



The Reacceleration of the Shock Wave in the Radio Remnant of SN 1987A

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Abstract

We report on updated radio imaging observations of the radio remnant of SN 1987A at 9 GHz, taken with the Australia Telescope Compact Array (ATCA), covering a 25 yr period (1992–2017). We use Fourier modeling of the supernova remnant to model its morphology, using both a torus model and a ring model, and find that both models show an increasing flux density and have shown a continuing expansion of the remnant. As found in previous studies, we find that the torus model most accurately fits our data and has shown a change in the remnant expansion at day 9300 ± 210 from $2300 \pm 200 \text{ km s}^{-1}$ to $3610 \pm 240 \text{ km s}^{-1}$. We have also seen an increase in brightness in the western lobe of the remnant, although the eastern lobe is still the dominant source of emission, unlike what has been observed at contemporary optical and X-ray wavelengths. We expect to observe a reversal in this asymmetry by the year ~ 2020 , and we note that the southeastern side of the remnant is now beginning to fade, as has also been seen in optical and X-ray data. Our data indicate that high-latitude emission has been present in the remnant from the earliest stages of the shock wave interacting with the equatorial ring around day 5000. However, we find that the emission has become increasingly dominated by the low-lying regions by day 9300, overlapping with the regions of X-ray emission. We conclude that the shock wave is now leaving the equatorial ring, exiting first from the southeast region of the remnant, and is reaccelerating as it begins to interact with the circumstellar medium beyond the dense inner ring.

Key words: circumstellar matter – Magellanic Clouds – supernovae: individual

1. Introduction

SN 1987A is the closest observed supernova to Earth since the invention of the telescope. The initial supernova event was observed on 1987 February 23, and since then monitoring of the supernova remnant (SNR) at multiple wavelengths has provided crucial information in understanding the remnant's evolution (McCray & Fransson 2016). The SNR has been shown to evolve on a timescale of months to years, and its relatively near distance in the Large Magellanic Cloud (~ 50 kpc) has allowed for many details in the structure to be visible.

The progenitor star for SN 1987A, Sanduleak $-69^\circ 202$, was surrounded by an unusual structure of material, believed to be emitted by the progenitor before the supernova explosion. The most striking optical feature consists of two outer rings forming an hourglass structure and one dominant equatorial ring (ER; Burrows et al. 1995). The origin of these rings is unclear, but it is thought that they could have originated from a binary merger $\sim 20,000$ yr ago (Morris & Podsiadlowski 2009, 2007; Menon & Heger 2017; Urushibata et al. 2018), or perhaps a fast-rotating progenitor star (Chita et al. 2008). These rings became visible during the ionizing flash of photons released by the supernova event (Burrows et al. 1995), and the ER is located on the shock front boundary between the H II region of the red supergiant (RSG) progenitor and the RSG free wind (Chevalier & Dwarkadas 1995). The density in the polar directions is thought to be somewhat lower, and little is known about the region beyond the ER (Chevalier & Dwarkadas 1995; Mattila et al. 2010).

The first radio emission from SN 1987A was detected 2 days after the supernova event (1987 February 25) by the Molonglo Observatory Synthesis Telescope (MOST; Turtle et al. 1987).

This emission reached a peak 4 days after the explosion and then faded below a 3σ detection limit ~ 200 days after the explosion (Ball et al. 1995). Emission was then detected again ~ 1200 days after the supernova event (mid-1990), with both MOST and the Australia Telescope Compact Array (ATCA; Staveley-Smith et al. 1992; Ball et al. 1995). Since then, constant monitoring in the 9 GHz band shows that the radio remnant has steadily increased in radio emission, thought to originate from synchrotron emission as electrons are accelerated by the expanding shock waves from the original supernova explosion (Ball & Kirk 1992). Continuous multiwavelength monitoring suggests that the shock wave reached the optical inner ring around day 5500–6500, which corresponded with an increase in observed radio luminosity (Zanardo et al. 2010).

Recent data at both visible and X-ray wavelengths suggest that the SNR is now reaching the end of its current phase of passing through the ER. Fransson et al. (2015) reported that the densest clumps of the emission region have been fading since day ~ 8000 , with diffuse emission and hot spots appearing outside the optical ring around day ~ 9500 . They predicted that the inner ring of the supernova will be destroyed by ~ 2025 . In the X-ray, Frank et al. (2016) report that the 0.5–2 keV light curve has remained constant since day 9500 and that the southeastern side of the ER is fading, which is consistent with optical observations. This suggests that the blast wave is indeed leaving the ER and that the SNR is expanding into the surrounding region. Potter et al. (2014) recently presented a model for radio emission that included the fact that the shock is expanding above and below the ER.

In this paper, we are interested in the most recent evolution of the SN 1987A radio remnant at 9 GHz, as part of a series of

continuing monitoring (Gaensler et al. 1997; Ng et al. 2008, 2013; Zanardo et al. 2013). The most recent observations of the SNR showed a potential break in the expansion of the remnant, which was perhaps due to a change in emission morphology (Ng et al. 2013). Furthermore, a decreasing trend in the east–west surface emissivity of the remnant was observed, with predictions that the western lobe of the SNR would soon dominate in radio emission (Ng et al. 2013; Potter et al. 2014). The eastern side of SN 1987A has always been brighter in earlier epochs, typically attributed to faster shocks in the east (Gaensler et al. 1997; Zanardo et al. 2010), which were possibly caused by an asymmetric explosion (Zanardo et al. 2013). Ng et al. (2013) first noted the decrease in the ER asymmetry at day 7000, which was attributed to these faster shocks in the east encountering the ER and then slowing down and exiting the ER faster than shocks in the west. We seek to identify whether these trends have continued and also whether there is evidence of the shock wave leaving the ER as was reported at optical and X-ray wavelengths.

In this paper, we report on the updated radio observations of SN 1987A through day 10,942 after the supernova explosion, using 9 GHz ATCA data from 1992 January to 2017 February. In Section 2, we discuss our observations and data reduction. In Section 3, we show our resulting images and discuss our analysis of the remnant including Fourier modeling techniques and the subsequent results. In Section 4 we discuss the physical implications of our results and compare SN 1987A to the handful of other spatially resolved radio supernovae.

2. Observations and Data Reduction

Our radio observations are part of a continuing ATCA imaging project at 9 GHz of SN 1987A, which has been bright enough for imaging since day 1786 (Staveley-Smith et al. 1993). These observations are taken using 6 km configurations only, with typically ~ 10 hr of on-source time. This publication covers all observations taken to 2017 February of the source, with observations prior to 2013 July 18 also discussed by Ng et al. (2013). Our new observations are summarized in Table 1.

Observations before 2009 in this monitoring campaign were made in two bands centered at 8.512 and 8.896 GHz, respectively, with a usable bandwidth of 104 MHz each. Since the Compact Array Broadband Backend (CABB; Wilson et al. 2011) upgrade, which enables observations on 2 GHz bandwidth on each band, we have restricted the analysis of 9 GHz monitoring data to two 104 MHz subbands that match the older observation settings.

The data were reduced using the MIRIAD software package (Sault et al. 1995), first using standard flagging and calibration techniques, and then implementing self-calibration (see Gaensler et al. 1997; Ng et al. 2008). We averaged the visibility data first in 1-minute intervals and then formed intensity maps from the visibility data using a maximum entropy algorithm (Gull & Daniell 1978). Finally, we applied a super-resolution technique by restoring the cleaned maps with an FWHM beam of $0''.4$ based on the method outlined by Briggs (1994, 1995).

3. Results

3.1. Images

The 9 GHz images of the remnant derived since 1992 are shown in Figure 1. The remnant forms a circular shell, with brightness varying between different regions. The left (east)

side of the shell is consistently brighter than when it was first observed in 1992, and it has steadily increased in brightness until the present day. The right (west) side of the shell is increasing in brightness but is less bright than the eastern side at all epochs. Emission is also present but more limited in the top (north) and bottom (south) regions. While emission is not uniform, we can see that all of the shell is increasing in brightness during our observations.

We can also see a clear expansion in the shell from 1992 to the present day. In 1992, the radius of the emission region from the center of the SNR to the edge of emission in the eastern side can be measured directly from the image as $\sim 0''.6$, and the 2017 image shows expansion to $\sim 1''.4$. A quantitative analysis of this expansion can be found in Section 3.3.

We have also included contour plots of the images that are new to this paper in Figure 2. We can see that the circular structure of the remnant is present at all epochs and that the remnant is getting brighter. We also see that the southeastern part of the remnant is the only region decreasing in brightness, which can be seen in the final two most recent observations. Specifically, the average flux density in our first three images measured at a 135° angle, which is measured from north to east (from days 9642, 9756, and 9915, respectively), is 10.0 ± 0.1 mJy, which fades to 9.0 ± 0.1 mJy by the observation on day 10,061 and 8.2 ± 0.1 mJy on day 10,942. We acquired these values by measuring the flux density along the southwestern region by drawing a box in the image plane using KVIS, which is marked in Figure 2.

3.2. Fitting

The resolution of imaging data allows us to fit various models to the supernova shell structure and to obtain several parameters for its expansion. For this, we used the Fourier modeling script outlined by Ng et al. (2008) and Ng et al. (2013), which assesses the geometry of the remnant in the visibility (uv) plane, which is defined by a 2D Fourier transform of the sky brightness. The fitting was done using a modified UVFIT task in MIRIAD, which, in addition to the parameter values for the model, also provides χ^2 values in order to confirm the reliability of the fit.

We fit two geometries to the remnant: a 3D torus model and a 2D ring model. Based on previous studies of 9 GHz observations (e.g., Ng et al. 2008, 2013) and the complex remnant geometry (see simulations by Potter et al. 2014), we fit the data with two geometrical models: a 2D ring and a 3D torus. The 2D models allow us to compare to the model used in X-ray studies (Racusin et al. 2009; Helder et al. 2013; Frank et al. 2016). For the torus model, we fit for eight parameters: flux density, center position (in R.A. and decl.), radius, half-opening angle (θ), thickness (as a fraction of the radius), asymmetry (as a percentage), and direction of a linear gradient in surface emission (ϕ) (see Section 3 of Ng et al. 2013). The parameters we obtained can be seen in Table 2, along with the confidence intervals from the χ^2 distribution.

For the ring model, we fit the semimajor axis (R_1) and semiminor axis (R_2), as well as the flux density and center position (see Section 3 of Ng et al. 2013). The obtained parameters can be seen in Table 3 with the χ^2 fit.

