IMPURITY INDUCED DISORDERING PRODUCED LATERAL OPTICAL CONFINEMENT IN AlGaAs AND InGaAs (ON GaAs) QUANTUM WELL WAVEGUIDES

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Abstract—Impurity induced disordering technique is employed to an AlGaAs/GaAs quantum well optical waveguide to provide lateral optical confinement. The modal propagation constant and field profile are analysed using an improved Fourier decomposition method. Single mode operating region are given in terms of thickness of quantum well layers.
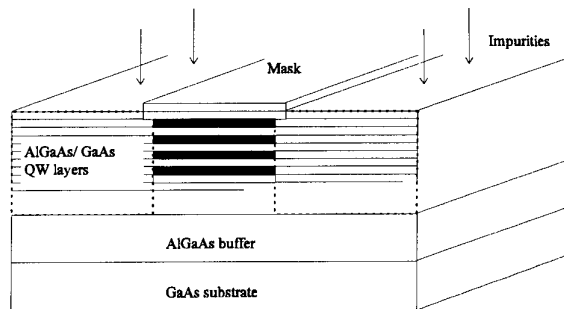
Fig. 1. The schematic of cross section of IID QW waveguide

I. INTRODUCTION

The control modification of the rate of Al/Ga interdiffusion, such as by the introduction of impurities on masked pattern, interdiffusion across $Al_wGa_{1-w}As$/GaAs quantum well (QW) interface is a process of considerable interest for the fabrication of optoelectronic device [1]. This impurity induced disordering (IID) technique provides an efficient way to realize two dimensional (2-D) waveguiding structure in optoelectronic integrated circuits. The electronic and optical properties of the interdiffusion modified AlGaAs/GaAs QW strucures, such as the band strucutre and refractive index have been studied [2], [3]. A 2-D waveguide structure fabricated by using the IID technique has been studied theoretically and a simple model is used to describe the interdiffusion profile and band-gap shifts [4], however, the modal properties of waveguides have not been considered. In this paper, a detailed model of the 2-D waveguide structure fabricated using such technique is presented. In the next section, an outline is given in the implementation of a 2-D waveguide using the IID technique. In Section III, a numerical method is employed to solve the wave equation. Solution of the equation are modal propagation constant and field amplitude. Results are presented in Section IV. Finally, the requirement for single mode operation is presented.

II. IMPLEMENTATION

The structure to be modeled consists of layers of GaAs QW on a thick $Al_{0.3}Ga_{0.7}As$ buffer layer. The schematic of the structure is show in Fig. 1. The implantation process produces a modification of the QW material which in turn leads to differences in refractive index in different region [5]. The implanted region has lower refractive index than the non-implanted region, hence produce lateral confinement for light and a 2-D waveguide is formed. The refractive index of the waveguiding strucutre fabricated by such technique is inhomogeneous.

The steps involved in the implementation of IID QW waveguide is illustrated in Fig. 2. To find out the refractive index profile of QW layers, we computed the impurity density as implanted for a 2-D (x-y axes) structure, where x is defined as the lateral direction of the waveguide and the depth y is perpendicular to it. The concentration of the implanted impurity is described by an equation base on the experimental and simulation results [6], such as the one shown as follows:

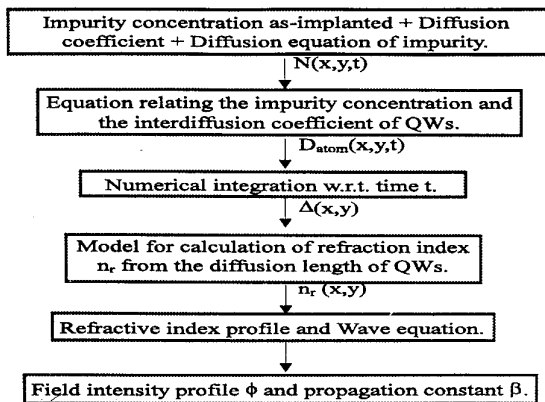$$N(x,y) = \frac{N_o}{\sqrt{2\pi}\Delta R_p} \exp\left[-\frac{(y - R_p)^2}{2\Delta R_p^2}\right] \quad (1)$$

Fig. 2. Flow chart to describe steps for implementation.

$$\times \frac{1}{2} \left[\mathrm{erfc} \left(\frac{x-a}{\sqrt{2\Delta R_{pL}}} \right) \right.$$
$$\left. - \mathrm{erfc} \left(\frac{x+a}{\sqrt{2\Delta R_{pL}}} \right) \right]$$

where N_o is the implanted dose, $2a$ is the mask width, ΔR_p is the standard derivation of the projected range R_p, and ΔR_{pL} is the lateral spread.

When the sample was heated, diffusion of Al/Ga and the defect occurs simultaneously. Their motion is described by a classical diffusion law. For short times we shall assume that the diffusion of the impurity is independent of the motion of Al/Ga atoms and the diffusion coefficients D_{ion} is a constant through out the sample for any time t. The diffusion equation for the impurities is

$$\frac{\partial N(x,y,t)}{\partial t} = D_{\mathrm{ion}} \nabla^2 N(x,y,t), \qquad (2)$$

where $N(x,y,t)$ is the impurity concentration profile.

