

Analysis of Multiuser MIMO Downlink Networks Using Linear Transmitter and Receivers

Zhengang Pan

Department of Electrical and Electronic Engineering, The University of Hong Kong, Pokfulam Road, Hong Kong
Email: zgpan@eee.hku.hk

Kai-Kit Wong

Department of Electrical and Electronic Engineering, The University of Hong Kong, Pokfulam Road, Hong Kong
Email: kitwong@ieee.org

Tung-Sang Ng

Department of Electrical and Electronic Engineering, The University of Hong Kong, Pokfulam Road, Hong Kong
Email: tsng@eee.hku.hk

Received 30 November 2003; Revised 7 April 2004

In contrast to dirty-paper coding (DPC) which is largely information theoretic, this paper proposes a *linear* codec that can spatially multiplex the multiuser signals to realize the rich capacity of multiple-input multiple-output (MIMO) downlink broadcast (point-to-multipoint) channels when channel state information (CSI) is available at the transmitter. Assuming single-stream (or single-mode) communication for each user, we develop an iterative algorithm, which is stepwise optimal, to obtain the multiuser antenna weights accomplishing orthogonal space-division multiplexing (OSDM). The steady state solution has a straightforward interpretation and requires only maximal-ratio combiners (MRC) at the mobile stations to capture the optimized spatial modes. Our main contribution is that the proposed scheme can greatly reduce the processing complexity (at least by a factor of the number of base station antennas) while maintaining the same error performance when compared to a recently published OSDM method. Intensive computer simulations show that the proposed scheme promises to provide multiuser diversity in addition to user separation in the spatial domain so that both diversity and multiplexing can be obtained at the same time for multiuser scenario.

Keywords and phrases: dirty-paper coding, joint-channel diagonalization, MIMO, multiuser communication, orthogonal space-division multiplexing.

1. INTRODUCTION

Recently, multiple-input multiple-output (MIMO) antenna coding/processing has received considerable attention because of the extraordinary capacity advantage over systems with single antenna at both transmitter and receiver ends. Independent studies by Telatar [1] and Foschini and Gans [2] have shown that the capacity of a MIMO channel grows at least linearly with the number of antennas at both ends without bandwidth expansion nor increase in transmit power. This exciting finding has proliferated numerous subsequent studies on more advanced MIMO antenna systems (e.g., [3, 4, 5, 6, 7, 8, 9]). Performance enhancement utilizing MIMO antenna for single-user (point-to-point) wireless communications is by now well developed. The presence of other cochannel users in a MIMO system is, nonetheless, much less understood.

In general, a base station is allowed to have more antennas and is able to afford more sophisticated technologies. Therefore, it is always the responsibility of the base station to design techniques that can manage or control cochannel signals effectively. In the uplink (from many mobile stations (MSs) to one base station), space-division multiple-access (SDMA) can be accomplished through linear array processing [10, 11] or multiuser detection by sphere decoding [12]. However, since a mobile station has to be inexpensive and compact, it rarely can afford the required complexity of performing multiuser detection or have a large number of receiving antennas. Support of multiple users sharing the same radio channel is thus much more challenging in downlink (from one base station to many mobile stations).

Promoting spectral reuse in downlink broadcast channels traces back several decades and the method is based on so-called “dirty-paper coding” (DPC) [13]. By means of known

preinterference cancellation at the transmitter, DPC encodes the data in a way that the codes align themselves as much as possible with each other so as to maximize the sum capacity of a broadcast channel [14, 15, 16]. However, dirty-paper techniques are largely information theoretic and worse of all, the encoding process to achieve the sum capacity is data dependent. This makes it inconsistent with existing communication architectures. For this reason, conventional downlink space-division multiplexing approaches tend to control the multiuser signals based on their signal-to-interference-plus-noise ratio (SINR) using linear transmitter and receivers [17, 18, 19].

In [17, 18], the objective is to maintain for every user a preset SINR for acceptable signal reception. A joint power control and beamforming approach is presented, but a solution is not guaranteed to exist. Subsequently in [19], a closed-form solution that optimizes the base station antenna array in maximizing a lower bound of the product of multiuser SINR is proposed. The problem, however, is that in any of these works, the cochannel users are not truly uncoupled, and the residual cochannel interference (CCI) will not only degrade users' performance, but also more importantly, destroy the independency for managing multiuser signals (since the power of cochannel users must be carefully adjusted jointly). Since it is advantageous to handle users in an orthogonal manner (i.e., zero forcing (ZF)) in the spatial domain, recent attempts focus on the new paradigm of orthogonal space-division multiplexing (OSDM) in the downlink [20, 21, 22, 23, 24, 25, 26, 27].

In [20, 21], support of multiple users using a so-called joint transmission method is introduced in the context of code-division multiple-access (CDMA) systems. Because single-element mobile terminals are considered, these methods solve only the problem for multiuser multiple-input single-output (MISO) scenario. OSDM techniques for multiuser MIMO systems are recently proposed by several authors (e.g., [22, 23, 24, 25, 26, 27]). In [22, 23, 24], by placing nulls at the antennas of all the unintended users, the downlink channel matrix is made block diagonal to eliminate the CCI. However, these methods fail to obtain the rich diversity of the channels and require an unnecessary larger number of transmit antennas at the base station when the mobile stations have multiple antennas. More recently in [25, 26, 27], iterative solutions that are able to optimize the receive antenna combining are presented. Among them, the iterative null-space-directed singular value decomposition (iterative Nu-SVD) proposed in [27] emerges as the most general method that is able to tradeoff between diversity and multiplexing [28] and requires the least possible number of transmit and receive antennas. The drawback, however, is that its complexity grows roughly with the number of base station antennas to the fourth-to-fifth power (see Section 3.2 for details). This greatly limits the scalability of the system when many users are to be served simultaneously.

In this paper, our aim is to devise a reduced-complexity linear codec for OSDM in broadcast MIMO channels and study the diversity and multiplexing behavior of the proposed system. It is assumed (as in [22, 23, 24, 25, 26, 27])

that the channel state information (CSI) is known to both the transmitter and the receivers. By considering only single-stream (or single-mode) communication for each user, we derive a stepwise optimal iterative solution to obtain downlink OSDM. Surprisingly, we will show that the steady state solution has a straightforward interpretation, which ends up every user with a maximal-ratio combiner (MRC) under the ZF constraint. This intuition is then used to render a method that requires much less overall computational complexity. Simulation results demonstrate that the overall complexity of the proposed method is at least a factor of the number of base station antennas smaller than that of the iterative Nu-SVD, yet achieving the same error probability performance.

The proposed scheme is analyzed by intensive computer simulations. In summary, results will reveal that the proposed scheme promises to provide multiuser diversity in addition to user separation in the spatial domain (i.e., both diversity and multiplexing can be obtained at the same time; consistent with single-user MIMO antenna systems [28]). The diversity is not diminishing with the number of users if the number of base station antennas is kept at least the same as the number of users. In addition, the system performance improves with the number of receive antennas at the mobile stations (unlike [22, 23, 24]), showing the importance of collapsing the receive antennas to release the degree of freedom available at the transmitter. Furthermore, the performance degradation is mild even in the presence of spatial correlation as high as 0.4, easily achievable with current antenna design technologies.

The remainder of the paper is organized as follows. In Section 2, we introduce the system model of a multiuser MIMO antenna system in downlink. Section 3 presents the optimality conditions for single-mode OSDM and proposes the iterative method that leads to the solution. Simulation results will be provided in Section 4. Finally, we conclude the paper in Section 5.

Throughout this paper, we use italic letters to denote *scalars*, boldface capital letters to denote *matrices*, and boldface lowercase letters to denote *vectors*. For any matrix \mathbf{A} , \mathbf{A}^\dagger denotes the conjugate transpose of \mathbf{A} and \mathbf{A}^T denotes the transpose of \mathbf{A} , and $a_{n,m}$ or $[\mathbf{A}]_{n,m}$ refers to the (n, m) th entry of \mathbf{A} . In addition, \mathbf{I} denotes the identity matrix, $\mathbf{0}$ denotes the zero matrix, $\|\cdot\|$ denotes the Frobenius norm, and $\mathcal{N}(0, \sigma^2)$ is the complex Gaussian distribution function with zero mean and variance σ^2 .

2. MULTIUSER MIMO SYSTEM MODEL

2.1. Linear signal processing at transmitter and receiver

The system configuration of a multiuser MIMO system in downlink is shown in Figure 1, where signals are transmitted from one base station to M mobile stations, n_T antennas are located at the base station; and n_{R_m} antennas are located at the m th mobile station. The data symbol, z_m , of the m th mobile user, before being transmitted from all of

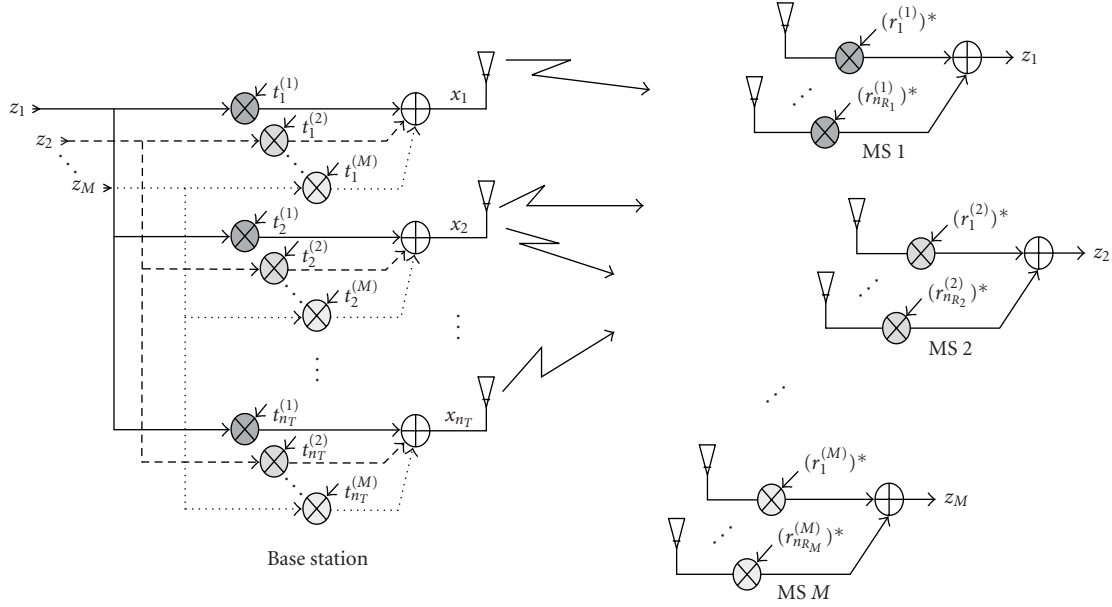


FIGURE 1: System configuration of a multiuser MIMO downlink system.