Table 1
Observations and Parameters for the Data Sets in This Study

Observing Date	Days since Supernova	Array Configuration	Center Frequency ^a (MHz)	Time on Source (hr)	Epoch Shown in Figure 1 ^b
1992 Jan 14	1786	6B	8640	12	...
1992 Mar 20	1852	6A	8640	10	...
1992 Oct 21	2067	6C	8640, 8900	13	1992.9
1993 Jan 4	2142	6A	8640, 8900	9	1992.9
1993 Jan 5	2143	6A	8640, 8900	6	1992.9
1993 Jun 24	2313	6C	8640, 8900	8	1993.6
1993 Jul 1	2320	6C	8640, 8900	10	1993.6
1993 Oct 15	2426	6A	8640, 9024	17	1993.6
1994 Feb 16	2550	6B	8640, 9024	9	1994.4
1994 Jun 27–28	2681	6C	8640, 9024	21	1994.4
1994 Jul 1	2685	6A	8640, 9024	10	1994.4
1995 Jul 24	3073	6C	8640, 9024	12	1995.7
1995 Aug 29	3109	6D	8896, 9152	7	1995.7
1995 Nov 6	3178	6A	8640, 9024	9	1995.7
1996 Jul 21	3436	6C	8640, 9024	14	1996.7
1996 Sep 8	3485	6B	8640, 9024	13	1996.7
1996 Oct 5	3512	6A	8896, 9152	8	1996.7
1997 Nov 11	3914	6C	8512, 8896	7	1998.0
1998 Feb 18	4013	6A	8896, 9152	10	1998.0
1998 Feb 21	4016	6B	8512, 9024	7	1998.0
1998 Sep 13	4220	6A	8896, 9152	12	1998.9
1998 Oct 31	4268	6D	8502, 9024	11	1998.9
1999 Feb 12	4372	6C	8512, 8896	10	1999.7
1999 Sep 5	4577	6D	8768, 9152	11	1999.7
1999 Sep 12	4584	6A	8512, 8896	14	1999.7
2000 Sep 28	4966	6A	8512, 8896	10	2000.9
2000 Nov 12	5011	6C	8512, 8896	11	2000.9
2001 Nov 23	5387	6D	8768, 9152	8	2001.9
2002 Nov 19	5748	6A	8512, 8896	8	2003.0
2003 Jan 20	5810	6B	8512, 9024	9	2003.0
2003 Aug 1	6003	6D	8768, 9152	10	2003.6
2003 Dec 5	6129	6A	8512, 8896	9	2004.0
2004 Jan 15	6170	6A	8512, 8896	9	2004.0
2004 May 7	6283	6C	8512, 8896	9	2004.4
2005 Mar 25	6605	6A	8512, 8896	9	2005.2
2005 Jun 21	6693	6B	8512, 8896	9	2005.5
2006 Mar 28	6973	6C	8512, 8896	9	2006.2
2006 Jul 18	7085	6A	8512, 8896	9	2006.5
2006 Dec 8	7228	6B	8512, 9024	8	2006.9
2008 Jan 4	7620	6A	8512, 9024	11	2008.0
2008 Apr 23	7730	6A	8512, 8896	11	2008.3
2008 Oct 11	7901	6A	8512, 8896	11	2008.8
2009 Jun 6	8139	6A	9000	11	2009.4
2010 Jan 23	8370	6A	9000	11	2010.1
2010 Apr 11	8448	6A	9000	11	2010.3
2011 Jan 25	8737	6A	9000	11	2011.1
2011 Apr 22	8824	6A	9000	11	2011.3
2012 Jan 12	9089	6A	9000	11	2012.0
2012 Jun 5	9233	6D	9000	11	2012.4
2012 Sep 1	9321	6A	9000	10	2012.7
2013 Mar 7	9509	6A	90006	11	2013.2
2013 May 5	9568	6C	9000	11	2013.3
2013 Jul 18	9642	6A	8512, 8896	10	2013.5
2013 Nov 09	9756	6A	8512, 8896	9	2013.9
2014 Apr 16	9915	6A	8512, 8896	8	2014.3
2016 Mar 03	10601	6B	8512, 8896	8	2016.2
2017 Feb 7	10942	6D	8512, 8896	9	2017.2

Notes. The line between days 9568 and 9756 denotes new data unique to this work.

^a Since the CABB upgrade in mid-2009, data have been recorded over a 2 GHz bandwidth. However, in this analysis we used two 104 MHz subbands with center frequencies of 8.512 and 8.896 GHz, for consistency with the bandwidth of pre-CABB data.

^b Some early data sets have been averaged together to generate the corresponding images in Figure 1 for the listed epoch.

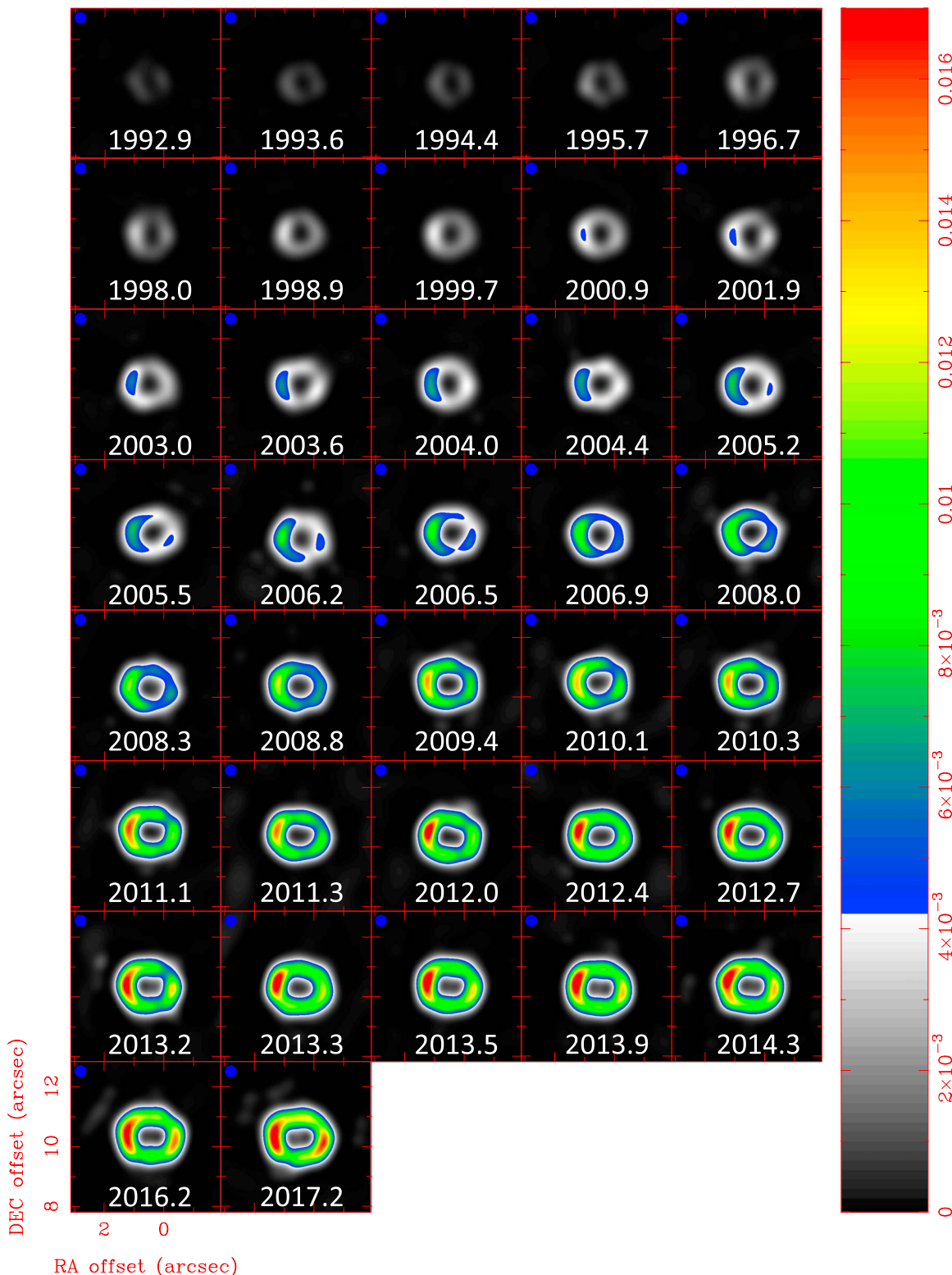


Figure 1. Super-resolved false-color pixel images of SN 1987A at 9 GHz with ATCA data from 1992 to 2017. North is up and east is left. The scale on the right-hand side is the intensity in Jy beam^{-1} , and we have provided the beam size for each image (blue circle, upper left corner) for reference.

3.3. Expansion

The obtained radii for the torus model and for the ring model can be seen in Figure 3. We also included the X-ray radius reported by Frank et al. (2016) for reference, who fit their data with a ring model using a single radius. All three of our models show a clear increase in the radius over the entire time period.

Ng et al. (2013) analyzed the SNR expansion data from day 4000 and reported a break in the expansion rate for the torus model at 7000 ± 200 to a lower speed (with a similar break occurring at the same time in R_2) and a linear trend in R_1 . Thus, when examining our most current data, first we examined data from day 4000 onward in our analysis, as we were most

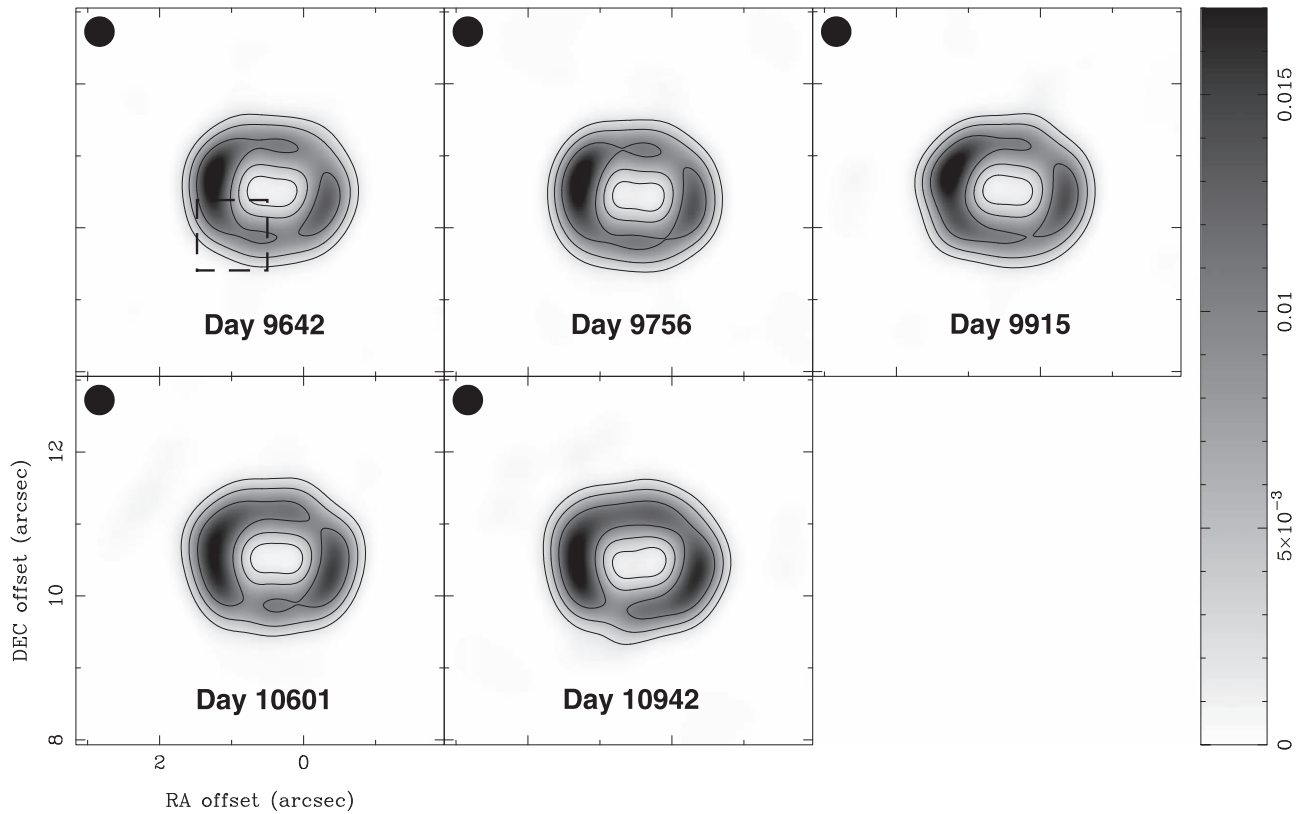


Figure 2. Contour plots of the last five images in Figure 1, by epoch of observation. The contour levels correspond with 2, 5, 10, and 20 mJy beam⁻¹, respectively. The circle in the upper left corner of each image is the beam size, and the dark blue box in the day 9642 image is the southeast corner region.

