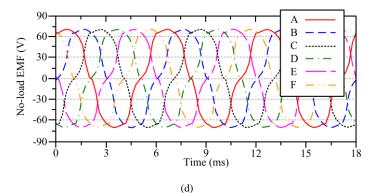
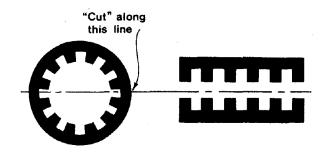


Fig. 7 Dual-mode machines. (a) Machine structure [91]. (b) Control circuit [91]. (c) Back EMF waveforms at MT mode with low operating speed [66]. (d) Back EMF waveforms at ST mode with high operating speed [66].

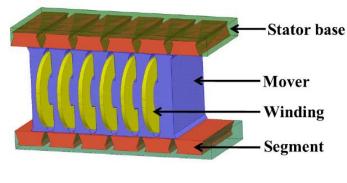
# D. Linear Topology

Due to the widespread of applications, the rotatory machines have attracted most of the attentions in the past few decades. Yet, upon the enhancing development on the mass transit technology, there are increasing needs on the research of the linear machines. The basic structure of the linear machine can be regarded as the extension from the rotatory counterparts [92], as shown in Fig. 8(a).

Same as the AF machine, the linear machines can be derived from its corresponding rotatory ancestors. As one of the most mature candidates, the rotatory SRM has been developed as the linear SRM (L-SRM) [93]. The design considerations of the mover, as the analogue of the rotor in the rotatory machine, are well studied. To improve the force density, the dual-side mover L-SRM with the segmental stator topology has been developed [94], as shown in Fig. 8(b). In addition to the L-SRM, there are also researches on the L-IM [95], L-FSDCM [96] and L-FRDCM [97]. Since the PM installations for the long-stator is very expensive, the magnetless linear machine has been regarded as the very promising structure for the railway transportation system.



(a)



(b)

Fig. 8 Linear machines. (a) Analogue between rotatory and linear machines [92]. (b) Dual-side L-SRM with the segmental stator topology [94].

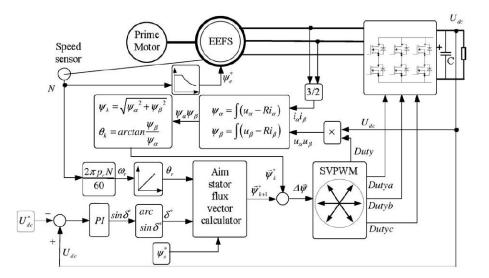


Fig. 9 Improved DTC scheme with the SVPWM [98].

# E. Advanced Control Algorithm

As one of the most conventional control scheme, the direct torque control (DTC) has been widely employed for the BLAC operating machines, while the traditional approach suffers from low estimation accuracy and system complexity. To improve the situation, the integration among the fifth-order filter, the high-pass filter and the logical calculation has been proposed [98]. Upon the adoption of the developed algorithm, better estimation capability and improved system quality can be achieved.

In the meantime, the relationship between the independent dc-field excitation of the DSDCM and the system quality has been analyzed. Consequently, the space vector pulse width modulation (SVPWM) has been implemented with the existing DTC scheme. By utilizing the linear co-relation between the electromagnetic torque and the sine value of torque angle, the improved control scheme is formed [99], as shown in Fig. 9. As a result, the torque loop can be eliminated while the output torque can be

regulated linearly by the voltage loop. Based on the improved DTC scheme, smaller torque pulsation and lower current total harmonic distortion (THD) are resulted.

### IV. CONCLUSION

The backgrounds, modern developments and upcoming technologies of the magnetless brushless machines have been reviewed, with the clear descriptions on the operating principles, machine structures and control algorithms. The characteristics of the magnetless machines are discussed, with the highlights of the corresponding unique features. Upon the definite advantages of cost-effectiveness and flux regulation capability, the advanced magnetless machines have shown the great potential in some industry applications, such as electric vehicles, wind power generations, ship propulsion systems, and mass transit applications. The future work of this machine type should be the new machine designs with improved power density, reduced torque pulsation, greater operating flexibility and advanced control strategy.

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