We shall also assume the interdiffusion coefficient, D_{atom}, depends on the local defect density only which is described by the equation, $D_{\mathrm{atom}}(x,t) = \alpha D_{\mathrm{ion}} N(x,y,t)$, where α is a numerical factor determined from experimental data. The diffusion equation for the Al/Ga atoms is

$$\frac{\partial C(x,y,t)}{\partial t} = \nabla \cdot [D_{\mathrm{atom}}(x,y,t)\nabla C(x,y,t)], \qquad (3)$$

where $C(x,y,t)$ is the Al/Ga atom concentration.

Once we have obtain the Al/Ga concentration profile, the position dependent diffusion length of the Al/Ga atoms at any time can be obtained. Using a previously developed model [7], a 2-D refractive index profile $n_r(x,y)$ was then calculated from these diffusion lengths, as shown in Fig. 3.
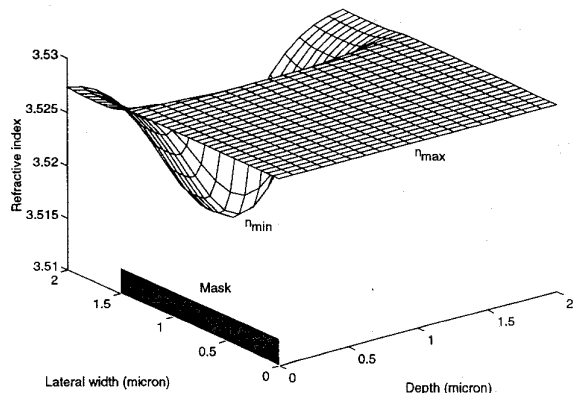

Fig. 3. A typical refractive index profile (half symmetry) of a waveguide structure with 20 multi-QW layers, mask width of 1.5μm and operating wavelength at 0.9μm.

III. WAVE EQUATION

Consider a translationally invariant, real refractive index profile, $n_r(x,y)$, which only changes slightly across the QW layers as shown in Fig. 3. The maximum refractive index of the QW layers $n_{\max}$ is similar to the minimum refractive index of the QW layers $n_{\min}$, and weak-guidance approximation is applicable. Within this approximation, all polarization properties of the waveguide are neglected and Maxwell's equations reduce to the scalar wave equation:

$$\left[\frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + k^2 n_r^2(x,y) - \beta^2 \right] \Psi(x,y) = 0 \qquad (4)$$

Here, $\Psi(x,y)$ denotes the transverse modal electric field, $k = 2\pi/\lambda$, where λ represents the free-space wavelength and β is the associated propagation constant. It should be noted that there are no exact analytical solutions of Eq. (4) for the QW waveguide illustrated in Fig. 3. To this end, an improved Fourier decomposition method (FDM), based on the mapping of the whole $x-y$ plane onto a unit square in $u-v$ space was adopted to solve the scalar wave equation [8].

For the below calculations, 30 harmonics (in each direction) in the Fourier series are used to expand the mode field in a mapped space (resulting in a matrix equation of size 900 × 900).

IV. MODAL PROPERTIES

For a given refractive index profile, $n_r(x,y)$, the normalised propagation constant P^2 is calculated, where $P^2 = [(\beta/k) - n_{\min}^2]/(n_{\max}^2 - n_{\min}^2)$. Fig. 4 shows the normalised propagation constants as a function of QW layers thickness, t_{QW}. The guided mode of the wave-
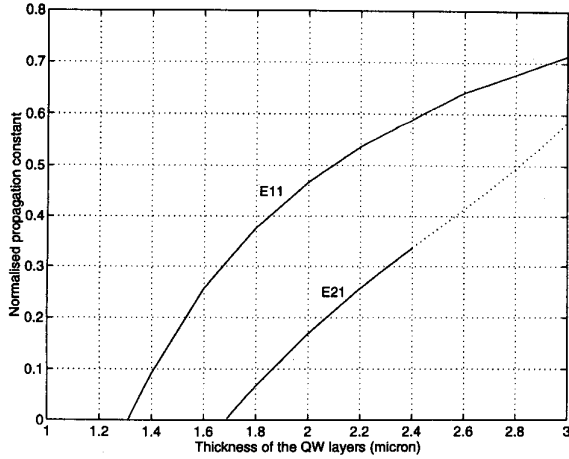
Fig. 4. Normalised propagation constant as a function of thickness of the QW layers with mask width of $1.5\mu m$ and operating wavelength at $0.9\mu m$.

guide is denoted by E_{mn} mode (m, n are both positive integers) with $m-1$ and $n-1$ field zeros in the x and y directions, respectively. The symmetric E_{11} field profiles, for the case $t_{QW} = 1.6\mu m$ is displayed in Fig. 5. The corresponding confinement factor or fraction of power in the core η is 94.7%. Where

$$\eta = \frac{\int_{A_{core}} \Psi(x,y)^2 dA}{\int_{A_\infty} \Psi(x,y)^2 dA} \qquad (5)$$

and A_{core} is the area of QW layers under the mask.