interested in recent changes in the expansion of the emission. For each of our models, we considered both a linear fit from day 4000 to the present and a break in expansion where the initial rate of linear expansion of the emission region changes to a second rate of expansion. In the latter case, we fit a piecewise function consisting of two different linear slopes, and the transition day where the slope changed was fit as a free parameter. This data fit is consistent with the earlier analysis of Ng et al. (2013) and should emphasize that we do not believe that these times do not necessarily refer to physical events, but rather this method was used in order to identify roughly where changes in the expansion rate occurred. For each fit, we then calculated the Bayesian Information Criterion (BIC; Hogg et al. 2010) so we could compare the two models for each data set (Table 4), where the lower value indicates a more accurate fit. We chose this over the χ^2 fit because the broken linear fit has an extra parameter when compared to a simple linear fit, and the BIC takes into account potential overfitting with this method. As in Kass & Raftery (1995), given $\Delta B_{ij} = |B_i - B_j|$, where B_i and B_j are the BIC values associated with two statistical models, if $3 < \Delta B_{ij} < 10$, the smaller BIC value provides *substantial* evidence that the associate model is more accurate. For $\Delta B_{ij} > 10$, the smaller BIC value provides *strong* evidence that the associate model is more accurate. Therefore, the BIC values listed in Table 4 indicate that the torus model is the most accurate representation of the data after day 7000, since $\Delta B_{ij} = |B_4 - B_2| = 43.6$.

From this, our results for the expansion velocities can be seen in Table 5, where we assumed a distance to the supernova of 51.4 kpc to obtain expansion velocities in km s⁻¹. We found that during this entire period, R_1 has continued expanding

linearly with a velocity of 3800 ± 460 km s⁻¹, which is in agreement with the reported value in Ng et al. (2013) of 3890 ± 50 km s⁻¹. Our test also confirmed the break previously observed at day 7000 in the cases of both the torus model and R_2 . Based on this, we further examined the data from day 7000 to the present with another BIC test comparing a broken linear versus linear model. In this case, linear expansion was the best model for R_2 from day 7000, with a velocity of 2120 ± 40 km s⁻¹, which is greater than the previously reported value for day 7000–9568 from Ng et al. (2013) of 1750 ± 300 km s⁻¹. For the torus model, we identified a second break in the expansion velocity that best fits our data from day 7000 to the present period. This occurred at day 9300 ± 200 , where the expansion rate of the torus model changed from 2300 ± 200 km s⁻¹ to 3610 ± 240 km s⁻¹. For reference, the best fits to our data are in Figure 4.

3.4. Radio Light Curve

The integrated flux densities obtained via the torus and ring models are compared in Figure 5. We chose to measure and list the flux of the model, not the source itself, because this value is tied to the overall geometry versus the individual fluctuations, and our goal was to understand how the models can change. For consistency, we checked the flux of the source in KVIS for the first and last natural images in our data set. For the day 1786 date, we found a flux density of 4.3 ± 0.1 mJy, which can be compared to 4.2 ± 0.2 mJy for the torus model and 3.70 ± 0.12 mJy in the ring model. On day 10,942, we measure 212 ± 3 mJy with this method, compared to 216.43 ± 0.06 mJy for the torus model and 209.78 ± 0.06 mJy for the

Table 2
Best-fit Parameters for the Torus Model with Statistical Uncertainties at 68% Confidence Level

Day	Flux (mJy)	Radius (arcsec)	Half-opening Angle, θ (deg)	Thickness (%)	Asymmetry (%)	ϕ (deg)	$\chi^2_\nu / \text{dof}^a$
1786	4.2 ± 0.2	0.60 ± 0.10	84 ⁺⁶ ₋₂₀	150 ± 50	70 ± 30	187 ± 16	1.8/2107
1852	4.0 ± 0.3	0.62 ± 0.05	80 ± 10	100 ± 50	100 ₋₆₀	180 ⁺¹⁰ ₋₃₀	3.7/1642
2067	5.73 ± 0.12	0.62 ± 0.05	33 ± 4	175 ± 25	81 ± 7	121 ± 6	4.3/3602
2142	5.32 ± 0.14	0.65 ± 0.02	44 ± 2	172 ± 10	96 ± 3	114 ± 7	17/2702
2143	5.7 ± 0.2	0.64 ± 0.01	<12	<20	40 ± 8	108 ± 6	16/1392
2313	6.73 ± 0.11	0.63 ± 0.01	34 ± 7	<20	40 ± 5	94 ± 14	3.6/2902
2320	7.04 ± 0.13	0.67 ± 0.02	37 ± 7	44 ⁺¹⁵ ₋₂₀	38 ± 5	95 ± 13	4.5/2962
2426	6.65 ± 0.10	0.69 ± 0.01	55 ± 4	33 ⁺¹⁰ ₋₁₆	42 ± 5	85 ± 12	5.2/4372
2550	6.63 ± 0.15	0.64 ± 0.04	26 ± 5	175 ± 20	80 ± 6	108 ± 5	7.5/2992
2681	8.41 ± 0.08	0.67 ± 0.01	48 ± 3	18 ⁺¹⁰ ₋₁₇	33 ± 4	92 ± 10	6.0/6142
2685	8.11 ± 0.10	0.66 ± 0.01	54 ± 4	<14	38 ± 6	113 ± 12	5.7/3256
3073	11.11 ± 0.12	0.67 ± 0.01	34 ± 5	46 ± 14	40 ± 3	93 ± 8	5.6/2662
3109	9.7 ± 0.1	0.64 ± 0.02	18 ⁺¹⁰ ₋₁₈	<15	42 ± 2	88 ± 7	17/1598
3178	11.71 ± 0.09	0.685 ± 0.007	45 ± 2	<10	39 ± 2	103 ± 7	4/3442
3436	15.17 ± 0.09	0.705 ± 0.005	47 ± 2	24 ± 11	42 ± 2	95 ± 4	4.9/4337
3485	15.42 ± 0.08	0.707 ± 0.005	51 ± 2	<10	43 ± 2	102 ± 5	5.2/4702
3512	15.43 ± 0.12	0.708 ± 0.006	53 ± 2	<18	42 ± 3	94 ± 6	3.3/2632
3914	17.57 ± 0.14	0.694 ± 0.007	42 ± 3	<10	38 ± 3	111 ± 7	2.4/1272
4013	19.09 ± 0.10	0.754 ± 0.005	46.4 ± 1.4	<5	45.1 ± 1.5	104 ± 4	3.0/2830
4016	18.72 ± 0.10	0.745 ± 0.006	51 ± 2	<5	46 ± 2	103 ± 5	3.1/2512
4220	20.20 ± 0.09	0.729 ± 0.004	43.4 ± 1.3	2 ⁺¹³ ₋₂	37.6 ± 1.3	100 ± 3	2.2/2955
4268	21.78 ± 0.13	0.736 ± 0.006	40 ± 2	28 ± 8	38 ± 2	107 ± 4	7.3/3862
4372	22.94 ± 0.10	0.727 ± 0.005	37 ± 2	23 ± 9	37.4 ± 1.5	114 ± 3	3.6/3532
4577	23.89 ± 0.14	0.757 ± 0.007	40 ± 2	21 ± 6	39 ± 2	103 ± 4	7.0/3442
4584	25.23 ± 0.07	0.747 ± 0.003	42.0 ± 1.0	<5	38.5 ± 1.0	109 ± 2	2.9/4222
4966	29.45 ± 0.06	0.764 ± 0.002	40.8 ± 0.6	<5	39.5 ± 0.6	108.3 ± 1.3	1.3/50689
5011	32.97 ± 0.07	0.775 ± 0.002	44.1 ± 0.7	1 ⁺⁵ ₋₁	40.1 ± 0.6	104.9 ± 1.4	1.4/50531
5387	34.11 ± 0.08	0.790 ± 0.003	41.4 ± 0.8	<3	41.5 ± 0.7	107.8 ± 1.5	1.6/39604
5748	41.68 ± 0.07	0.811 ± 0.002	43.8 ± 0.5	<2	40.2 ± 0.5	103.1 ± 1.2	1.3/38992
5810	42.46 ± 0.07	0.815 ± 0.002	42.9 ± 0.5	1 ⁺⁴ ₋₁	42.8 ± 0.6	117.4 ± 1.0	1.6/46012
6003	46.50 ± 0.07	0.815 ± 0.002	39.6 ± 0.5	<2	38.4 ± 0.5	101.2 ± 1.1	1.6/44992
6129	52.82 ± 0.08	0.833 ± 0.002	42.7 ± 0.5	<2	42.1 ± 0.4	107.7 ± 1.1	1.3/46012
6170	54.05 ± 0.08	0.831 ± 0.002	42.2 ± 0.5	<2	38.8 ± 0.4	107.8 ± 1.1	1.5/43672
6283	53.63 ± 0.07	0.829 ± 0.001	39.6 ± 0.4	<2	38.8 ± 0.4	107.7 ± 0.9	1.5/44842
6605	61.36 ± 0.10	0.843 ± 0.002	38.2 ± 0.5	<2	39.1 ± 0.5	109.0 ± 1.1	2.9/42892
6693	62.69 ± 0.08	0.858 ± 0.001	43.0 ± 0.4	<3	35.9 ± 0.4	101.5 ± 1.0	1.5/38992
6973	73.81 ± 0.08	0.880 ± 0.001	44.6 ± 0.3	<2	42.1 ± 0.4	117.4 ± 0.7	1.5/40357
7085	77.19 ± 0.08	0.872 ± 0.001	39.3 ± 0.3	<1	39.8 ± 0.3	111.8 ± 0.6	1.5/29112
7228	82.51 ± 0.08	0.874 ± 0.001	40.0 ± 0.3	<1	39.4 ± 0.3	109.1 ± 0.7	1.4/35677
7620	93.61 ± 0.09	0.893 ± 0.001	42.7 ± 0.3	<4	38.9 ± 0.3	105.1 ± 0.6	1.3/42892
7730	98.98 ± 0.08	0.8905 ± 0.0008	36.2 ± 0.2	<1	36.3 ± 0.2	109.4 ± 0.5	1.6/40942
7901	107.73 ± 0.08	0.8916 ± 0.0007	35.8 ± 0.2	<2	35.9 ± 0.2	109.1 ± 0.4	1.5/44452
8139	121.59 ± 0.08	0.9095 ± 0.0006	37.6 ± 0.1	<4	32.0 ± 0.1	104.4 ± 0.4	0.5/278820
8370	128.07 ± 0.08	0.9142 ± 0.0006	36.6 ± 0.2	<1	33.4 ± 0.2	105.4 ± 0.4	0.8/254302
8448	132.59 ± 0.07	0.9109 ± 0.0008	33.5 ± 0.2	12 ± 3	28.7 ± 0.1	103.4 ± 0.4	0.9/301177
8737	142.25 ± 0.07	0.9185 ± 0.0005	32.8 ± 0.1	<1	29.8 ± 0.1	104.2 ± 0.4	0.6/251707
8824	136.58 ± 0.08	0.9169 ± 0.0008	28.4 ± 0.2	1 ⁺³ ₋₁	26.9 ± 0.1	105.7 ± 0.4	0.7/241327
9089	155.92 ± 0.06	0.9251 ± 0.0005	30.5 ± 0.1	<1	25.8 ± 0.1	102.3 ± 0.4	1.1/265987
9233	161.00 ± 0.06	0.9290 ± 0.0006	28.8 ± 0.1	1 ⁺² ₋₁	25.8 ± 0.1	102.4 ± 0.3	1.0/301177
9321	165.62 ± 0.05	0.9304 ± 0.0003	29.1 ± 0.1	<1	23.5 ± 0.1	98.4 ± 0.3	0.9/284272
9509	168.68 ± 0.05	0.9467 ± 0.0003	31.7 ± 0.1	<1	26.7 ± 0.1	97.8 ± 0.2	1.4/288550
9568	176.01 ± 0.04	0.9378 ± 0.0002	28.6 ± 0.1	<1	18.4 ± 0.1	111.6 ± 0.3	1.3/283341
9,642	175.81 ± 0.04	0.9464 ± 0.0002	29.68 ± 0.05	<1	21.30 ± 0.04	99.6 ± .2	0.693/ 234782
9756	179.87 ± 0.04	0.9508 ± 0.0002	30.84 ± 0.06	<1	21.98 ± 0.05	103.5 ± 0.2	0.764/ 233190
9915	185.96 ± 0.0005	0.9583 ± 0.0003	30.55 ± 0.06	<2	20.57 ± 5	94.7 ± 0.3	0.7947/230290
10,601	199.45 ± .06	0.9857 ± 0.0003	32.48 ± 0.07	<7	15.42 ± 0.5	88.6 ± 0.4	0.578/118446
10,942	216.43 ± 0.06	0.9975 ± 0.0002	28.36 ± 0.05	9 ± 8	10.36 ± 6	87.5 ± 0.5	0.546/190019