the n_T base station antennas, is postmultiplied by a complex antenna vector:

$$\mathbf{t}_m = [t_1^{(m)} \ t_2^{(m)} \ \dots \ t_{n_T}^{(m)}]^T \in \mathbb{C}^{n_T}, \quad (1)$$

where $t_k^{(m)}$ represents the transmit antenna weight of the symbol z_m at the k th base station antenna. The weighted symbols of all users at the k th antenna are then summed up to produce a signal x_k , which is finally transmitted from the antenna. Defining the transmitted signal vector as $\mathbf{x} \triangleq [x_1 \ x_2 \ \dots \ x_{n_T}]^T$ and the multiuser transmit weight matrix as $\mathbf{T} \triangleq [\mathbf{t}_1 \ \mathbf{t}_2 \ \dots \ \mathbf{t}_M]$, the transmitted signal vector can be expressed as

$$\mathbf{x} = \sum_{m=1}^M \mathbf{t}_m z_m \equiv \mathbf{Tz}, \quad (2)$$

where $\mathbf{z} \triangleq [z_1 \ z_2 \ \dots \ z_M]^T$ is defined as the multiuser symbol vector. Note that single signal-stream (or single-mode) communication has been assumed for each user.

Given a flat fading channel, at the m th mobile receiver, the signal at each receive antenna is a noisy superposition of the n_T transmitted signals perturbed by fading. As a result, we have

$$\mathbf{y}_m = \mathbf{H}_m \mathbf{x} + \mathbf{n}_m, \quad (3)$$

where $\mathbf{y}_m = [y_1^{(m)} \ y_2^{(m)} \ \dots \ y_{n_{R_m}}^{(m)}]^T$ is the received signal vector with element $y_\ell^{(m)}$ denoting the received signal at the ℓ th antenna of the m th mobile station, \mathbf{n}_m is the noise vector

with elements assumed to have distribution $\mathcal{N}(0, N_0)$, and \mathbf{H}_m denotes the channel matrix from the base station to the m th mobile station, given by

$$\mathbf{H}_m = \begin{bmatrix} h_{1,1}^{(m)} & h_{1,2}^{(m)} & \dots & h_{1,n_T}^{(m)} \\ h_{2,1}^{(m)} & h_{2,2}^{(m)} & \dots & \vdots \\ \vdots & \vdots & \ddots & \vdots \\ h_{n_{R_m},1}^{(m)} & \dots & \dots & h_{n_{R_m},n_T}^{(m)} \end{bmatrix} \in \mathbb{C}^{n_{R_m} \times n_T}, \quad (4)$$

where $h_{\ell,k}^{(m)}$ denotes the fading coefficient from the base station antenna k to the receive antenna ℓ of the m th mobile station. We model $h_{\ell,k}^{(m)}$'s statistically by spatial correlated zero-mean complex Gaussian random variables with unit variance (i.e., $E[|h_{\ell,k}^{(m)}|^2] = 1$), so the amplitudes are Rayleigh distributed and their phases are uniformly distributed from 0 to 2π . Detailed description of spatial correlated multiuser MIMO channel model will be presented in the next subsection.

An estimate of the transmitted symbol, z_m , can be obtained by combining the received signal vector at the m th mobile station. This is done by

$$\hat{z}_m = \mathbf{r}_m^\dagger \mathbf{y}_m, \quad (5)$$

where $\mathbf{r}_m = [r_1^{(m)} \ r_2^{(m)} \ \dots \ r_{n_{R_m}}^{(m)}]^T$ is the receive antenna weight vector of the m th mobile station. Consequently, we can write the multiuser MIMO antenna system as [19, 25]

$$\hat{z}_m = \mathbf{r}_m^\dagger (\mathbf{H}_m \mathbf{Tz} + \mathbf{n}_m) \quad \forall m. \quad (6)$$

If we further define

$$\mathbf{H} \triangleq \begin{bmatrix} \mathbf{H}_1 \\ \vdots \\ \mathbf{H}_M \end{bmatrix}, \quad (7)$$

$\hat{\mathbf{z}} \triangleq [\hat{z}_1 \ \hat{z}_2 \ \cdots \ \hat{z}_M]^T$, $\mathbf{R} \triangleq \text{diag}(\mathbf{r}_1, \mathbf{r}_2, \dots, \mathbf{r}_M)$, and $\mathbf{n} \triangleq [\mathbf{n}_1^T \ \mathbf{n}_2^T \ \cdots \ \mathbf{n}_M^T]^T$, the entire system can be written as

$$\hat{\mathbf{z}} = \mathbf{R}^\dagger \mathbf{H} \mathbf{T} \mathbf{z} + \mathbf{R}^\dagger \mathbf{n}. \quad (8)$$

The definition of (7) will become useful when we introduce the spatial correlation model next.

2.2. Spatially correlated multiuser MIMO channel model

Provided the channels are spatially uncorrelated, then

$$\langle h_{\ell_1, k_1}^{(m_1)}, h_{\ell_2, k_2}^{(m_2)} \rangle = 0, \quad (9)$$

if $m_1 \neq m_2$ or $k_1 \neq k_2$ or $\ell_1 \neq \ell_2$, where $\langle x, y \rangle = \text{E}[xy^*]$. To model the spatial correlation among the antenna elements at the transmitter and receivers, we use the *separable* correlation model [29], which assumes that the correlation among receiver and transmitter array elements is independent from one another. An intuitive justification is that in most situations, only immediate surroundings of the antenna array impose the correlation between array elements and have no impact on correlations observed between the elements of the array at the other end of the link.

With this assumption, spatial correlation can be introduced by postmultiplying the transmitter correlation matrix, $\mathbf{\Gamma}_T^{1/2}$ and premultiplying the receiver correlation matrix, $\mathbf{\Gamma}_R^{1/2}$ so that

$$\mathbf{H} = \mathbf{\Gamma}_R^{1/2} \tilde{\mathbf{H}} (\mathbf{\Gamma}_T^{1/2})^\dagger, \quad (10)$$

where $\tilde{\mathbf{H}}$ is an independent and identically distributed (i.i.d.) channel matrix satisfying (9). Furthermore, as the distance between different mobile stations is generally large enough, it is much reasonable to assume that the correlation between antennas of different mobile stations is zero. Following this, a matrix of the receiver correlation coefficients can be constructed as

$$\mathbf{\Gamma}_R = \text{diag}(\mathbf{\Gamma}_{R_1}, \mathbf{\Gamma}_{R_2}, \dots, \mathbf{\Gamma}_{R_M}). \quad (11)$$

The values of the correlation coefficients may vary according to different communication environments and are usually determined empirically. In order to make our analysis tractable, the single-parameter correlation model proposed

in [30] is used to determine $\mathbf{\Gamma}_T$ and $\mathbf{\Gamma}_R$ as a function of only parameters, γ_T and γ_{R_m} , respectively. Therefore,

$$\mathbf{\Gamma}_T = \begin{bmatrix} 1 & \gamma_T & \gamma_T^4 & \cdots & \gamma_T^{(n_T-1)^2} \\ \gamma_T & 1 & \gamma_T & \ddots & \vdots \\ \gamma_T^4 & \gamma_T & 1 & \ddots & \gamma_T^4 \\ \vdots & \ddots & \ddots & \ddots & \gamma_T \\ \gamma_T^{(n_T-1)^2} & \cdots & \gamma_T^4 & \gamma_T & 1 \end{bmatrix}, \quad (12)$$

$$\mathbf{\Gamma}_{R_m} = \begin{bmatrix} 1 & \gamma_{R_m} & \gamma_{R_m}^4 & \cdots & \gamma_{R_m}^{(n_{R_m}-1)^2} \\ \gamma_{R_m} & 1 & \gamma_{R_m} & \ddots & \vdots \\ \gamma_{R_m}^4 & \gamma_{R_m} & 1 & \ddots & \gamma_{R_m}^4 \\ \vdots & \ddots & \ddots & \ddots & \gamma_{R_m} \\ \gamma_{R_m}^{(n_{R_m}-1)^2} & \cdots & \gamma_{R_m}^4 & \gamma_{R_m} & 1 \end{bmatrix}.$$

3. SINGLE-MODE OSDM IN DOWNLINK

3.1. Optimization of the linear processors

In this section, our objective is to determine the transmit and receive antenna weights, (\mathbf{T}, \mathbf{R}) , that can project the multiuser signals onto orthogonal subspaces (see (14) defined later) and at the same time maximize the sum-gain metric (or the sum of the squared resultant channel responses of the spatial modes). Mathematically, this can be written as

$$(\mathbf{T}, \mathbf{R})_{\text{opt}} = \arg \max_{\mathbf{T}, \mathbf{R}} \|\mathbf{B}\|^2 \quad (13)$$

$$\text{subject to } \mathbf{R}^\dagger \mathbf{H} \mathbf{T} \triangleq \mathbf{B} = \text{diag}(\beta_1, \beta_2, \dots, \beta_M), \quad (14)$$

where β_m is considered as the resultant channel response for user m . Without loss of optimality, hereafter, we will assume that $\|\mathbf{t}_m\| = \|\mathbf{r}_m\| = 1$.