The antisymmetric E_{21} field profiles, for the case $t_{QW} = 2.2\mu m$ is displayed in Fig. 6.

Finally, the single mode (SM) region is considered. To have single mode operation, the high order mode, E_{21} mode, must be cutoff and only the fundamental mode, E_{11} mode, propagates. Therefore, the thickness of QW layers for SM operation is from $1.3\mu m$ to $1.7\mu m$.

V. CONCLUSION

The modal properties of a multi-quantum well waveguide fabricated using the impurity induced disordering technique is investigated. Modal properties include propagation constant, modal field, confinement factor and single mode operating region. The modal study is based on an improved Fourier decomposition method.

The algorithms developed in present studies can also applied to other optical waveguide employing the impurity induced disordering technique. Example like InGaAs/GaAS quantum well waveguide.
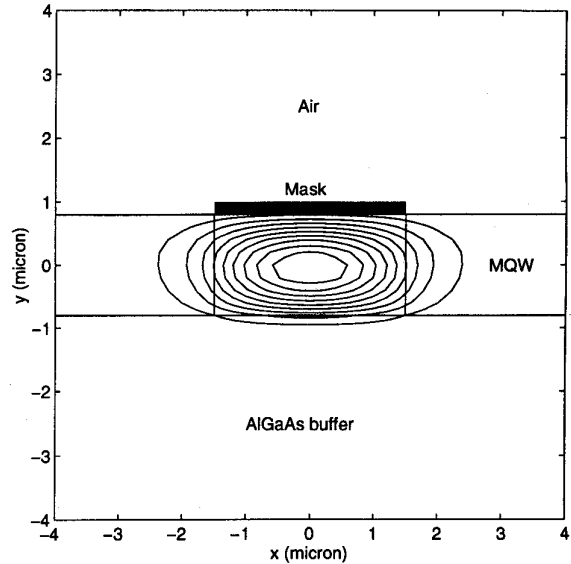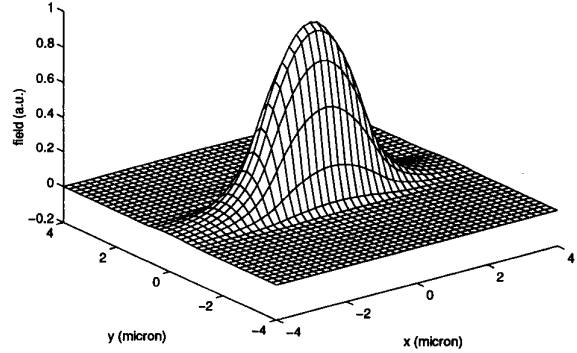
ACKNOWLEDGMENT

Fig. 5. Symmetric E_{11} field profile as determined by FDM with QW layers thickness of $1.6\mu m$. Contour levels are at 10% intervals of the maximum field amplitude.

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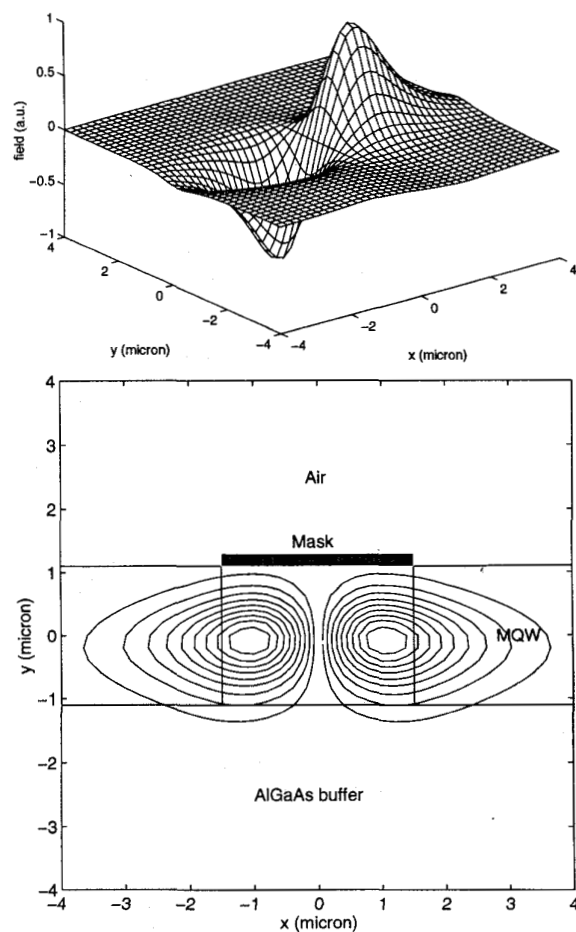
Fig. 6. Antisymmetric E_{21} field profile as determined by FDM with QW layers thickness of $2.2\mu m$. Contour levels are at 10% intervals of the maximum field amplitude.

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