Note.

^a Before 2000, all 26 frequency channels in the data were averaged into one band of effective bandwidth 208 MHz to boost the signal; between 2000 and 2009, 26 Hanning-smoothed channels, each of width 8 MHz, were used in the fit; since mid-2009, after the installation of the CABB, 208 channels in the same frequency range were extracted, each of width 1 MHz. Since 2012, the ATCA sensitivity has improved by ~40% as a result of the installation of new receivers.

ring model. This shows that our using this method to measure total flux is consistent with measuring it for the entire source region and can even be more accurate.

We find that the ring and torus flux density were in agreement, except the ring model is lower than the flux density measurement when compared to the torus measurement in later

epochs. The discrepancy between the two values, which begins at day ~ 6000 , has increased over time, to a ~ 7 mJy difference in 2017, or 3% of the total. Measuring the flux density using another method such as the peak flux value using a conventional software package like KVIS could not distinguish between the two models, as the uncertainty from this method is larger than the difference in flux density between the two models. Instead, we examined the maps of the residual visibilities (i.e., our data minus the model) for both the torus and ring models. We found that the torus model accounted for the emission more accurately than the ring model by showing less residual flux. This leads us to conclude that the flux emission from the torus model is more accurate than the ring model, although we include values for the ring model here for completeness.

Ng et al. (2013) reported that the fluxes obtained were lower than expected from the exponential fit given by Zanardo et al. (2010) from day ~ 7500 . After this time, our data confirm a continuation of this trend. As such, we considered data from day 7500 onward to derive a new modified power-law fit. The radio light curve of SN 1987A can be parameterized by

$$S(\text{mJy}) = K \left(\frac{\nu}{5 \text{ GHz}} \right)^\alpha \left(\frac{t - t_0}{1 \text{ day}} \right)^\beta, \quad (1)$$

where K is the parameter fit due to the flux density, ν is the frequency of observation, α is the spectral index, and β is the modified power-law fit for the light curve (Weiler et al. 2002). Using $\nu = 9 \text{ GHz}$, $\alpha = -0.74$ (Zanardo et al. 2013), and the curve fitting package in SCIPY (Jones et al. 2001), we obtained the parameter values seen in Table 6. The data generated with this model, along with the relevant fits, can be seen in Figure 6 for both models.

We also did the same fitting routine by dividing the flux values for each model by the number of days since the supernova explosion (Figure 7), in order to see whether there are changes in the increase in flux density itself. Here, we can see that from day 7500 the rate of brightness increase has been growing more slowly over time.

3.5. Morphological Behavior

Although the remnant of SN 1987A is increasing in brightness on a power-law scale, this is not evenly distributed throughout the entire ring. Surface brightness asymmetry has been apparent in the remnant since the earliest radio observations, with the eastern (left) lobe the brightest area. We confirm that the eastern lobe is still increasing in flux, although emission from the southeastern quadrant is fading (Figure 2).

On the western side of the source, emission is increasing at a faster rate than previous years when compared to the eastern side. This is particularly visible in the east–west asymmetry of surface emissivity, defined as the slope of the gradient of flux in the image plane (north to east), as seen in Figure 8. We note that this decrease is greater in the ring model than in the torus model. We provide a fit for the change in asymmetry gradient over time, the parameters for which can be seen in Table 7.

The torus model also provides us with the half-opening angle (θ). A plot of these data can be seen in Figure 9. The orientation of the half-opening angle has become more stable after day 4000, and between day 4000 and 7700 it has a mean value $\theta = 41^\circ$. From this point, θ begins to rapidly decrease, until

stabilizing again at day 8800 with a new mean value of $\theta = 29^\circ$.

In the case of the ring model, Ng et al. (2013) noted that the ratio of R_2/R_1 closely follows the trends seen in θ . Results for this ratio over time can be seen in Figure 10. We find that during the day 4000–7700 period, the R_2/R_1 ratio is 0.78 ± 0.01 , and after day 8800 (when θ stabilizes), the ratio is 0.74 ± 0.02 . As such, our findings are consistent with the results from Ng et al. (2013) and have continued to day 11,000.

4. Discussion

The current radio emission from SN 1987A at 9 GHz is dominated by the interaction of the supernova shock wave with the ER, which is a smooth ring interspersed with denser clumps, plus an unknown contribution of polar emission from outside the dense ring. We are currently witnessing the forward shock from the supernova explosion leaving the ER as the reverse shock is driven back into this ring. We first discuss the picture of the SN 1987A CSM during the period when the supernova blast wave pushed through the CSM (day 4000–9300), in both the morphological and physical contexts.

Our breakdown of the day 4000–9300 period in Section 4 is as follows. First, in Section 4.1.1 we discuss the expansion index of both the ring and torus models, which indicates that the increased expansion rate during this period is caused by shock waves at high latitudes in the SNR. In Section 4.1.2, we discuss the coupling between θ and the expansion of the remnant. In Section 4.1.3, we compare our radio observations to X-ray data and discuss how the difference in size between the two is likely physical. In Section 4.1.4, we discuss the delayed change in the asymmetry between the eastern and western lobes of the SNR as predicted from theory and seen at other wavelengths. And in Section 4.1.3, we discuss our increasing flux brightness in the context of potential high-latitude emission and a potential change in emission region within the ER.

After this, in Section 4.2 we will discuss the observed changes in SN 1987A from day 9300 onward, which we interpret as the time at which the shock wave left the ER. In Section 4.3, we will discuss our future predictions for the SNR, including factors such as high-latitude emission and the unknown composition of the region beyond the ER, and make future predictions for the change in asymmetry in emission. Finally, in Section 4.4, we compare SN 1987A to other resolved radio supernovae and discuss in this context how SN 1987A can be used to contrast features such as hot spots and expansion rates in various SNRs.

4.1. Day 4000–9300

4.1.1. Rate of Expansion

In Section 3.3 and Figure 3, we presented our results from the expansion of both the torus and ring models of SN 1987A. When comparing our two models for the SNR expansion, there is a discrepancy in the values for the radius measurement between the torus model radius and R_1 , where the torus values are consistently larger than R_1 (and R_2). This discrepancy was first noted by Ng et al. (2013), who described the cause of this phenomenon in more detail and presented two explanations for it. The first is that the torus model, unlike the ring model, is dependent on the half-opening angle, θ (see Section 4.1.2).

Table 3
Best-fit Parameters for the Ring Model with Statistical Uncertainties at 68% Confidence Level