According to (13) and (14), it is clear that the optimal solution of \mathbf{T} and \mathbf{R} will depend on each other. In order to be able to solve this optimization, we will begin by first assuming that all the receive vectors are already fixed and known, and later, consider the optimization over all possible receive vectors. By doing so, the overall system can be reduced to a multiuser MISO system with an equivalent multiuser channel matrix, \mathbf{H}_e , as

$$\mathbf{H}_e \triangleq \mathbf{R}^\dagger \mathbf{H} = \begin{bmatrix} \mathbf{r}_1^\dagger \mathbf{H}_1 \\ \mathbf{r}_2^\dagger \mathbf{H}_2 \\ \vdots \\ \mathbf{r}_M^\dagger \mathbf{H}_M \end{bmatrix} \in \mathbb{C}^{M \times n_T}. \quad (15)$$

Following (13) and (14), we are thus required to find the

optimal transmit antenna weight vectors \mathbf{t}_m 's so that

$$\mathbf{t}_m|_{\text{opt}} = \arg \max_{\mathbf{t}_m} |\beta_m|^2 \quad \forall m, \quad (16)$$

$$\mathbf{H}_e \mathbf{t}_m = [0 \cdots 0 \beta_m 0 \cdots 0]^T. \quad (17)$$

Now, we define another set of weight vectors

$$\mathbf{g}_m \triangleq \frac{\mathbf{t}_m}{|\beta_m|}. \quad (18)$$

Then, the optimization problem (16) and (17) can be rewritten as

$$\mathbf{g}_m|_{\text{opt}} = \arg \min_{\mathbf{g}_m} \|\mathbf{g}_m\|^2 \quad \forall m, \quad (19)$$

$$\mathbf{H}_e \mathbf{g}_m = \mathbf{e}_m \triangleq [0 \cdots 0 \underbrace{1}_{\text{the } m\text{th entry}} 0 \cdots 0]^T, \quad (20)$$

respectively. Further, by defining a matrix $\mathbf{G} \triangleq [\mathbf{g}_1 \mathbf{g}_2 \cdots \mathbf{g}_M]$, (20) can be concisely expressed as

$$\mathbf{H}_e \mathbf{G} = \mathbf{I} \in \mathbb{C}^{M \times M}. \quad (21)$$

In order for (21) to exist, we must have $\text{rank}(\mathbf{H}_e)$, $\text{rank}(\mathbf{G}) \geq \text{rank}(\mathbf{I}) = M$. As a result, OSDM is possible only when $n_T \geq M$ and this constitutes one necessary condition for OSDM in multiuser MISO/MIMO channels [25, 27].

When $n_T = M$, the optimal solution for the weights, \mathbf{G} , is simply

$$\mathbf{G}_{\text{opt}} = \mathbf{H}_e^{-1}, \quad (22)$$

where the superscript -1 denotes inversion of a matrix. Note that this is the one and only one solution for (21).

When $n_T > M$, there are generally infinitely many possible solutions for \mathbf{G} . Among these possible solutions, we need to select the one that performs the minimization of (19), and hence (16). This problem can be recognized as a typical least squares problem for an underdetermined linear system [31] and this can be solved by the following.

Decomposing the equivalent channel matrix as $\mathbf{H}_e = \mathbf{U}\mathbf{\Lambda}\mathbf{V}^\dagger$, where $\mathbf{U} = [\mathbf{u}_1 \mathbf{u}_2 \cdots]$ is the left unitary matrix, $\mathbf{V} = [\mathbf{v}_1 \mathbf{v}_2 \cdots]$ is the right unitary matrix, and $\mathbf{\Lambda} = \text{diag}(\lambda_1, \lambda_2, \dots) \in \mathbb{R}^{M \times n_T}$ whose elements are the singular values of \mathbf{H}_e , the optimal solution for \mathbf{g}_m (in the sense of (19) and (20) jointly) is then given by [31]

$$\mathbf{g}_m|_{\text{opt}} = \sum_{i=1}^M \frac{\mathbf{u}_i^\dagger \mathbf{e}_m}{\lambda_i} \mathbf{v}_i \quad \forall m. \quad (23)$$

More importantly, it can be shown that the solution (23) can be rewritten in a more easy-to-compute form, as the pseudoinverse of \mathbf{H}_e , that is,

$$\mathbf{G}_{\text{opt}} = \mathbf{H}_e^\dagger (\mathbf{H}_e \mathbf{H}_e^\dagger)^{-1} \equiv \mathbf{H}_e^+, \quad (24)$$

where the superscript $+$ denotes the Moore-Penrose pseu-

doinverse of a matrix [31]. Accordingly, we can find the optimal transmit antenna weights by

$$\mathbf{t}_m|_{\text{opt}} = \frac{\mathbf{g}_m|_{\text{opt}}}{\|\mathbf{g}_m|_{\text{opt}}\|} \quad \forall m. \quad (25)$$

Thus far, we have maximized the resultant channel gain based on fixed-value receive vectors. Now, we will further optimize it over all possible receive vectors.

Given the set of the "optimal" transmit vectors, the problem remains to solve the receive weight vector that best balances the CCI and noise at each mobile station (relaxing the ZF constraint for the moment). Apparently, the minimum mean square error (MMSE) solution gives the optimum:

$$\mathbf{r}_m = \frac{\left[(\mathbf{H}_m \tilde{\mathbf{T}}_m) (\mathbf{H}_m \tilde{\mathbf{T}}_m)^\dagger + N_0 \mathbf{I} \right]^{-1} \mathbf{H}_m \mathbf{t}_m}{\left\| \left[(\mathbf{H}_m \tilde{\mathbf{T}}_m) (\mathbf{H}_m \tilde{\mathbf{T}}_m)^\dagger + N_0 \mathbf{I} \right]^{-1} \mathbf{H}_m \mathbf{t}_m \right\|}, \quad (26)$$

where $\tilde{\mathbf{T}}_m = [\mathbf{t}_1 \cdots \mathbf{t}_{m-1} \mathbf{t}_{m+1} \cdots \mathbf{t}_M]$. Equations (25) and (26) jointly compose the optimality conditions for our problem.

To find the antenna weights that satisfy the conditions, an iterative updating process is necessary to tune the transmit and receive vectors because when using (26) for a given (generally not optimal) \mathbf{T} , the orthogonality between different mobiles may be lost due to the mismatch. The details of the algorithm are given as follows.

- (1) Initialize $\mathbf{r}_m = (1/\sqrt{n_{R_m}})[1 \ 1 \ \cdots \ 1]^T$ for all m .
- (2) Obtain \mathbf{H}_e using (15).
- (3) Find \mathbf{T} by (23) and (25).
- (4) For all mobile stations m , update \mathbf{r}_m using (26).
- (5) Compute

$$\mathbf{r}_m^\dagger \mathbf{H}_m \mathbf{T} = (\epsilon_1 \cdots \epsilon_{m-1} \beta_m \epsilon_{m+1} \cdots \epsilon_M). \quad (27)$$

If $|\epsilon_i|$ satisfies a certain condition (will be described next), the convergence is said to be achieved. Otherwise, go back to step (2).

We refer to this method as iterative pseudoinverse MMSE (iterative Pinv-MMSE). By changing the rule for convergence, the iterative algorithm can be used to achieve either OSDM (i.e., ZF) or SINR balancing. For example, if we require that $|\epsilon_i| \leq \epsilon_0$ for all i , where ϵ_0 is a preset value (typically less than 10^{-6}), it ends up ZF. Alternatively, we can have

$$\frac{p_m \beta_m^2}{N_0/2 + \sum_{n=1, n \neq m}^M p_n \epsilon_n^2} \geq \gamma_0, \quad (28)$$

where p_n denotes the transmit power for the n th mobile station, and γ_0 is the preset SINR for ensuring certain link reliability. The above criterion leads to SINR balancing. As stated before, the SINR balancing method involves joint tuning of power distribution, p_n 's and the weight vectors, so it will suffer high complexity and sometimes may not converge. Therefore, we concentrate on the ZF method only.

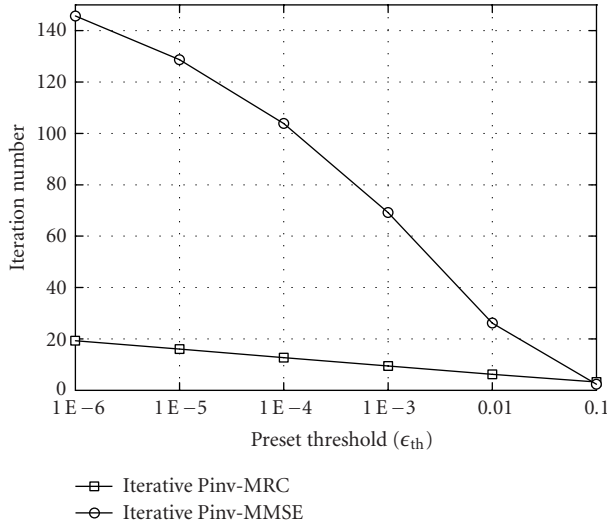


FIGURE 2: Number of iterations versus the preset threshold ϵ_0 .

According to (24) and (26), it is obvious that the optimal solution of \mathbf{T} can be expressed as a function of the noise level N_0 , that is,

$$\mathbf{T}_{opt} = f_{\mathbf{H}}(N_0). \quad (29)$$

However, it can be proved (see the appendix) that with the ZF constraint, the optimum MMSE receiver (26) can be simplified as

$$\mathbf{r}_m = \frac{\mathbf{H}_m \mathbf{t}_m}{\|\mathbf{H}_m \mathbf{t}_m\|}, \quad (30)$$

which is essentially an MRC receiver. This actually reveals that the optimal solution is independent of N_0 . What is important here is that the MMSE solution (26) in step (4) can be replaced by the MRC solution (30) to greatly reduce the computational complexity of the iterative algorithm (to be discussed in Section 3.2). We refer to the method using (30) as iterative Pinv-MRC.