Day	Flux (mJy)	Semimajor Axis (arcsec)	Seminor Axis (arcsec)	Asymmetry (%)	ϕ (deg)	χ^2/dof^a
1786	3.70 ± 0.12	0.55 ± 0.03	0.50 ± 0.03	33 ± 16	141 ± 26	1.8/2108
1852	3.59 ± 0.14	0.53 ± 0.04	0.48 ± 0.04	25 ± 17	124 ± 46	3.7/1643
2067	5.17 ± 0.09	0.57 ± 0.02	0.49 ± 0.01	27 ± 5	105 ± 16	4.4/3603
2142	4.84 ± 0.11	0.53 ± 0.02	0.51 ± 0.02	17 ± 8	132 ± 29	17/2703
2143	5.62 ± 0.14	0.63 ± 0.03	0.44 ± 0.02	39 ± 8	94 ± 24	16/1393
2313	6.68 ± 0.09	0.57 ± 0.02	0.44 ± 0.01	34 ± 5	90 ± 15	3.6/2903
2320	6.87 ± 0.10	0.61 ± 0.02	0.47 ± 0.01	31 ± 4	92 ± 13	4.5/2963
2426	6.47 ± 0.08	0.56 ± 0.01	0.50 ± 0.01	28 ± 4	86 ± 9	5.2/4373
2550	6.12 ± 0.12	0.58 ± 0.02	0.54 ± 0.02	32 ± 6	117 ± 12	7.5/2993
2681	8.23 ± 0.06	0.58 ± 0.01	0.48 ± 0.01	26 ± 3	87 ± 8	6.0/6143
2685	7.94 ± 0.08	0.56 ± 0.01	0.49 ± 0.01	29 ± 4	109 ± 10	5.7/3257
3073	10.86 ± 0.10	0.62 ± 0.01	0.47 ± 0.01	33 ± 2	87 ± 8	5.6/2663
3109	9.73 ± 0.23	0.60 ± 0.01	0.50 ± 0.01	36 ± 8	92 ± 32	17/1599
3178	11.50 ± 0.07	0.601 ± 0.007	0.487 ± 0.006	32 ± 2	98 ± 6	4.0/3443
3436	14.76 ± 0.07	0.607 ± 0.005	0.495 ± 0.004	33 ± 1	94 ± 4	5.0/4338
3485	15.07 ± 0.07	0.598 ± 0.006	0.510 ± 0.004	33 ± 2	98 ± 4	5.2/4703
3512	15.06 ± 0.10	0.592 ± 0.007	0.508 ± 0.005	32 ± 2	91 ± 5	3.4/2633
3914	17.31 ± 0.12	0.624 ± 0.006	0.491 ± 0.007	33 ± 3	107 ± 7	2.4/1273
4013	18.53 ± 0.09	0.646 ± 0.005	0.527 ± 0.004	35.5 ± 1.2	99 ± 3	3.0/2831
4016	18.36 ± 0.09	0.632 ± 0.005	0.545 ± 0.006	35.8 ± 1.3	98 ± 4	3.1/2513
4220	19.76 ± 0.07	0.643 ± 0.004	0.509 ± 0.003	31.4 ± 1.0	96 ± 3	2.2/2956
4268	21.19 ± 0.11	0.656 ± 0.006	0.506 ± 0.005	31.1 ± 1.5	104 ± 4	7.4/3863
4372	22.43 ± 0.08	0.663 ± 0.004	0.500 ± 0.004	32.1 ± 1.2	111 ± 3	3.6/3533
4577	23.26 ± 0.12	0.674 ± 0.006	0.515 ± 0.005	32.7 ± 1.4	98 ± 4	7.1/3443
4584	24.69 ± 0.07	0.663 ± 0.003	0.521 ± 0.003	31.6 ± 0.8	103 ± 2	2.9/4223
4966	28.75 ± 0.05	0.681 ± 0.002	0.527 ± 0.002	32.9 ± 0.5	102 ± 1	1.3/50690
5011	32.03 ± 0.06	0.677 ± 0.002	0.531 ± 0.002	32.7 ± 0.5	100 ± 1	1.4/50532
5387	33.19 ± 0.07	0.694 ± 0.002	0.547 ± 0.002	34.0 ± 0.5	102 ± 1	1.6/39605
5748	40.56 ± 0.06	0.710 ± 0.002	0.564 ± 0.001	33.0 ± 0.4	97 ± 1	1.3/38993
5810	41.24 ± 0.06	0.723 ± 0.002	0.568 ± 0.002	34.8 ± 0.4	110 ± 1	1.6/46013
6003	45.35 ± 0.06	0.723 ± 0.002	0.561 ± 0.002	32.2 ± 0.4	94 ± 1	1.6/44993
6129	51.43 ± 0.07	0.733 ± 0.002	0.579 ± 0.002	34.7 ± 0.3	100 ± 1	1.3/46013
6170	52.63 ± 0.07	0.734 ± 0.001	0.577 ± 0.002	32.1 ± 0.3	102 ± 1	1.5/43673
6283	52.18 ± 0.06	0.743 ± 0.001	0.569 ± 0.001	32.8 ± 0.3	101 ± 1	1.5/44843
6605	59.86 ± 0.09	0.758 ± 0.002	0.586 ± 0.002	33.0 ± 0.4	101 ± 1	2.9/42893
6693	61.21 ± 0.07	0.7622 ± 0.0013	0.5979 ± 0.0013	30.1 ± 0.3	95 ± 1	1.5/38993
6973	71.33 ± 0.07	0.7743 ± 0.0011	0.6118 ± 0.0014	33.7 ± 0.3	110 ± 1	1.5/40358
7085	74.60 ± 0.07	0.7695 ± 0.0012	0.5939 ± 0.0011	32.6 ± 0.2	103 ± 1	1.6/29113
7228	80.53 ± 0.07	0.7825 ± 0.0009	0.6171 ± 0.0010	33.0 ± 0.2	101 ± 1	1.4/35678
7620	90.47 ± 0.08	0.7830 ± 0.0011	0.6208 ± 0.0009	31.8 ± 0.2	97 ± 1	1.4/42893
7730	96.36 ± 0.07	0.8058 ± 0.0008	0.6179 ± 0.0008	30.9 ± 0.2	102 ± 1	1.6/40943
7901	104.94 ± 0.06	0.8075 ± 0.0007	0.6220 ± 0.0007	30.8 ± 0.1	102 ± 0	1.5/44453
8139	117.73 ± 0.07	0.8241 ± 0.0006	0.6263 ± 0.0006	27.7 ± 0.1	97 ± 0	0.5/278821
8370	124.86 ± 0.07	0.8243 ± 0.0006	0.6428 ± 0.0007	28.6 ± 0.1	98 ± 0	0.8/254303
8448	129.50 ± 0.06	0.8406 ± 0.0005	0.6282 ± 0.0006	25.6 ± 0.1	94 ± 0	0.9/301178
8737	139.17 ± 0.06	0.8433 ± 0.0005	0.6430 ± 0.0005	26.2 ± 0.1	96 ± 0	0.7/251708
8824	133.95 ± 0.07	0.8582 ± 0.0006	0.6373 ± 0.0007	24.1 ± 0.1	96 ± 0	0.7/241328
9089	153.09 ± 0.05	0.8593 ± 0.0004	0.6438 ± 0.0005	23.1 ± 0.1	92 ± 0	1.1/265988
9233	157.94 ± 0.05	0.8698 ± 0.0004	0.6401 ± 0.0005	23.4 ± 0.1	93 ± 0	1.1/301178
9321	162.98 ± 0.05	0.8703 ± 0.0003	0.6527 ± 0.0004	21.5 ± 0.1	88 ± 0	0.9/284273
9509	165.10 ± 0.04	0.8761 ± 0.0003	0.6583 ± 0.0003	24.0 ± 0.1	88 ± 0	1.4/288551
9568	173.03 ± 0.04	0.8818 ± 0.0002	0.6574 ± 0.0003	16.2 ± 0.1	100 ± 0	1.4/283342
9642	171.54 ± .04	0.8781 ± 0.0002	0.6580 ± 0.0002	19.28 ± 0.04	81.7 ± 0.2	0.762/258312
9756	176.54 ± .04	0.8810 ± 0.0002	0.669 ± 0.0003	19.53 ± 0.04	93.1 ± 0.1	0.837/4255481
9915	181.69 ± .05	0.8916 ± 0.0003	0.663 ± 0.0003	18.87 ± 0.05	89.1 ± 0.3	0.655/152784
10601	195.68 ± .06	0.9182 ± 0.0003	0.691 ± 0.0003	14.61 ± 0.06	74.1 ± 0.4	0.651/133454
10942	209.78 ± .06	0.9348 ± 0.0003	0.634 ± 0.0003	10.64 ± 0.07	64.1 ± 0.4	0.653/227191

Note.

^a Before 2000, all 26 frequency channels in the data were averaged into one band of effective bandwidth 208 MHz to boost the signal; between 2000 and 2009, 26 Hanning-smoothed channels, each of width 8 MHz, were used in the fit; since mid-2009, after the installation of the CABB, 208 channels in the same frequency range were extracted, each of width 1 MHz. Since 2012, the ATCA sensitivity has improved by ~40% as a result of the installation of new receivers.

This then creates a projection effect, as the torus model approximates a ring when $\theta = 0^\circ$ but is a shell as θ increases to 90° , and the shell model can have its emission peak inside the shell's radius. Another proposed explanation is that because

the shock wave travels faster in the lower-density regions above the ER (Blondin et al. 1996), any high-latitude material present would manifest in a higher radius measurement for the 3D-sensitive torus model.

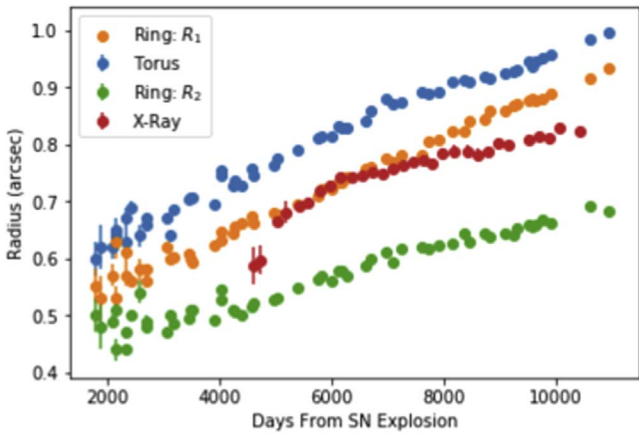


Figure 3. Radius of SN 1987A as a function of time, as measured using the torus model (blue), and the semimajor (R_1) and semiminor (R_2) axes for the ring model (yellow and green, respectively). The radius as measured in the X-ray by *Chandra* (red) is provided for reference from Frank et al. (2016).

Table 4

Bayes Factors Calculated via the Bayesian Information Criterion (BIC) for Six Linear and Multilinear (Piecewise) Models of the Radio Remnant that Rely on Three Radius Geometry Parameters (Torus, Semimajor Radius R_1 , Semiminor Radius R_2)

Model	Type	BIC
Torus	Piecewise	-368.7
Torus	Linear	-325.1
Ring (R_1)	Piecewise	-373.7
Ring (R_1)	Linear	-378.8
Ring (R_2)	Piecewise (semiminor axis)	-365.6
Ring (R_2)	Linear (semiminor axis)	-338.7

Note. All models fit data from day 7200 to day 10,942. Smaller BIC values indicate more accurate fits.

In the case of spherical symmetry in the SNR and a power-law density distribution, one can model the expansion of the SNR as $R \propto t^m$ (Chevalier 1982; Chevalier & Imamura 1982). This is because we expect the forward and reverse shocks to drive our observed expansion, and we can expect these shocks to slow down over time as the ejecta transfer some amount of their kinetic energy into the swept-up material. We can assume that the shock wave entered the ER by day 5600 (Helder et al. 2013), and from this point to the transition observed at day 9300 (see Section 4.2), we find $m = 0.30 \pm 0.01$ for the torus data and 0.41 ± 0.01 for R_1 (Figure 11).

4.1.2. Expansion and Half-opening Angle

When considering the expansion rate of the radio remnant, we already explained in Section 4.1.1 that the torus and ring models give us different values for the radius. However, the ratio between the torus radius and R_1 is not constant, due to the changing velocity of the torus radius (Figure 3). Figure 12 shows the changing ratio of the torus radius divided by R_1 from day 4000. For reference, we have indicated the deceleration at day 7000 and reacceleration at day 9300 (as measured from the torus model) with black dashed lines (see Table 5).

Before day 7000, we find that the ratio is 1.13 ± 0.01 . This corresponds with a period during which Ng et al. (2013) reports that the torus model velocity is higher than the R_1 velocity, at

$4600 \pm 200 \text{ km s}^{-1}$ compared to $3890 \pm 50 \text{ km s}^{-1}$, respectively. These faster initial velocities in the torus model imply that higher-latitude radio emission played a large contribution during this period. From day 7000 to 9300, we see the torus/ R_1 ratio decrease as emission from the low-lying areas begins to dominate, which corresponds with the period when the torus velocity decreases to $2300 \pm 200 \text{ km s}^{-1}$ and R_1 remains constant at $3800 \pm 460 \text{ km s}^{-1}$ in our analysis.