Here, it is worth pointing out two facts. First of all, although iterative Pinv-MRC and iterative Pinv-MMSE converge to the same point, for each iteration, MRC and MMSE receivers do give different updates. As a matter of fact, the two methods may have different convergent properties. Figure 2 shows the number of iterations for convergence versus the preset threshold ϵ_0 , for a system with 4 transmit antennas communicating to 2 mobile stations each with 2 receive antennas, and at signal-to-noise ratio (SNR) of 20 dB. As can be seen, the number of required iterations for iterative Pinv-MMSE is much larger than that for iterative Pinv-MRC.

Secondly, although the iterative process described before involves the computation of receive vectors, they are only temporary variables in the process to optimize the transmit

vectors. In other words, the optimal transmit vectors can be computed solely at the transmitter without the need of coordination with the receivers. This can be made apparent by combining the optimality conditions (24) and (30) together, to yield

$$\mathbf{T} = \begin{bmatrix} \mathbf{t}_1^\dagger \mathbf{H}_1^\dagger \mathbf{H}_1 \\ \mathbf{t}_2^\dagger \mathbf{H}_2^\dagger \mathbf{H}_2 \\ \vdots \\ \mathbf{t}_M^\dagger \mathbf{H}_M^\dagger \mathbf{H}_M \end{bmatrix}^+ \begin{bmatrix} \mu_1 & 0 & \cdots & 0 \\ 0 & \mu_2 & & \vdots \\ \vdots & & \ddots & \\ 0 & \cdots & & \mu_M \end{bmatrix}, \quad (31)$$

where μ_m 's are real constants to ensure $\|\mathbf{t}_m\| = 1$ for all m . Accordingly, we have the following fixed point iteration:

$$\mathbf{T}^{(\nu)} = f(\mathbf{T}^{(\nu-1)}), \quad \nu = 1, 2, \dots, \quad (32)$$

where the superscript ν denotes the ν th iterate, and f indicates the updating procedure stated in (31). The updating equation alone will solve the optimization at the transmitter. As for each mobile receiver, (30) can be used to capture the optimized spatial mode.

3.2. Complexity analysis

Iterative Pinv-MRC offers a linear codec for OSDMM at an affordable complexity compared to existing schemes. To highlight this, the complexity requirements per iteration in terms of the number of floating point operations (flops) for the proposed method and the iterative Nu-SVD method in [27] are listed in Table 1, where $n_{R_m} = n_R$ for all m has been assumed. Further, it is assumed that recursive SVD [31] is used for computing SVD and null-space while matrix inversion is performed using Gaussian elimination.

Note that in most cases, $n_T \geq M \gg n_R$. The dominant factors which determine the computational complexity are M and n_T . It follows that iterative Nu-SVD algorithm needs roughly $O(11n_T^3M + 2n_T^2M^2)$ flops per iteration, while the proposed method requires only $O(4n_TM^2)$ flops per iteration. Therefore, for each iteration, complexity reduction by a factor of at least n_T can be achieved. On the other hand, the complexity is also determined by the number of iterations required for convergence and it will be shown that iterative Pinv-MRC in general requires similar or in some cases a slightly greater number of iterations than iterative Nu-SVD. A more detailed discussion will be provided in Section 4.2 where examples are considered.

4. SIMULATION RESULTS AND DISCUSSION

Monte Carlo simulations have been carried out to assess the system performance of the proposed multiuser MIMO antenna system. Results on average bit error rate (BER) for various SNR are presented. In order to assess how effective the transmit powers are transformed into received power, the SNR used here is the average transmit energy per branch-to-branch versus the power of noise. Perfect CSI is assumed to be available at the base station and all mobile stations.

TABLE 1: Computational complexity requirements.

Iterative Nu-SVD [27]		Iterative Pinv-MRC	
Operation	Number of flops	Operation	Number of flops
\mathbf{H}_e	$2Mn_Tn_R$	\mathbf{H}_e	$2Mn_Tn_R$
$\mathbf{H}_e^{(m)-}$	—	$\mathbf{J} = \mathbf{H}_e\mathbf{H}_e^\dagger$	$2M^2n_T$
$\mathbf{Q}_m = \text{null}\{\mathbf{H}_e^{(m)-}\}$	$2(M-1)n_T^2 + 11n_T^3$	$\mathbf{T} = \mathbf{J}^{-1}$	$(M^3 + M)/3$
For all m $\mathbf{H}_m\mathbf{Q}_m$	$2n_Tn_R(n_T - M + 1)$	$\mathbf{T} = \mathbf{H}_e^\dagger\mathbf{L}$	$2M^2n_T + 3n_TM$
$(\mathbf{r}_m, \mathbf{b}_m) \Leftarrow \text{SVD}(\mathbf{H}_m\mathbf{Q}_m)$	$4n_R^2(n_T - M + 1) + 22(n_T - M + 1)^3$	For all m $\mathbf{r}_m = \mathbf{H}_m\mathbf{t}_m$	$2n_Tn_R + 3n_R$
$\mathbf{t}_m = \mathbf{Q}_m\mathbf{b}_m$	$2n_T(n_T - M + 1)$		

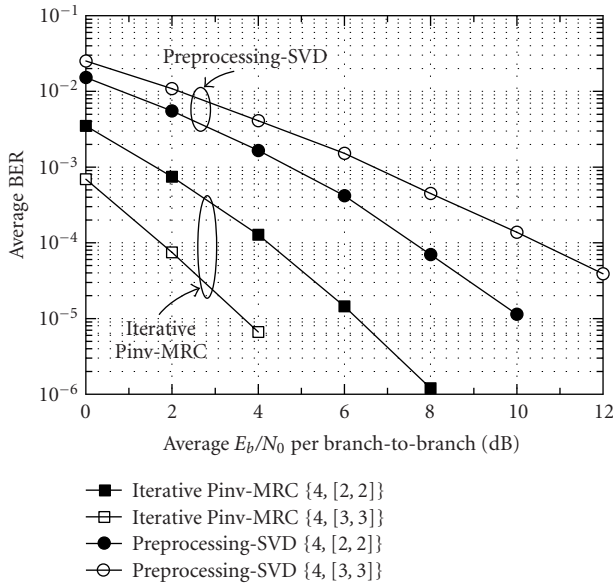


FIGURE 3: Performance comparison of the proposed iterative Pinv-MRC method with the preprocessing-SVD method in [22, 23, 24].

The channel model is assumed to be quasistatic flat Rayleigh fading so that the channel is fixed during one frame and changes independently between frames. The fading coefficients among transmit and receive antenna pairs are spatially correlated and modelled by (10). The frame length is set to be 128 symbols and 4- and 16-QAM (quadrature amplitude modulation) will be used. More than 100 000 independent channel realizations are used to obtain the numerical results for each simulation. For convenience, we will use the notation $\{n_T, [n_{R_1}, \dots, n_{R_M}]\}$ to denote a multiuser MIMO antenna system, which has n_T transmit antennas at the base station and M mobile users each with n_{R_m} receive antennas.

4.1. BER results

4.1.1. Comparison with previous OSDM schemes [22, 23, 24, 25, 26, 27]

In Figure 3, we provide the average BER results for the proposed iterative Pinv-MRC and the approach in [22, 23, 24] (referred to as preprocessing-SVD) for various SNRs

assuming no spatial correlation (i.e., $\gamma_T, \gamma_R = 0$). The system configurations we consider are: (a) $\{4, [2, 2]\}$ and (b) $\{4, [3, 3]\}$. As can be seen in this figure, the performance of iterative Pinv-MRC is significantly better than that of [22, 23, 24]. Specifically, more than an order of magnitude reduction in BER is possible for $\{4, [2, 2]\}$ systems and even more improvement is achieved for $\{4, [3, 3]\}$ systems. Most importantly, for the method in [22, 23, 24], the performance gets worse if the number of mobile station antennas increases since more degrees of freedom need to be consumed for nullification of signals at the receive antennas. However, this is not true for our proposed method, whose performance is shown to improve by increasing the number of receive antennas at the mobile station. This can be explained by the fact that for iterative Pinv-MRC, only one degree of freedom is needed at the transmitter for CCI suppression while the method in [22, 23, 24] requires n_R ($= 2$ or 3) degrees of freedom. The remaining degrees of freedom left at the base station can be utilized for diversity enhancement.

In Figure 4, the average BER results for the proposed iterative Pinv-MRC, the iterative Nu-SVD [27], and the Jacobi-like approach in [25] are plotted against the average SNR for the configuration $\{2, [3, 3]\}$. Results indicate that the three OSDM approaches perform nearly the same. This is further confirmed by other results (which are not included in this paper because of limited space) that the three methods have nearly the same performance with inappreciable difference for the scenarios when all of them obtain downlink OSDM. However, it is worth emphasizing that the method in [25] requires for every mobile station one additional antenna for interference space while the iterative Nu-SVD requires a much higher computational complexity than the proposed iterative Pinv-MRC (see results in Section 4.2).

4.1.2. BER results versus the number of receive antennas at the mobile station

In Figure 5, we investigate the impact on the performance of one user (say, user 1) by varying the number of antennas at another mobile receiver (say, user 2). Three system configurations, $\{2, [1, n_{R_2}]\}$, $\{2, [2, n_{R_2}]\}$, and $\{4, [1, n_{R_2}, 1]\}$ are considered, where n_{R_2} changes from 1 to 8. Specifically, 4-QAM and SNR at 12 dB have been assumed. Results for single-user systems $\{2, [1]\}$, $\{2, [2]\}$ and a 2-user system $\{4, [1, 1]\}$ are also included for comparisons. When n_{R_2} increases, the

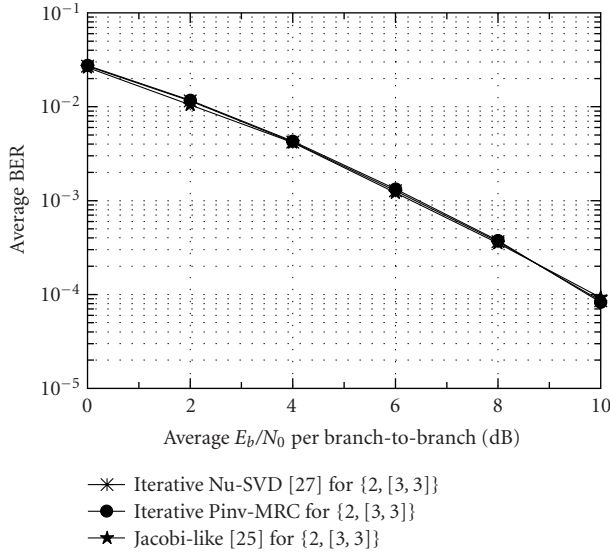


FIGURE 4: Performance comparison of the proposed iterative Pinv-MRC method with the iterative Nu-SVD [27] and the method in [25].