The system restabilized at day 9300 before the ring and torus models could converge, meaning that emission from high latitudes continues to be a factor in the radio remnant. The existence of such emission would also help explain the expansion of both the torus and R_1 sizes beyond the optically observed ER before the shock wave interacted with it (Plait et al. 1995). Further, there is a clear correlation between the expansion of the torus radii and θ during this time period, as shown in Figure 13.

We also see a coupling between the torus/ R_1 radius ratio and the half-opening angle, as shown in Figure 14. This implies that the radio emission has become more ring-like and 2D in nature over time and that the emission is increasingly dominated by lower latitudes. This could be due to one of two reasons. First, it is possible that there previously was a higher amount of high-latitude emission, which has steadily decreased over time. The second option is that while high-latitude emission is still present, the emission from lower latitudes has increasingly dominated, as the shock wave interacted with increasingly dense regions of the ER (Potter et al. 2014).

Finally, we should note that this occurred in conjunction with a decrease in the R_2/R_1 ratio from 0.78 ± 0.01 to 0.74 ± 0.02 , respectively (Figure 10). The ER region is known to have an orientation of 41° to the line of sight (Sugerman et al. 2005), which would imply a ratio of ~ 0.70 . This supports the interpretation that some high-latitude emission has been persistent, but that emission from the ER has dominated more recently.

4.1.3. Size Comparison to X-Ray

The ring model allows us to compare the size of the remnant with X-ray data, which appears to follow a ring model fit (Frank et al. 2016). When comparing the ring model to the X-ray data, the radio-emitting region has consistently been larger than the X-ray-emitting region since day 7500, which was first noted by Ng et al. (2013). Since this date, the trend has continued (Figure 3). This difference is likely physical as opposed to a difference in measuring technique between X-ray and radio (Gaensler et al. 2007; Ng et al. 2009, 2013).

Ng et al. (2009) applied the torus spatial model to day 7736 X-ray observations and found a value of $\theta = 26^\circ \pm 3^\circ$. We note that radio observations at this time yielded a value for θ of 36.2° —that is, at the beginning of the transition of θ from a higher value to its lower one (Figure 9). Further, the X-ray emission at this time is believed to originate from the shock wave interacting with the dense clumps in the ER (Orlando et al. 2015; Frank et al. 2016). The fact that θ derived from our torus model from day 8800 is in agreement with the θ obtained by Ng et al. (2009) suggests that the radio emission also largely originates from the same half-opening angle region as does the X-ray radiation during this time, although the overall emission torus may be larger in radio.

Table 5
Expansion Velocities and Errors of the Radio Remnant from Day 4000 over Time

Model	Transition Date (Days from SN)		Velocity (km s ⁻¹)		
	Transition 1	Transition 2	v_1	v_2	v_3
Torus	7000 ± 200	9300 ± 200	4600 ± 200	2300 ± 200	3610 ± 240
Ring: semimajor axis (R_1)	3800 ± 460
Ring: semiminor axis (R_2)	7000 ± 300	...	3300 ± 200	2120 ± 40	...

Note. Values for v_1 were obtained from Ng et al. (2013), v_2 corresponds with the velocity after the first transition date, and v_3 corresponds with the velocity after the second transition date. A dash corresponds with when no transition to a different velocity was observed.

4.1.4. Asymmetry

The morphological changes in SN 1987A have also included a reduction in the asymmetry of surface brightness between the eastern and western parts of the remnant (Figure 8). A 3D simulation of SN 1987A by Potter et al. (2014) used this assessment and predicted that the faster shocks would first depart the eastern lobe at day 7000 and shocks from the western lobe would later emerge at day 8000. At this point, the model predicted that the asymmetry between the two lobes should pass parity (where the emission is equally bright between the eastern and western lobes), and ultimately the asymmetry should be brighter in the western side by day 9000–10,000. However, we do not observe this in our data; instead, it appears that we are only beginning to approach parity between the eastern and western lobes (where both are equally bright) by day 11,000. This could be attributed to several possibilities, such as an overdensity compared to what was used in theoretical models in the eastern lobe, which would delay the egress of the shock from this area. Another possibility is that the assumed distribution in emission used by Potter et al. (2014) between the forward and reverse shocks is incorrect and that there is instead a longer exit phase as different shocks leave the ring. It should be noted, however, that despite the delay, our observations show a trend that is consistent with model predictions.

We can also compare the asymmetry to what we see in X-ray data. Although it is not known whether the X-ray emission and radio emission necessarily originate from the same region, Frank et al. (2016) note that the radio emission evolves similarly to the X-ray and optical data but is delayed by ~ 2000 days, which appears consistent with our findings (Figure 1). They further suggest that the “hard” component (~ 2 – 10 keV) best matches the radio data in morphology and that the east–west asymmetry only began to reverse in this X-ray band around day ~ 9500 . This delay would be consistent with what we see in our data, where by day 11,000 we have not yet reached parity in the brightness between the eastern and western lobes. As such, it does appear that there is some similarity in the emission region from the ER between the radio and X-ray data.

4.1.5. Flux Density

Radio emission in SN 1987A is thought to be distributed between the forward and reverse shocks (Jun & Norman 1996), although the exact distribution between these is still unknown. In the case of SN 1987A, the picture is further complicated by potential emission from multiple components (Blondin et al. 1996), such as a component arising from the ER and emission from high latitudes. Our residuals when the model was subtracted from the data favored the torus model over the ring

model. This fact suggests that the picture including high-latitude emission is more accurate.

Radio emission in the period from day 5000 to 7500 increases exponentially (Figure 5) and was thought to be caused by interactions between the shock wave and the ER (Zanardo et al. 2010). From day 7500, we still see an increase in brightening of the remnant, but at a reduced rate compared to that in earlier epochs (Figure 6). This transition likely corresponds with a decrease of material interacting with the shock wave during this time, likely corresponding to the shock wave beginning to leave the ER. If the asymmetry of the ER is caused by faster shocks in the east (see Section 4.1.4), as the shock wave leaves the eastern lobe a part of the shock wave would still be interacting with the western lobe, and this would cause the overall flux of the ER to continue increasing until the entire shock wave leaves the ring completely.

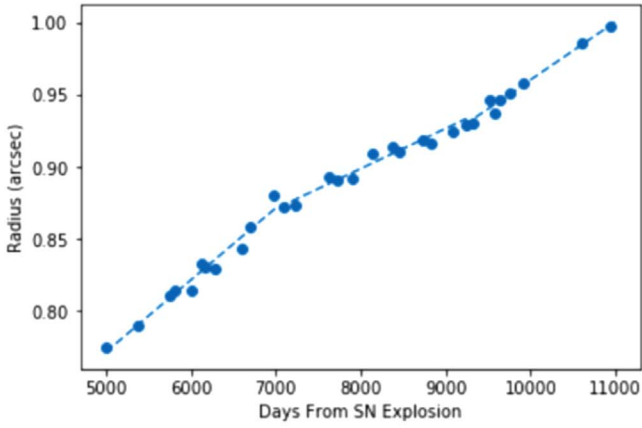
4.1.6. Summary of Day 4000–9300

The day 4000–9300 period was clearly a time of transition in SN 1987A, with many changes observed over the epoch. First, our observed expansion rate in both torus and ring models is consistent with the shock wave interacting with the dense ER. Second, there is a coupling between θ and the torus radii, as shown in Figure 13, whereby the decrease in the rate of expansion of the torus radii at day 7000 corresponds with the half-opening angle for the emission decreasing. The expansion rate for the torus radii then begins to increase again once θ stabilizes. We attribute this to high-latitude emission being present from earlier stages, and then later the lower latitudes beginning to dominate the emission profile. The size of the radio remnant also appears to be larger than that of the X-ray remnant. Further, the radio remnant appears to lag in flux density over time compared to what is seen in the X-ray by ~ 2000 days.

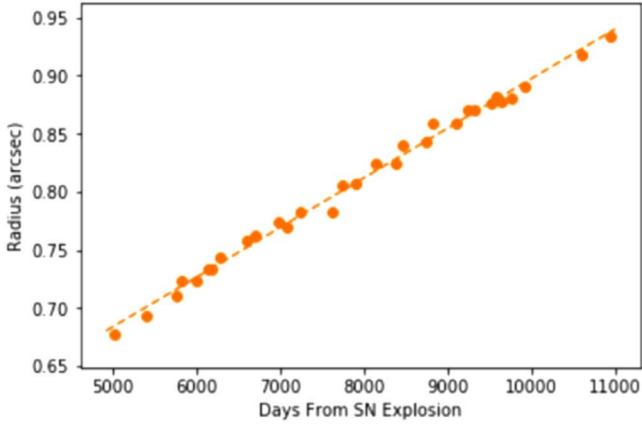
The asymmetry observed between the eastern and western limbs of the ER is delayed compared to predictions in theoretical models, which during this period predicted parity between brightness in both sides and that the western limb would become subsequently brighter. Instead, we see the eastern limb remaining brighter than the western limb. Finally, the flux density of the SNR has continued to increase, but from day 7500 the increase has continued at a lower rate than what was measured for days 4000–7500. This could be due to the shock wave leaving the ring from this period, but the contribution of any emission from high latitudes that has been present since the ER was first encountered is unknown.

4.2. Day 9300 Onward

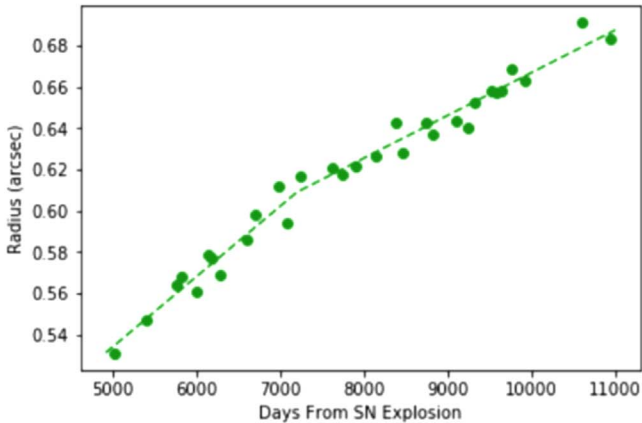
From day 9300, the SNR has undergone several changes. These include the reacceleration to a faster expansion rate in



(a) Torus Radii



(b) Semi-Major Axis in Ring fit (R_1)



(c) Semi-Minor Axis in Ring (R_2)

Figure 4. Subset of data shown in Figure 3 to highlight the difference in fit between the torus radii, R_1 , and R_2 . Here we show the multilinear fit for the torus radius from day 7500 and the linear fit to R_1 and R_2 from day 7000.

the torus model fits to the data to $3610 \pm 240 \text{ km s}^{-1}$ (Table 5 and Figure 3). This is in agreement with the velocity value obtained for R_1 , as well as θ stabilizing at 29.9 ± 0.1 degrees, as seen in Figure 13. This reacceleration has corresponded with an expansion rate $R \propto t^m$ of $m = 0.43 \pm 0.02$ for the torus model and 0.44 ± 0.02 for R_1 . This indicates that a transition occurred around day 9300, which we interpret as the forward shock leaving the ER.