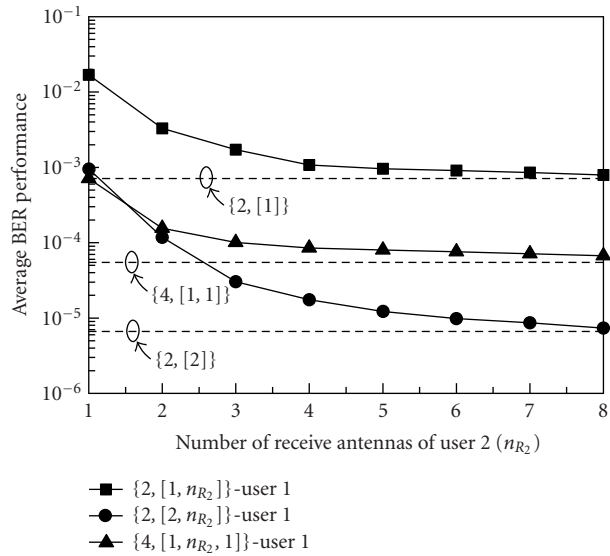


FIGURE 5: Average BER performance of user 1 with increasing number of antennas of user 2 at SNR = 12 dB.

BER performances of user 1 for all three configurations reduce and eventually settle to certain error rates. Intriguingly, for $\{2, [1, n_{R_2}]\}$, if n_{R_2} is large, its performance becomes a single-user system $\{2, [1]\}$. Similarly, $\{2, [2, n_{R_2}]\}$ and $\{4, [1, n_{R_2}, 1]\}$ converge to, respectively, $\{2, [2]\}$ and $\{4, [1, 1]\}$ systems when n_{R_2} is large. In other words, by increasing the number of antennas at mobile station 2, user 2 will appear to be invisible to user 1. The reason is that with sufficiently large number of antennas at mobile station 2, little is needed to be done at the base station for suppressing the CCI to mobile station 2. Consequently, the optimization will be performed as if mobile station 2 does not exist.

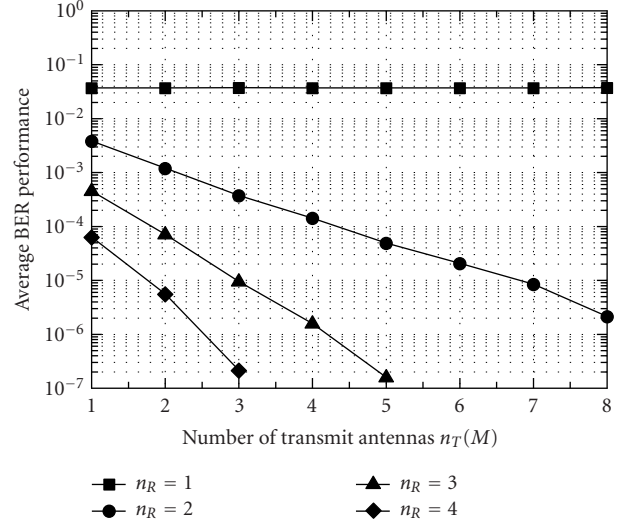


FIGURE 6: Average BER performance of the proposed iterative Pinv-MRC method with various number of users, $n_T = M$, and at SNR = 8 dB.

4.1.3. BER results versus the number of users

In Figure 6, we study the impact of the number of mobile users in the iterative Pinv-MRC system. In this study, transmissions are 4-QAM with 8 dB of average SNR. Making OSDM possible, the number of transmit antennas n_T must be equal to or greater than the number of mobile users M (i.e., $n_T \geq M$) [27]. In this figure, we set $n_T = M$ to see if BER performance depends on the number of users in the system. Results are plotted for various n_R (from 1 to 4). When $n_R = 1$, the BER performance remains unchanged as M increases. This can be explained by the fact that for multiuser MISO antenna systems, the system performance of each mobile station is the same as that of a single-user MISO system with $n_T - M + 1 = 1$ transmit antennas. When $n_R > 1$, the BER performance improves significantly as the number of receive antennas increases and more diversity can be achieved for a system with more users. The reason is that on having more users in the system, more base station antennas need to be employed for user separation. The increase in the degree of freedom contributes partly to maintain the orthogonalization and partly to obtain diversity. Therefore, if the number of transmit antennas keeps matching with the number of users, supporting more users in the system is beneficial, rather than detrimental. Hence, both diversity and multiplexing can be achieved at the same time not only for single-user [28] but also multiuser MIMO antenna systems as well.

4.1.4. BER performances versus number of iterations

Compared to some existing closed-form solutions for multiuser MIMO system [22, 23, 24], the drawback of our method is the need of an iterative process which sometimes may induce unpredictable computational complexity. The investigation of the iteration number needed for

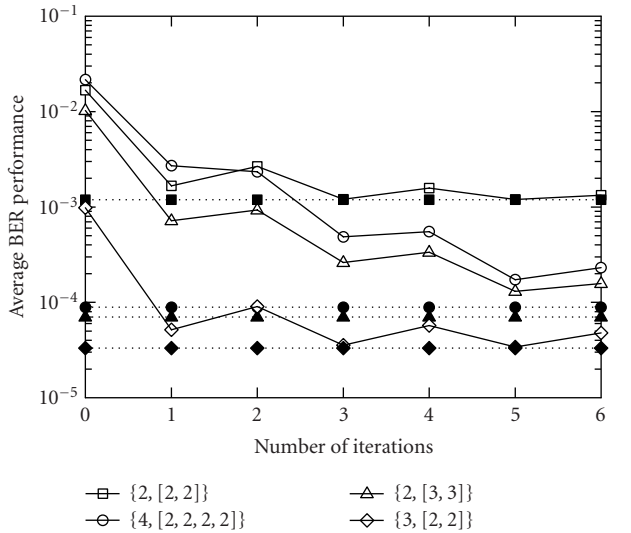


FIGURE 7: Average BER performance of the proposed iterative Pinv-MRC method for various number of iterations at SNR = 8 dB and 4-QAM.

convergence will be presented in the next subsection. Here we show that, in most cases, after a few number of iterations, the system performance will be very close to the steady state solution. Figure 7 gives the average BER performance versus the iteration number under four different system configurations. In this figure, the average SNR is fixed to 8 dB and 4-QAM is used; the dash lines with filled symbols are the steady state performance of the corresponding configurations. It is worth mentioning that the BER performances at 0 iteration are actually the performances of the scheme proposed in [23]. With respect to this point, we can see that our scheme can have significant performance improvement compared to [23] with just a few iterations. Specifically, for $\{2, [2, 2]\}$ and $\{3, [2, 2]\}$, results illustrate that the performance with 1 iteration makes a very significant improvement and converges to the steady state result after only 3 iterations. In addition, results also indicate that the iteration process is not very sensitive to the number of transmit antennas. However, when we increase the number of users M or the number of receive antennas n_R per user, the number of iterations required to give close to the best performance will increase. For instance, for systems $\{4, [2, 2, 2, 2]\}$ and $\{2, [3, 3]\}$, more than 5 iterations would be required to have comparable performance as the steady state result.

4.2. Complexity results

Tables 2 and 3 demonstrate the complexity of the iterative Nu-SVD [27] and the proposed method. Four receive antennas at every mobile station (i.e., $n_{R_m} = n_R = 4$ for all m) is assumed. Results for the average number of iterations for convergence and the number of flops for each iteration are given, respectively, in Tables 2 and 3.

A close observation of Table 2 reveals that the average number of iterations required grows almost linearly with the number of users, M , for both methods. Note, however, that for any fixed M , the average number of iterations required slightly decreases with the number of antennas at the base station, n_T , for iterative Nu-SVD. This does not occur for the proposed iterative Pinv-MRC system where the average number of iterations required increases with the number of base station antennas. Notice also that, in general, the proposed system requires higher number of iterations than that of iterative Nu-SVD, but the difference becomes smaller as the number of users increases. In addition, when $n_T = M$, both systems require more or less the same number of iterations for convergence.

From Table 3, it is apparent that iterative Nu-SVD requires much larger number of flops for each iteration compared with iterative Pinv-MRC. Though the number of flops per iteration for both systems increases with the number of users and the number of base station antennas, the complexity of iterative Nu-SVD is much more sensitive to the increase of the number of base station antennas. In particular, an increase by about a factor of two is observed for an addition of a base station antenna. Results in Table 3 also demonstrate that a reduction by at least a factor of n_T in the number of flops for each iteration can be obtained using the proposed iterative Pinv-MRC. More reduction can be achieved for large M or n_T . For example, in the case of $M = 4$ and $n_T = 8$, reduction by a factor of more than 32 is achieved.

Comparisons of the overall complexity of the two methods are given by the examples in Table 4. As can be seen, reduction by more than an order of magnitude is always realized when $n_T > M$. Specifically, for the $\{5, [2, 2]\}$ system, iterative Pinv-MRC can reduce the overall complexity by a factor of about 18 as compared to iterative Nu-SVD. Note also that for the examples under investigation, more reduction can be obtained if the difference $n_T - M$ is larger. To summarize, for any values of n_T , M , n_R , iterative Pinv-MRC can significantly reduce the complexity of performing OSDM when compared to iterative Nu-SVD, a recently published OSDM system [27], while maintaining the error probability performances as have been demonstrated in Section 4.1.