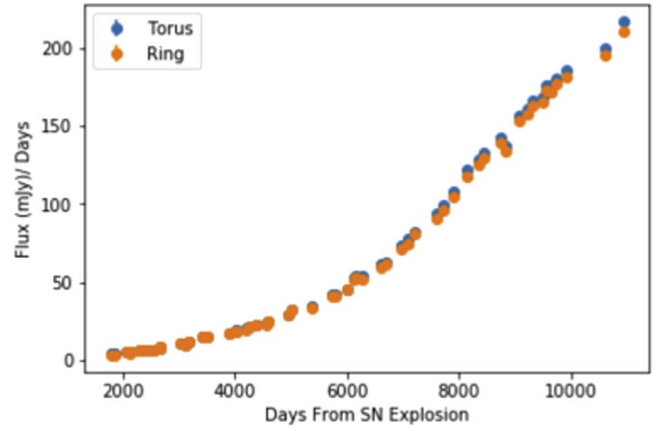


Figure 5. Measured flux densities for the SN 1987A emission region for both the torus and ring models. Note that the errors are included in this plot but are too small to be visible.

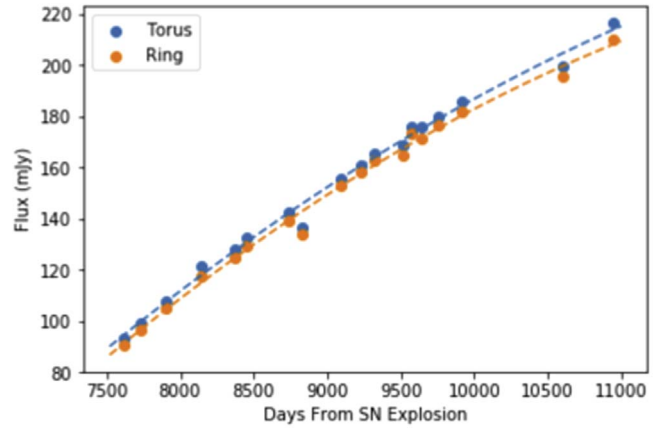


Figure 6. Measured flux densities for the SN 1987A emission region for both the torus and ring models from day 7500, along with the exponential fits to the data following Equation (1) and Table 6.

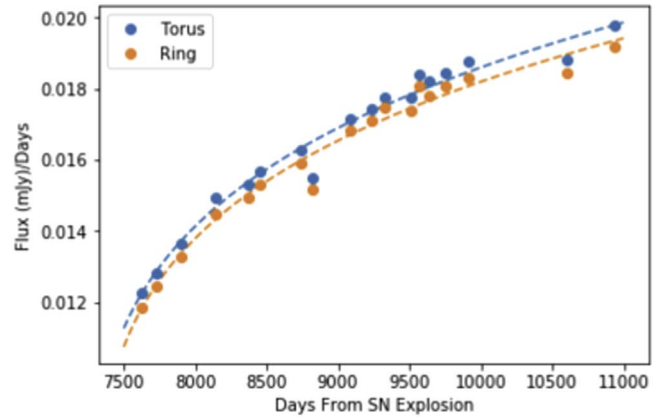


Figure 7. Same as Figure 6, but with the fluxes divided by the day number. This is done to highlight the fact that the rate of brightening in both models has been growing more slowly with time.

Table 6
Parameters for the Exponential Fits Seen in Figure 6

Model	K	t_0 (days)	β
Torus	1.5 ± 0.1	6540 ± 80	0.59 ± 0.02
Ring	2.0 ± 0.12	6680 ± 80	0.55 ± 0.02

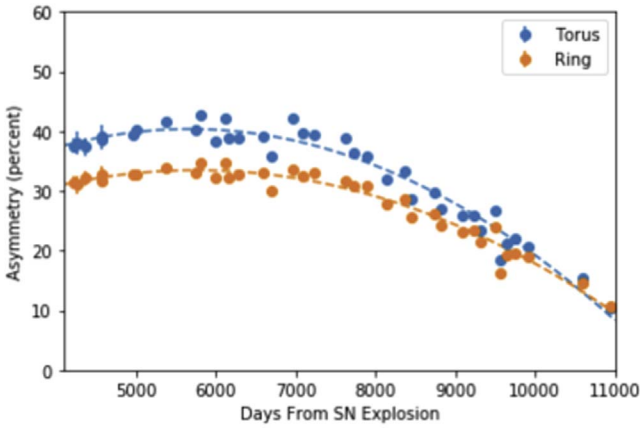


Figure 8. East–west asymmetry in the SN 1987A emission region for both the torus and ring models, modeled as a linear gradient in emissivity across the equatorial plane. The parameters for the fits can be found in Table 7.

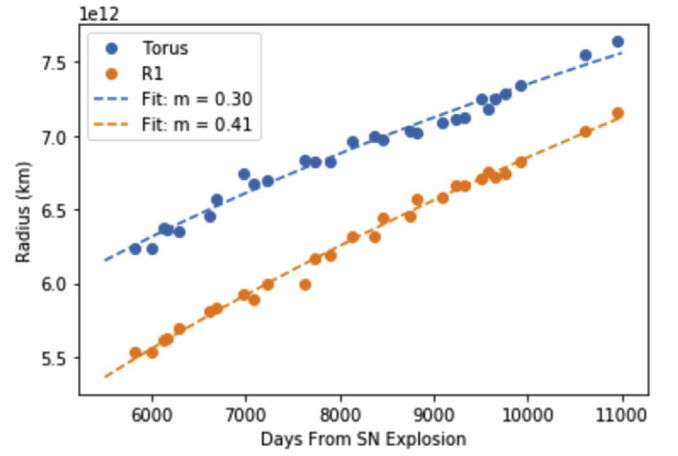


Figure 11. Radius as a function of time during the period when the shock wave was interacting with the ER. We fit the data to $R \propto t^m$, which resulted in a value of $m = 0.30 \pm 0.01$ for the torus model and $m = 0.41 \pm 0.01$ for R_1 .

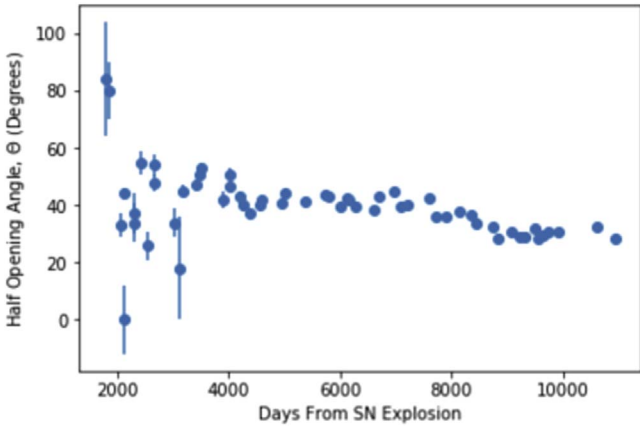


Figure 9. Measured half-opening angle (θ) in the SN 1987A remnant for the torus model.

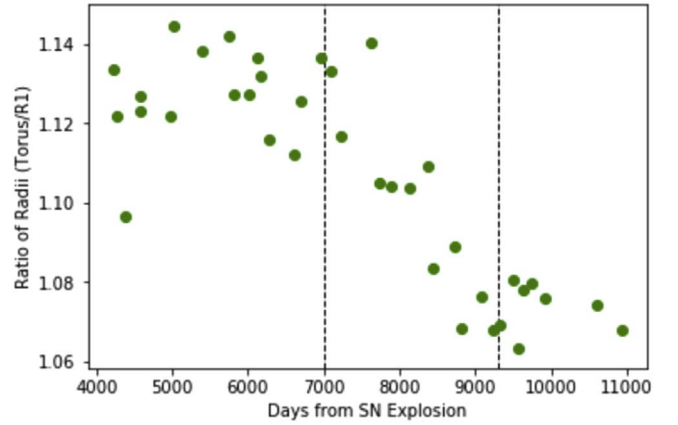


Figure 12. Ratio of the torus radii to R_1 from day 4000 to the present. The black dashed lines are at the two breaks in velocity detected in the torus radius at day 7000 and day 9300, respectively.

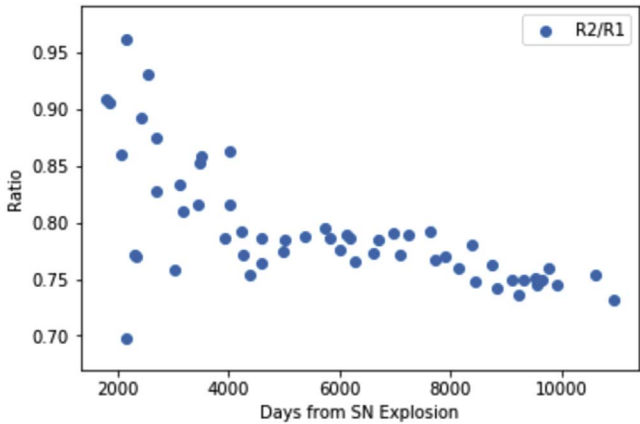


Figure 10. Measured ratio for R_1/R_2 for the ring model. We will note that in this plot the errors are included but are too small to be visible.

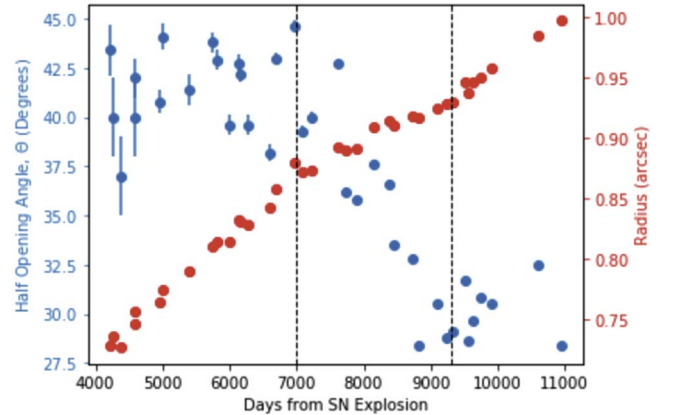


Figure 13. Measured half-opening angle (θ ; blue) in the SN 1987A remnant compared with the radii measured in the torus model (red). Black dashed lines are provided for reference at the two changes in expansion seen in the torus radii at day 7000 and day 9300, respectively.

Table 7

Parameters for the Asymmetry Fits Seen in Figure 8

Model	a	t_0 (days)	β
Torus	4.0 ± 0.1	6540 ± 80	$-1.129 \times 10^{-6} \pm 9 \times 10^{-9}$
Ring	4.6 ± 0.2	6680 ± 80	$-8.71 \times 10^{-7} \pm 9 \times 10^{-9}$

As the SN expands beyond the ER, high-latitude emission components of the radio remnant become more prominent (Potter et al. 2014). Given the hourglass structure of the nebula and its inclination along the line of sight, emission components above and below the equatorial plane have been identified as

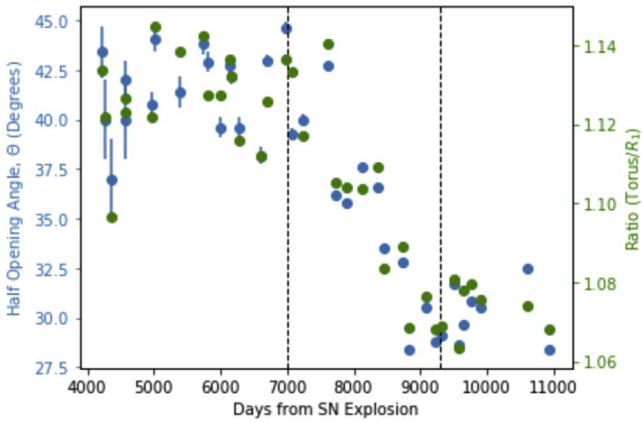


Figure 14. Same as Figure 13, but with the measured half-opening angle plotted with the ratio between the torus model and R_1 (green).

extended bright sites in the northern and southern sectors of the SNR (Zanardo et al. 2018). At 9 GHz, although we cannot distinguish the specific contribution of high-latitude emission from that of emission sites specifically located within the equatorial plane, i.e., where the dense CSM is located, we measured a marked increase of the emission from the northern and southern sites. In particular, within 1000 days (day 9915–10,942), the emission observed in the northern and southern sectors has undergone an increase of 20%, compared to the 10% increase across the eastern lobe (see flux density contours in Figure 2). At day 11,000, the integrated flux density over the northern and southern sites is 12 mJy, while the emission from the brightest eastern sites is 18 mJy. Further, Ng et al. (2013) predicted that if shocks from the lower latitudes continue to dominate the emission, the radius measurements between both the torus and ring measurements should converge. With the reacceleration of the torus expansion rate, we do not see that this will be the case in the future.

The southern part of the emission paints a more complex picture, as we can see by day 10,600 that the southeastern area of the ring has begun to fade (Figure 2). This is consistent with the break-up seen in the X-ray and optical data (Fransson et al. 2015; Frank et al. 2016). Hot spots beyond this area have also been observed in the optical, interpreted as due to the direct interaction of the shock wave with gas beyond the ER (Fransson et al. 2015).

4.3. Future Predictions

The SN 1987A remnant is transitioning into a new phase. Much of what happens next in SN 1987A depends on the density of the area beyond the visible emission region that the shock wave is now entering. Mattila et al. (2010) estimated a mass for the ring but emphasized that this calculation only included the mass ionized by the initial shock breakout from the supernova. As such, it is possible that the density beyond the visible ER could be greater than expected, assuming that the shock wave will enter a region where the CSM will originate from a free RSG wind emitted by the progenitor star (Chevalier & Dwarkadas 1995).

Observations of hot spots appearing beyond the ER at optical wavelengths (Fransson et al. 2015) also indicate that the structure beyond the ER may be more complex than expected. Understanding this structure is particularly important if the CSM is from a binary progenitor model (Morris &

Podsiadlowski 2009; Menon & Heger 2017; Urushibata et al. 2018), as the distribution of material could shed light on slow and fast merger scenarios. Radio observations should tell us more about this environment, as a further increase in shock wave velocity over the next few thousand days would indicate that the density of gas with which the shock wave is interacting is decreasing. Simulations from Potter et al. (2014) predicted a velocity at a few thousand days as high as 6000 km s^{-1} , although this is dependent on the temperature and density for the region.

When it comes to the asymmetry of the SN emission, if we extrapolate the rate of asymmetry decrease seen in Figure 8, we expect the asymmetry to reach parity (where the east and west sides are equally bright) on day $11,650 \pm 60$ using the torus model and on day $12,300 \pm 60$ with the ring model. This prediction is also consistent with the picture seen in X-rays, which is typically 2000 days ahead of the radio (Frank et al. 2016). We also expect this asymmetry to then increase as the western limb increases in brightness and the eastern limb continues to fade, although we note that the rate of asymmetry may change depending on the rate of destruction of the ER in the east and on whether there are notable amounts of ionized or neutral gas beyond the ER that may be as dense as the ER, but not visible. The picture on the western limb may also be more complex, as analysis by Zanardo et al. (2014) suggested residual emission in the western region at higher frequencies that may be attributed to a pulsar wind nebula (PWN).

High-latitude emission may also play a factor in the asymmetry, although we note that the difference in brightness between these two nodes matches very well the picture seen in X-ray data, which indicates that the two bright eastern and western nodes are likely originating from the same region. Currently, the asymmetry values between the torus and ring models are in agreement, which also indicates that the emission creating the asymmetry comes from this region. A divergence in the future asymmetry between the two models would indicate the presence of emission from higher latitudes. Further, if there are notable amounts of polar emission emerging in the next few thousand days, we expect to see further brightening in both the northern and southern areas of the ER. Such emission would be accompanied by an increase in θ .

Finally, the radio flux for the SNR will provide a good indicator for any future high-latitude emission beyond the ER. Little is known of this region, although its contents are thought to be from the RSG wind of the progenitor (Chevalier & Dwarkadas 1995; Mattila et al. 2010). If the material in the SNR is concentrated wholly in the ER, we expect the radio flux to plateau in the next few thousand days as the reverse shock leaves the ER, similar to what was seen in the X-ray emission (Potter et al. 2014; Frank et al. 2016). New material interacting with the shock waves, however, could contribute to a further increase in radio flux.

4.4. Comparison to Other Supernovae

SN 1987A provides a unique opportunity for comparisons between different radio supernovae, as its proximity means that details in the structure can be seen that can only be resolved in a handful of other radio supernovae. Although these other radio supernovae are brighter and have a different CSM density, these comparisons over time allow us to learn how common features such as asymmetry and changes in shock wave velocity are in young supernova environments. In order to

highlight these similarities, in this section we will compare our observations of SN 1987A with those of two other spatially resolved radio SNRs, SN 1986J and SN 1993J.

4.4.1. SN 1986J

SN 1986J was first detected in 1986 via its radio emission, although it is estimated that its explosion epoch is 1983.2 ± 1.1 (Rupen et al. 1987; Bietenholz et al. 2002). It is a Type II_n supernova located at a distance of ~ 10 Mpc (Rupen et al. 1987). Radio emission from the expanding shell of the SNR was the dominant observed emission for many years (Bietenholz et al. 2010), but at present the emission of the shell is decreasing, with the brightness of the outer edge fading faster than the edge near the center (Bietenholz & Bartel 2017). This is because SN 1986J also has an observable central component at its center, first detected at $t \simeq 20$ yr, which is now approximately 10 times brighter than the shell component.

Radio observations of the SN 1986J shell have included a hot spot region brighter than the rest of the shell once resolution was sufficient to observe it (Bietenholz et al. 2002). This is consistent with other spatially resolved radio supernovae, such as SN 1993J (Bietenholz et al. 2010), SN 2011dh (de Witt et al. 2016), and SN 2014C (Bietenholz et al. 2018), where the brighter hot spot regions have expanded homologously with the SNR as the shock wave expanded through the surrounding regions. Further, the SN 1986J shell was reported by Bietenholz & Bartel (2017) as expanding at a velocity of $2810 \pm 750 \text{ km s}^{-1}$, which is consistent with the velocities observed in SN 1987A. As such, it appears that the expansion in both remnants is dominated by the forward shock of the supernova event itself. However, it is likely that the CSM surrounding SN 1986J is much denser than that of SN 1987A based on the former's optical spectral lines (Filippenko 1997).

Overall, the expansion of the ring and the expansion of homologous hot spots with this area of the remnant in SN 1986J are consistent with our observations of SN 1987A. However, the CSM surrounding SN 1986J is distributed very differently, as evidenced by how radio luminosity was likely created by material in the CSM and that the ring is now fading. In the future of SN 1987A, however, any potential increase in radio luminosity detected on the inner edge of the observed ring may be evidence of a compact object. If the compact object in SN 1987A is off-center in the SNR, as suggested by Zanardo et al. (2014), such a brightening would most likely be visible on the inner western lobe.

4.4.2. SN 1993J

SN 1993J, at a distance of 3.62 Mpc in M81, is the second-brightest supernova observed in the past century after SN 1987A. A Type II_n supernova, its progenitor is believed to have had a significantly different mass-loss history compared to SN 1987A, with a simple $\rho \propto r^{-2}$ CSM during its first few hundred days (Staveley-Smith et al. 1993; Weiler et al. 2007). A radio shell was first observed 175 days after the explosion using Very Long Baseline Interferometry (VLBI) imaging, with multiple hot spots that shift in orientation through 2787 days (Bietenholz et al. 2010).

In the SN 1993J disk, an asymmetry in brightness is first seen when the disk appears, in the southeast, but this hot spot appears to shift within a few hundred days and disappear altogether by ~ 1000 days after the supernova explosion

(Bietenholz et al. 2003). This is much faster than what we observe for hot spots in SN 1987A and may imply greater density disparities in the SN 1993J ejecta than that seen in the ER for SN 1987A. Further, asymmetry has been suggested for the SN 1993J explosion based on optical spectra (Lewis et al. 1994), which may also cause radio hot spots similar to those observed for SN 1987A.

Bietenholz et al. (2001) fit the observed SN 1993J remnant with an optically thin spherical shell model, which they felt was accurate as the radio emission was circular to within 4%. If we compare our R_2/R_1 ratio for a 2D model of the emission ring, where we expect a 0.70 ratio based on the inclination of the system, we find that the emission from SN 1987A was more asymmetric during the period when the shock wave was interacting with the ER. This value decreased, however, to 0.74 ± 0.02 in recent observations, meaning that the emission has become more circular over time. This shows that the CSM emitted by the SN 1993J progenitor was more uniform than the complex structure surrounding SN 1987A.

5. Conclusions

We have reported our imaging results of SN 1987A at 9 GHz using ATCA, covering a 25 yr period from 1992 to 2017. We have also carried out Fourier modeling of the visibilities, with a torus model and ring model used to describe the evolving remnant. Both models have shown the continued expansion of SN 1987A through 2017 February, as well as an increasing flux density. Our data are most consistent with a torus model where high-latitude emission is present from soon after the shock wave encountered the ER. This is based on the rate of expansion of the remnant, the observed changes in the evolution of the torus radius at day 7000 and day 9300, and how these data are also coupled with the decrease of the half-opening angle of the remnant during this period. Lower-latitude emission then dominates during the later stages as the shock wave continues to plow through the ER. We should note that the radio remnant appears to be larger than the X-ray remnant, although the radio remnant appears to lag 2000 days after the morphology seen in X-ray data, which may be due to the magnetic fields in the remnant increasing in strength after the shock wave has passed through the medium.

Unlike at other wavelengths, we have not yet seen the western side of the radio remnant become brighter than the eastern side. We have also seen the southeastern side of the SNR begin to fade, which, combined with the similar fading seen in X-ray and optical data, suggests that the shock wave has left at least this region of the ER.

In the future, we expect the western side of the SNR to become the brightest region as the eastern continues to fade, and we also expect a further plateau in radio emission as the shock wave leaves the ER completely. Our observations will also help us understand the structure of material beyond the ER, which is from the progenitor star's stellar wind and about which little is known. Because of its proximity, studies of SN 1987A will also be useful for the comparison to other radio supernovae and their surrounding CSM.






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Facility: ATCA.

Software: MIRIAD, SciPy.

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