4.3. Impact of spatial correlation

In this subsection, we investigate the correlation between the number of iterations for convergence and the spatial correlation of the channels. A $\{4, [4, 4]\}$ system using iterative Pinv-MRC is studied and the results are provided in Figure 8. We can observe that when γ_R is fixed to zero, increasing γ_T almost has no effect on the number of iterations. This is not the case when γ_T is fixed to zero; as γ_R increases the number of iterations will decrease. This can be reasoned by the following. The role of receive vector is to combine the channel matrix \mathbf{H}_m and form the “effective” channel vector $\mathbf{r}_m^\dagger \mathbf{H}_m$. Based on the ZF criterion, iteration is required only when the change of receive antenna weights destroys the orthogonality provided by the transmit weights. The iterative process is thus largely dependent on the receive spatial correlation. When the receive spatial correlation is low, even a small

TABLE 2: Average number of iterations required for the iterative Nu-SVD [27]/the proposed iterative Pinv-MRC method when $n_R = 4$.

n_T	$M = 2$	$M = 3$	$M = 4$	$M = 5$	$M = 6$	$M = 7$	$M = 8$
2	21.10/19.98						
3	20.96/23.36	36.45/35.21					
4	19.34/26.30	34.88/35.97	52.52/50.80				
5	18.30/29.30	32.25/39.67	50.19/51.57	69.31/60.96			
6	16.95/30.53	30.88/42.77	45.51/52.44	64.97/61.04	81.85/73.79		
7	16.23/32.05	27.93/43.68	42.29/54.05	59.64/64.52	77.31/74.61	97.53/95.34	
8	15.60/33.46	26.39/45.45	39.96/56.65	58.69/68.57	72.90/76.56	92.30/97.24	111.4/107.3

TABLE 3: Number of flops required for each iteration of the iterative Nu-SVD [27]/the proposed iterative Pinv-MRC method when $n_R = 4$.

n_T	$M = 2$	$M = 3$	$M = 4$	$M = 5$	$M = 6$	$M = 7$	$M = 8$
2	436/135						
3	1406/189	1419/325					
4	3348/243	3552/418	3832/630				
5	6658/297	7353/511	7876/770	8755/1078			
6	11 732/351	13 416/604	14 424/910	15 680/1273	17 580/1694		
7	18 966/405	22 335/697	24 268/1050	26 085/1468	28 578/1952	32 011/2503	
8	28 756/459	34 704/790	38 200/1190	40 960/1663	44 172/2210	48 496/2832	54 064/3523

TABLE 4: Comparisons of the computational complexity and the required number of iterations.

System parameters	Iterative Nu-SVD [27]			Iterative Pinv-MRC		
	Average number of iterations	Flops/iteration	Overall (flops)	Average number of iterations	Flops/iteration	Overall (flops)
{4, [2, 2]}	11.67	2932	34 216	16.23	167	2710
{5, [2, 2]}	11.02	6074	66 935	17.98	206	3703
{6, [2, 2, 2]}	18.07	12 480	225 513	26.75	442	11 823
{6, [2, 2, 2, 2, 2]}	44.97	17 004	764 669	43.6	1730	75 428

adjustment of receive weights will result in dramatic change of the channel vector, leading to large number of iterations irrespective of the transmit spatial correlation. On the contrary, when the receive spatial correlation is high, any updating of the receive antenna weights results in only small change of effective channel vector and the number of iterations required will be small. In the extreme case that the receive antennas are entirely correlated (i.e., $\gamma_R = 1$), the multiuser MIMO system will degenerate to a multiuser MISO system which has a closed-form solution and no iteration is needed.

Results in Figure 9 are provided for illustrating the sensitivity of the BER performance on the spatial correlation of the channel. In this figure, the SNR is set to 16 dB and 4-QAM is assumed. Analysis is done by varying one value of spatial correlation coefficient $\gamma_T(\gamma_R)$ while the other $\gamma_R(\gamma_T)$ is fixed. As expected, results show that the BER is getting worse for higher spatial correlation (either γ_T or γ_R). In-

triguingly, the performance degradation is more severe on the transmit correlation factor than the receive correlation factor. It is worth noting that this is contrary to the known results of the single-user MIMO system where the transmit and receive correlation factors have the same effect on the system performance. In particular, when γ_T approaches 0.99 (perfectly correlated in space), BER becomes 0.5 indicating that the multiuser system actually breaks down. Otherwise, however, the BER performance degrades considerably, but is still able to give BER of 10^{-3} . The reason is that the orthogonality of the system is largely provided by the difference (or rank) of the channels seen by the transmit antenna array. Therefore, when γ_T increases, the channels of the users quickly become nondistinguishable while the effect of increasing γ_R goes only to the loss of receive diversity at the users. Overall, the system performance does not degrade a lot when the spatial correlation is as high as 0.4.

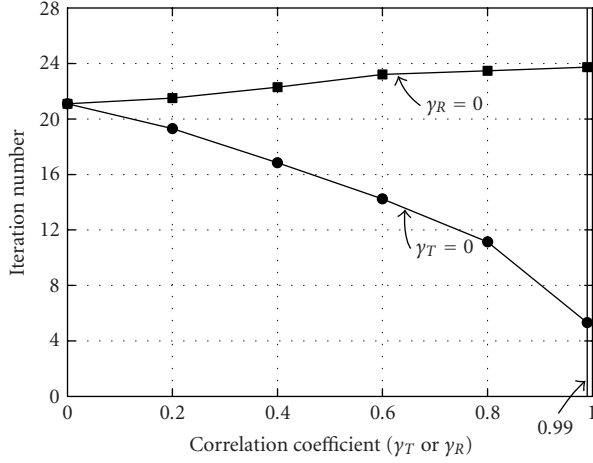


FIGURE 8: Total number of iterations required for iterative Pinv-MRC in spatial correlated downlink channels: a $\{4, [4, 4]\}$ system.

5. CONCLUSIONS

This paper has revisited the OSDM problem in multiuser MIMO downlink channels. A linear codec called iterative Pinv-MMSE, which is stepwise optimal, is proposed to obtain the multiuser antenna weights satisfying the optimality conditions. We have shown analytically that at the optimal point at convergence, we can do iterative Pinv-MRC, which is computationally simpler, yet achieves the same solution. Remarkably, the proposed scheme has been shown by simulation results to yield the same performance as a recently published method [27] with much lower processing complexity. Further, our simulation results have revealed several important findings:

- (1) performance improves as the number of receive antennas at the mobile station increases (unlike the systems in [22, 23, 24]),
- (2) more diversity gain can be achieved for a system with more users if the number of base station antennas keeps matching with the number of users (so both diversity and multiplexing can be obtained at the same time),
- (3) less number of iterations is required for channels with higher receive spatial correlation,
- (4) system performances do not degrade a lot when spatial correlation is as high as 0.4 which is achievable with current antenna design technologies.

APPENDIX

EQUIVALENCE OF MMSE RECEIVER AND MRC RECEIVER AT THE OPTIMUM POINT

As we know, multiplying a scalar value to the receive vector will not affect the final SNR. Therefore, we will ignore

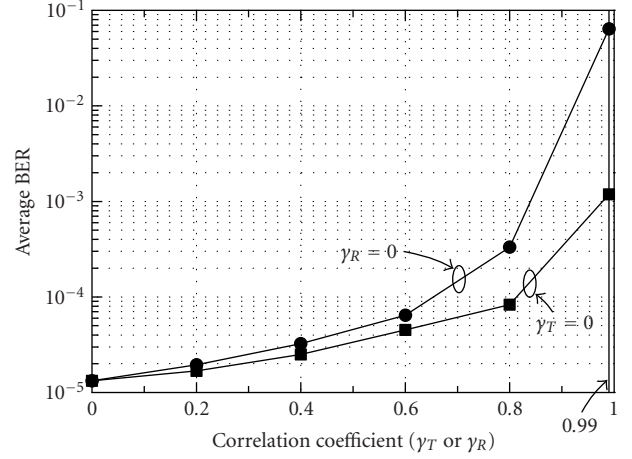


FIGURE 9: BER performance of $\{2, [2, 2]\}$ against various transmit and receive correlation coefficients at SNR = 16 dB and 4-QAM.

the normalization factor (i.e., the denominator) in (26) and (30) in this proof. We will show that, under ZF condition ($\mathbf{r}_m^\dagger \mathbf{H}_m \tilde{\mathbf{T}}_m = 0$), the MMSE receiver will have the same form as MRC receiver.

Before we proceed to the proof, a result on the computation of matrix inversion will be useful. For matrices that have the form as $\mathbf{A}^{-1} + \mathbf{B}\mathbf{B}^\dagger$, the inverse matrix can be computed as $\mathbf{A} - (\mathbf{A}\mathbf{B}(\mathbf{I} + \mathbf{B}^\dagger\mathbf{A}\mathbf{B})^{-1})\mathbf{B}^\dagger\mathbf{A}$. This can be verified by the following:

$$\begin{aligned}
 & (\mathbf{A}^{-1} + \mathbf{B}\mathbf{B}^\dagger) \left(\mathbf{A} - (\mathbf{A}\mathbf{B}(\mathbf{I} + \mathbf{B}^\dagger\mathbf{A}\mathbf{B})^{-1})\mathbf{B}^\dagger\mathbf{A} \right) \\
 &= \mathbf{I} + \mathbf{B}\mathbf{B}^\dagger\mathbf{A} - (\mathbf{B} + \mathbf{B}\mathbf{B}^\dagger\mathbf{A}\mathbf{B})(\mathbf{I} + \mathbf{B}^\dagger\mathbf{A}\mathbf{B})^{-1}\mathbf{B}^\dagger\mathbf{A} \quad (\text{A.1}) \\
 &= \mathbf{I} + \mathbf{B}\mathbf{B}^\dagger\mathbf{A} - \mathbf{B}(\mathbf{I} + \mathbf{B}^\dagger\mathbf{A}\mathbf{B})(\mathbf{I} + \mathbf{B}^\dagger\mathbf{A}\mathbf{B})^{-1}\mathbf{B}^\dagger\mathbf{A} \\
 &= \mathbf{I} + \mathbf{B}\mathbf{B}^\dagger\mathbf{A} - \mathbf{B}\mathbf{B}^\dagger\mathbf{A} = \mathbf{I}.
 \end{aligned}$$

With the above result, and by considering $\mathbf{A} = \mathbf{I}/N_0$ and $\mathbf{B} = \mathbf{H}_m \tilde{\mathbf{T}}_m$, we can compute the MMSE receiver as

$$\begin{aligned}
 \mathbf{r}_m &= (\mathbf{B}\mathbf{B}^\dagger + \mathbf{A}^{-1})^{-1} \mathbf{H}_m \mathbf{t}_m \\
 &= \left(\mathbf{A} - (\mathbf{A}\mathbf{B}(\mathbf{I} + \mathbf{B}^\dagger\mathbf{A}\mathbf{B})^{-1})\mathbf{B}^\dagger\mathbf{A} \right) \mathbf{H}_m \mathbf{t}_m \\
 &= \mathbf{A}\mathbf{H}_m \mathbf{t}_m + \left(\mathbf{A}\mathbf{B}(\mathbf{I} + \mathbf{B}^\dagger\mathbf{A}\mathbf{B})^{-1} \right) (\mathbf{B}^\dagger \mathbf{A}\mathbf{H}_m \mathbf{t}_m) \\
 &= \frac{1}{N_0} \mathbf{H}_m \mathbf{t}_m + \frac{1}{N_0} \left(\mathbf{A}\mathbf{B}(\mathbf{I} + \mathbf{B}^\dagger\mathbf{A}\mathbf{B})^{-1} \right) (\mathbf{B}^\dagger \mathbf{H}_m \mathbf{t}_m) \\
 &= \frac{1}{N_0} \mathbf{H}_m \mathbf{t}_m + \frac{1}{N_0} \left(\mathbf{A}\mathbf{B}(\mathbf{I} + \mathbf{B}^\dagger\mathbf{A}\mathbf{B})^{-1} \right) \left((\mathbf{H}_m \tilde{\mathbf{T}}_m)^\dagger \mathbf{H}_m \mathbf{t}_m \right). \quad (\text{A.2})
 \end{aligned}$$

Given $\mathbf{r}_m^\dagger \mathbf{H}_m \tilde{\mathbf{T}}_m = 0$, $\mathbf{r}_m = (1/N_0)\mathbf{H}_m \mathbf{t}_m$ will always be satisfied. As in this case, the second part of above equation will be zero because $(\mathbf{H}_m \tilde{\mathbf{T}}_m)^\dagger \mathbf{H}_m \mathbf{t}_m = N_0 (\mathbf{H}_m \tilde{\mathbf{T}}_m)^\dagger \mathbf{r}_m = 0$.

ACKNOWLEDGMENT

This work was supported in part by the Hong Kong Research Grant Council and the University of Hong Kong Research Committee.

REFERENCES

- [1] I. E. Telatar, "Capacity of multi-antenna Gaussian channels," Internal Tech. Memo, AT&T Bell Laboratories, Murray Hill, NJ, USA, June 1995.
- [2] G. J. Foschini and M. J. Gans, "On limits of wireless communications in a fading environment when using multiple antennas," *Wireless Personal Communications*, vol. 6, no. 3, pp. 311–335, 1998.
- [3] V. Tarokh, N. Seshadri, and A. R. Calderbank, "Space-time codes for high data rate wireless communication: performance criterion and code construction," *IEEE Transactions on Information Theory*, vol. 44, no. 2, pp. 744–765, 1998.
- [4] V. Tarokh, H. Jafarkhani, and A. R. Calderbank, "Space-time block codes from orthogonal designs," *IEEE Transactions on Information Theory*, vol. 45, no. 5, pp. 1456–1467, 1999.
- [5] S. M. Alamouti, "A simple transmit diversity technique for wireless communications," *IEEE Journal on Selected Areas in Communications*, vol. 16, no. 8, pp. 1451–1458, 1998.
- [6] A. L. Swindlehurst, "Simultaneous channel estimation and decoding for diagonal space-time codes," in *Proc. IEEE Sensor Array and Multichannel Signal Processing Workshop*, pp. 173–177, Cambridge, Mass, USA, March 2000.
- [7] B. L. Hughes, "Differential space-time modulation," *IEEE Transactions on Information Theory*, vol. 46, no. 7, pp. 2567–2578, 2000.
- [8] A. F. Molisch, M. Steinbauer, M. Toeltsch, E. Bonek, and R. S. Thoma, "Capacity of MIMO systems based on measured wireless channels," *IEEE Journal on Selected Areas in Communications*, vol. 20, no. 3, pp. 561–569, 2002.
- [9] K.-K. Wong, R. S.-K. Cheng, K. B. Letaief, and R. D. Murch, "Adaptive antennas at the mobile and base stations in an OFDM/TDMA system," *IEEE Trans. Communications*, vol. 49, no. 1, pp. 195–206, 2001.
- [10] P. Vandenameele, L. Van Der Perre, M. G. E. Engels, B. Gyselinckx, and H. J. De Man, "A combined OFDM/SDMA approach," *IEEE Journal on Selected Areas in Communications*, vol. 18, no. 11, pp. 2312–2321, 2000.
- [11] H. J. Yin and H. Liu, "Performance of space-division multiple-access (SDMA) with scheduling," *IEEE Transactions on Wireless Communications*, vol. 1, no. 4, pp. 611–618, 2002.
- [12] O. Damen, A. Chkeif, and J.-C. Belfiore, "Lattice code decoder for space-time codes," *IEEE Communications Letters*, vol. 4, no. 5, pp. 161–163, 2000.
- [13] M. Costa, "Writing on dirty paper," *IEEE Transactions on Information Theory*, vol. 29, no. 3, pp. 439–441, 1983.
- [14] A. J. Goldsmith and M. Effros, "The capacity region of broadcast channels with intersymbol interference and colored Gaussian noise," *IEEE Transactions on Information Theory*, vol. 47, no. 1, pp. 219–240, 2001.
- [15] G. J. Foschini and A. H. Diaz, "Dirty paper coding: Perturbing off the infinite dimensional lattice limit," in *Multiantenna Channels: Capacity, Coding and Signal Processing*, G. J. Foschini and S. Verdú, Eds., vol. 62 of *DIMACS: Series in Discrete Mathematics and Theoretical Computer Science*, pp. 1052–1798, American Mathematical Society, Providence, RI, USA, 2003.
- [16] G. Caire and S. Shamai, "On the achievable throughput of a multiantenna Gaussian broadcast channel," *IEEE Transactions on Information Theory*, vol. 49, no. 7, pp. 1691–1706, 2003.
- [17] C. Farsakh and J. A. Nossek, "Spatial covariance based downlink beamforming in an SDMA mobile radio system," *IEEE Trans. Communications*, vol. 46, no. 11, pp. 1497–1506, 1998.
- [18] R. Schmalenberger and J. J. Blanz, "Multi antenna C/I balancing in the downlink of digital cellular mobile radio systems," in *Proc. IEEE 47th Vehicular Technology Conference*, vol. 2, pp. 607–611, Phoenix, Ariz, USA, May 1997.
- [19] K.-K. Wong, R. D. Murch, and K. B. Letaief, "Performance enhancement of multiuser MIMO wireless communication systems," *IEEE Trans. Communications*, vol. 50, no. 12, pp. 1960–1970, 2002.
- [20] M. Meurer, P. W. Baier, T. Weber, Y. Lu, and A. Papathanassiou, "Joint transmission: advantageous downlink concept for CDMA mobile radio systems using time division duplexing," *Electronics Letters*, vol. 36, no. 10, pp. 900–901, 2000.
- [21] F. Kowalewski and P. Mangold, "Joint predistortion and transmit diversity," in *Proc. IEEE Global Telecommunications Conference (GLOBECOM '00)*, vol. 1, pp. 245–249, San Francisco, Calif, USA, November-December 2000.
- [22] R. L.-U. Choi and R. D. Murch, "A transmit preprocessing technique for multiuser MIMO systems using a decomposition approach," *IEEE Transactions on Wireless Communications*, vol. 3, no. 1, pp. 20–24, 2004.
- [23] M. Rim, "Multi-user downlink beamforming with multiple transmit and receive antennas," *Electronics Letters*, vol. 38, no. 25, pp. 1725–1726, 2002.
- [24] Q. H. Spencer and M. Haardt, "Capacity and downlink transmission algorithms for a multi-user MIMO channel," in *Proc. 36th Asilomar Conference on Signals, Systems, and Computers*, vol. 2, pp. 1384–1388, IEEE Computer Society Press, Pacific Grove, Calif, USA, November 2002.
- [25] K.-K. Wong, R. D. Murch, and K. B. Letaief, "A joint-channel diagonalization for multiuser MIMO antenna systems," *IEEE Transactions on Wireless Communications*, vol. 2, no. 4, pp. 773–786, 2003.
- [26] K.-K. Wong, "Performance analysis of single and multiuser MIMO diversity channels using Nakagami- m distribution," to appear in *IEEE Transactions on Wireless Communications*.
- [27] Z. G. Pan, K.-K. Wong, and T.-S. Ng, "Generalized multiuser orthogonal space division multiplexing," to appear in *IEEE Transactions on Wireless Communications*.
- [28] L. Zheng and D. N. C. Tse, "Diversity and multiplexing: a fundamental tradeoff in multiple-antenna channels," *IEEE Transactions on Information Theory*, vol. 49, no. 5, pp. 1073–1096, 2003.
- [29] D. Chizhik, G. J. Foschini, M. J. Gans, and R. A. Valenzuela, "Keyholes, correlations, and capacities of multielement transmit and receive antennas," *IEEE Transactions on Wireless Communications*, vol. 1, no. 2, pp. 361–368, 2002.
- [30] A. van Zelst and J. S. Hammerschmidt, "A single coefficient spatial correlation model for multiple-input multiple-output (MIMO) radio channels," in *Proc. 27th General Assembly of the International Union of Radio Science*, Maastricht, The Netherlands, August 2002.
- [31] G. H. Golub and C. F. Van Loan, *Matrix Computations*, The Johns Hopkins University Press, Baltimore, London, 2nd edition, 1989.

Zhengang Pan was born in Haimeng, Jiangsu Province, China, on February 27, 1975. He has received the B.S. (honors with distinction) and M.S. degrees in electronics engineering from Department of Radio, Southeast University, Nanjing City, Jiangsu Province, China, in 1997 and 2000, respectively. From 2000 to 2001, he was a Hardware Engineer at Xuji Automation & Communication Co. Ltd, focusing on the development of ASIC for power line communication. Since January 2001, he was a doctoral candidate at the Department of Electrical and Electronic engineering, The University of Hong Kong. His research interests include high-speed data transmission over wireless link, smart antenna (MIMO) system, OFDM, adaptive modulation and coding, joint spatial and frequency resource allocation, and implementation of communication systems. He is a student member of IEEE.



of Engineering degree by The University of Newcastle, Australia, in August 1997, the Senior Croucher Foundation Fellowship in 1999, and the IEEE Third Millennium Medal in February 2000. He is a Fellow of IEEE, IEE, and HKIE.

Kai-Kit Wong received the B.Eng., M.Phil., and Ph.D. degrees, all in electrical and electronic engineering, from the Hong Kong University of Science and Technology, Hong Kong, in 1996, 1998, and 2001, respectively. Since 2001, he has been with the Department of Electrical and Electronic Engineering, The University of Hong Kong (HKU), where he is a Research Assistant Professor. From 2003 till 2004, he worked as a Visiting Assistant Professor at the Smart Antennas Research Group, Stanford University, and a Visiting Research Scholar at the Wireless Communications Research Department, Lucent Technologies, Bell-Labs, Holmdel. He has worked in several areas including smart antennas, space-time processing/coding, and equalization. Dr. Wong was a corecipient of IEEE Vehicular Technology Society (VTS) Japan Chapter Award of the IEEE VTC2000-Spring, Japan. In 2002 and 2003, he was awarded the SY King Fellowships and the WS Leung Fellowships, respectively, from HKU. Also, he received the Competitive Earmarked Research Grant (CERG) Merit and Incentive Awards from 2003 till 2004. He is a Member of IEEE.



Tung-Sang Ng received the B.S.(Eng.) degree from the University of Hong Kong in 1972, and the M.Eng.Sc. and Ph.D. degrees from the University of Newcastle, Australia, in 1974 and 1977, respectively, all in electrical engineering. He worked for BHP Steel International and the University of Wollongong, Australia, after graduation for 14 years before he returned to The University of Hong Kong in 1991, taking up the position of Professor and Chair of electronic engineering. He was Head of Department of Electrical and Electronic Engineering from 2000 to 2003 and is currently Dean of Engineering. His current research interests include wireless communication systems, spread spectrum techniques, CDMA, and digital signal processing. He has published over 250 international journal and conference papers. He was the General Chair of ISCAS'97 and the VP Region 10 of IEEE CAS Society in 1999 and 2000. He was an Executive Committee Member and a Board Member of the IEE Informatics Divisional Board from 1999 till 2001 and was an ordinary member of IEE Council from 1999 till 2001. He was awarded the Honorary Doctor



Special Issue on Color in Image and Video Processing

Call for Papers

The perception of color has become of increasing importance in application areas such as digital imaging, multimedia, visual communications, computer vision, and consumer electronic industry. Color is considered since the last decade as a key element for a number of image and video processing systems. In particular, color plays a central role in digital photography, consumer electronic devices such as digital cameras, display applications, and printing applications, where color management algorithms are considered as the foundation to transport documents from one system to another. Color also plays a major important role in pattern recognition and multimedia systems, where color-based features and color segmentation have proven pertinent in detecting and classifying objects in biomedical applications and general purpose imagery. In particular, the fusion of color and edge-based features has improved the performance of image segmentation and object recognition. Color is of essential importance in compression-and transmission-based applications of visual content. There are many TV and cinematographic applications where accurate color communication is critical for specialists such as golden eyes and professionals. The motivation of this special issue is to fill the existing gap between academic institutions and research laboratories which deal with the manipulation of digital color images through the utilization of advanced signal processing techniques and practitioners, and research laboratories which deal with the perception of colors through computer vision and human vision.

This special issue will gather high-quality, original contributions on all aspects of the application of color in pattern recognition, computer vision, compression, indexing, multimedia content access, watermarking, and security.

Topics of interest include (but are not limited to) the theory and applications of color in:

- Computational color vision models
- Color constancy and color transfer
- Digital photography
- Postproduction in cinema
- Digital color camera image processing

- Color reproduction (printing, scanning, displays)
- High dynamic range color imaging and rendering
- Color image understanding and analysis
- Color data compression and encoding
- Color image/video indexing and retrieval
- Color image filtering and enhancement
- Digital color image content protection
- Color image/video quality assessment
- Spatiotemporal color modeling
- Multispectral imaging and analysis
- Applications and future trends

Authors should follow the EURASIP Journal on Image and Video Processing manuscript format described at the journal site <http://www.hindawi.com/journals/ivp/>. Prospective authors should submit an electronic copy of their complete manuscripts through the EURASIP Journal on Image and Video Processing Manuscript Tracking System at <http://mts.hindawi.com/>, according to the following timetable:

Manuscript Due	August 1, 2007
First Round of Reviews	November 1, 2007
Publication Date	February 1, 2008

Guest Editors:

Alain Tremeau, Laboratoire LIGIV EA 3070, Université Jean Monnet, 42000 Saint - Étienne, France; tremeau@ligiv.org

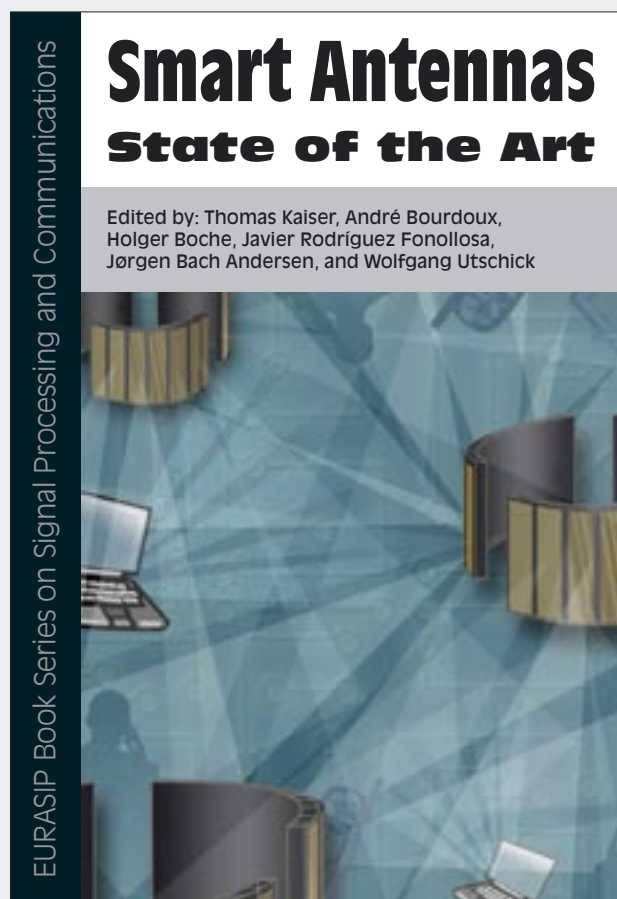
Konstantinos Plataniotis, Department of Electrical and Computer Engineering (ECE), University of Toronto, Toronto, ON, Canada M5S 3G4; kostas@comm.toronto.edu

Shoji Tominaga, Department of Information and Image Sciences, Chiba University, Chiba 263-8522, Japan; shoji@faculty.chiba-u.jp

Smart Antennas—State of the Art

Edited by: Thomas Kaiser, André Bourdoux,
Holger Boche, Javier Rodríguez Fonollosa,
Jørgen Bach Andersen, and Wolfgang Utschick

Limited-Time
Promotional Offer.
Buy this title NOW at
**20% discount plus
Free Shipping.**



Smart Antennas State of the Art

Edited by: Thomas Kaiser, André Bourdoux,
Holger Boche, Javier Rodríguez Fonollosa,
Jørgen Bach Andersen, and Wolfgang Utschick

Smart Antennas—State of the Art brings together the broad expertise of 41 European experts in smart antennas. They provide a comprehensive review and an extensive analysis of the recent progress and new results generated during the last years in almost all fields of smart antennas and MIMO (multiple-input multiple-output) transmission. The following represents a summarized table of contents.

Receiver: space-time processing, antenna combining, reduced rank processing, robust beamforming, subspace methods, synchronization, equalization, multiuser detection, iterative methods

Channel: propagation, measurements and sounding, modelling, channel estimation, direction-of-arrival estimation, subscriber location estimation

Transmitter: space-time block coding, channel side information, unified design of linear transceivers, ill-conditioned channels, MIMO-MAC strategies

Network Theory: channel capacity, network capacity, multihop networks

Technology: antenna design, transceivers, demonstrators and testbeds, future air interfaces

Applications and Systems: 3G system and link level aspects,

MIMO HSDPA, MIMO-WLAN/UMTS implementation issues

This book serves as a reference for scientists and engineers who need to be aware of the leading edge research in multiple-antenna communication, an essential technology for emerging broadband wireless systems.

EURASIP Book Series on SP&C, Volume 3, ISBN 977-5945-09-7

Please visit <http://www.hindawi.com/spc.3.html> for more information about the book. To place an order while taking advantage of our current promotional offer, please contact books.orders@hindawi.com